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WHAT YOU ARE, TAKES YOU FAR

Doctoral Dissertation

Doctoral Program in Computer and Control Engineering (29th cycle)

Frequent Itemset Mining for Big Data

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Politecnico di Torino

2018

Declaration

I hereby declare that, the contents and organization of this dissertation constitute my own original work and does not compromise in any way the rights of third parties, including those relating to the security of personal data.

Fabio Pulvirenti

2018

* This dissertation is presented in partial fulfillment of the requirements for **Ph.D. degree** in the Graduate School of Politecnico di Torino (ScuDo).

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I would like to dedicate this thesis to my loving parents, my sister Martina and my large Sicilian family. Without their support this dream would have not become true. A heartfelt thanks goes out to my girlfriend Giulia, for all her love, support and patience in these intense years.

Abstract

Traditional data mining tools, developed to extract actionable knowledge from data, demonstrated to be inadequate to process the huge amount of data produced nowadays. Even the most popular algorithms related to *Frequent Itemset Mining*, an exploratory data analysis technique used to discover frequent items co-occurrences in a transactional dataset, are inefficient with larger and more complex data.

As a consequence, many parallel algorithms have been developed, based on modern frameworks able to leverage distributed computation in commodity clusters of machines (e.g., Apache Hadoop, Apache Spark). However, frequent itemset mining parallelization is far from trivial. The search-space exploration, on which all the techniques are based, is not easily partitionable. Hence, distributed frequent itemset mining is a challenging problem and an interesting research topic.

In this context, our main contributions consist in an (i) exhaustive theoretical and experimental analysis of the best-in-class approaches, whose outcomes and open issues motivated (ii) the development of a distributed high-dimensional frequent itemset miner. The dissertation introduces also a data mining framework which takes strongly advantage of distributed frequent itemset mining for the extraction of a specific type of itemsets (iii). The theoretical analysis highlights the challenges related to the distribution and the preliminary partitioning of the frequent itemset mining problem (i.e. the search-space exploration) describing the most adopted distribution strategies. The extensive experimental campaign, instead, compares the expectations related to the algorithmic choices against the actual performances of the algorithms. We run more than 300 experiments in order to evaluate and discuss the performances of the algorithms with respect to different real life use cases and data distribu-

tions. The outcomes of the review is that no algorithm is universally superior and performances are heavily skewed by the data distribution. Moreover, we were able to identify a concrete lack as regards frequent pattern extraction within high-dimensional use cases. For this reason, we have developed our own distributed high-dimensional frequent itemset miner based on Apache Hadoop. The algorithm splits the search-space exploration into independent sub-tasks. However, since the exploration strongly benefits of a full-knowledge of the problem, we introduced an interleaving synchronization phase. The result is a trade-off between the benefits of a centralized state and the ones related to the additional computational power due to parallelism. The experimental benchmarks, performed on real-life high-dimensional use cases, show the efficiency of the proposed approach in terms of execution time, load balancing and reliability to memory issues. Finally, the dissertation introduces a data mining framework in which distributed itemset mining is a fundamental component of the processing pipeline. The aim of the framework is the extraction of a new type of itemsets, called misleading generalized itemsets.

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Chapter 1

Introduction

Nowadays, data stream from every-day life. Social networks, wearable devices and cities infrastructure are just few examples of current data sources. The reasons behind the collection of this huge amount of data concern its renovated value. Indeed, the so called *Big Data* revolution does not concern only the increasing quantity of data. The real innovation is related to the actionable knowledge which can be extracted from it [1]. Thanks to the analysis of huge amount of customers' information, currently, many companies are able to develop *predictive models* to target each customer with the proper campaign. *Recommendation systems* are used to propose products to customers relying on the choices of other *similar* customers. By means of municipal data collections, in urban scenarios, crimes are predicted or interesting *correlations* between health and air quality are extracted. The information collected by sensors in the automotive environment, instead, is leveraged in many research domains: from the training of *self-driving algorithms* to *predictive component replacement*.

The branch of computer science whose analytic tools are used to transform these huge collections of data into effective and useful knowledge is called *data mining*. In the last years, the interest towards data mining in Big Data contexts has risen. The trend is noticeable in both industrial and academic environments. For companies, as already discussed, it represents a very powerful source of information. In [2] it is explained how larger data can indeed be more valuable assets for predictive analytics. Companies with larger collections of data and, of course, the skills to take advantage of them, can obtain a competitive advantage.

On the other hand, in the academic domain, the design of big data algorithms represents a very inspiring challenge and research opportunity. In fact, the application of traditional data mining techniques to such large collection of data is very challenging. Furthermore, as the amount of data increases, the proportion that people are able to interpret decreases [3]. For this reason, there is a concrete and urgent need of a new generation of scalable tools.

In this dissertation, we focus on one of the most popular data mining techniques, *Frequent Itemset Mining*. Frequent itemset mining (FIM) is an exploratory data analysis method used to discover frequent co-occurrence among the items of a transactional dataset. Frequent itemsets are very useful for data summarization and correlation analysis. They can be used to identify the most relevant insights from large collections of data which cannot be manually examined because of their size. Itemsets are also used to generate Association Rules [4], which highlight and analyze relations between objects.

Several efficient frequent itemset mining algorithms have been proposed in the last decades. However, they are very efficient when the dataset could be stored in main memory but cannot cope with larger and more complex data. In this context, frequent itemset extraction becomes a challenging and interesting problem. For this reason, some scalable techniques have been introduced in the last years. All of them rely on different distribution strategies and this leads to different performances related to different use cases and data distributions.

Thesis statement: *The target of this dissertation is to thoroughly analyze the distributed frequent itemset mining environment, identify the open issues and make a step forward to fill in the discovered gap.*

In the final part of this Chapter, we resume the dissertation plan highlighting our research contribution.

1.1 Dissertation plan and research contribution

The dissertation is structured into three main parts, which follow the natural order of algorithms design and application. At the same, time, this division organically clusters my main research contributions:

1. A deep analysis of the most reliable frequent itemset mining tools for big data. In every research project, this preliminary effort is fundamental to better understand the domain and, above all, discover possible lacks or issues. This analysis is divided in two main components:
 - (a) A theoretical analysis introducing frequent itemset mining and outlining the motivations and the inherent challenges related to parallelization. Finally, the best-in-class distributed approaches are described.
 - (b) An experimental comparison aimed to compare the performances of the state-of-the-art approaches through different use-cases characterized by different data distribution (using both synthetic and real-life datasets) in order to identify possible open issues.
2. The enrichment of the scalable frequent pattern mining environment with a new distributed high-dimensional mining algorithm.
3. The integration of distributed frequent pattern mining in a real world context and within a big data mining framework.

The remainder part of this section will briefly introduce each phase in order to deliver a clear idea of the structure of the dissertation work.

1.1.1 Frequent Itemset Mining: motivations, challenges and state of the art

As already mentioned, with the increasing amount of generated data, different distributed and scalable frequent itemset algorithms have been developed.

In this section, we will firstly introduce the motivations behind the need of scalable frequent itemset mining algorithms and the current migration

towards the distributed computing frameworks [5, 6]. Since all the distributed approaches and their inherent algorithmic design choices strongly rely on a set of underlying centralized algorithms, the basic frequent itemset mining approaches will be introduced. This knowledge allows a better comprehension of the inherent challenges of parallelization, which will be extensively described. A new taxonomy based on the distribution strategy will be introduced as well. Finally, this section of the work describes how the best-in-class distributed frequent itemset mining approaches have addressed the parallelization issues to extract frequent itemsets from large amount of data.

1.1.2 State of the art experimental evaluation and open issues

The detailed description on the algorithmic choices of the distributed methods for frequent itemset mining is followed by an experimental analysis comparing the performance of state-of-the-art distributed implementations on both synthetic and real datasets. The strengths and weaknesses of the algorithms are thoroughly discussed with respect to the dataset features: e.g., data distribution, average transaction length and number of records. Finally, based on the theoretical and experimental analyses, open research directions for the parallelization of the itemset mining problem are presented. The outcomes of the experimental review is that no algorithm is universally superior and performances are heavily skewed by the use cases and the relative input data. Additionally, the experiments have highlighted the fundamental importance of Load Balancing, even sacrificing Communication Costs, which, in this scenario, could be considered as a price worth paying. All of the algorithms assess their reliability dealing with a huge number of transactions. None of them has been designed to cope with a huge number of attributes, i.e. high-dimensional data. As shown in the next subsection, we have tried to fill in this gap.

1.1.3 A Parallel Map-Reduce Algorithm to Efficiently Support Itemset Mining on High Dimensional Data

As mentioned in the previous subsection (and as clearly shown in Chapter 4), most of the current scalable frequent itemset mining algorithms are designed to cope with low-dimensional datasets, delivering poor performances in those use cases characterized by high-dimensional data. Chapter 5 introduces PaMPa-HD [7],[8], a MapReduce-based frequent closed itemset mining algorithm for high dimensional datasets. An efficient solution has been proposed to parallelize and speed up the mining process. Furthermore, different strategies have been proposed to easily tune-up the algorithm parameters. The experimental results, performed on real-life high-dimensional use cases, show the efficiency of the proposed approach in terms of execution time, load balancing and robustness to memory issues.

1.1.4 Big Data Mining frameworks and real-life scenarios

This section describes the integration of distributed frequent itemset mining in a real world context and, specifically, within a big data mining framework designed to mine a different type of itemsets[9]. The framework includes several steps, all of them relying on distributed processing, in order to be able to deal with large amount of data. In the framework, distributed frequent itemset extraction is just one of the required processes to extract the desired knowledge from raw data. We will specifically focus on the extraction of *misleading generalized itemset* [10], a particular type of itemsets obtained from frequent itemsets and a taxonomy of the input data. In this context, two real life use cases will be analyzed. The first is related to smart cities [10],[11] while the second consists network traffic logs [12].

1.1.5 Dissertation Plan

This dissertation is organized as follows. Chapter 2 introduces the background related to frequent itemset mining and the distributed platforms involved. In

Chapter 3, the problem of distributed frequent itemset mining will be motivated and the main challenges and parallelization strategies will be outlined. After that, a thorough review of the most affirmed solutions will be introduced. In Chapter 4 the performance of the best-in-class approaches will be evaluated through the utilization of synthetic and real datasets, evidencing the current limitation and the open issues of the academic state of the art. Then, in Chapter 5 an innovative distributed algorithm will be presented and evaluated, demonstrating its effectiveness in the context of high-dimensional pattern mining. In Chapter 6 a big data mining framework will be introduced and exploited to obtain a special type of frequent itemsets from network traffic and smart cities datasets. Finally, Chapter 7 summarizes the main results we achieved and provides some future possible work directions.

Chapter 2

Frequent Itemset Mining and distributed frameworks

As already introduced, data mining represents a family of tools and techniques aimed at extracting usable and effective knowledge from collections of data. It is possible to distinguish three main groups of techniques:

- Unsupervised Learning (Clustering) [13]
- Supervised Learning [14]
- Frequent Itemset Mining and Correlation Discovery [15]

The goal of clustering and, more in general, unsupervised learning, is to discover hidden structures in unlabeled data. Specifically, the aim of this set of techniques is grouping sets of objects in such a way that objects grouped together (in the same cluster) are more similar to each other than to those in other groups (clusters). The greater the homogeneity inside a group and the dissimilarity among different groups, the better the clustering results can be considered. The division into groups can be seen as an attempt to get the natural structure of the data.

Supervised Learning, instead, starting from a set of labeled input data, aims at building a predictive model from it. This model, which is an inferred function, should approximate the distribution of the input dataset, called training set, with respect to the class labels. The built model is then used to classify new unlabeled samples.

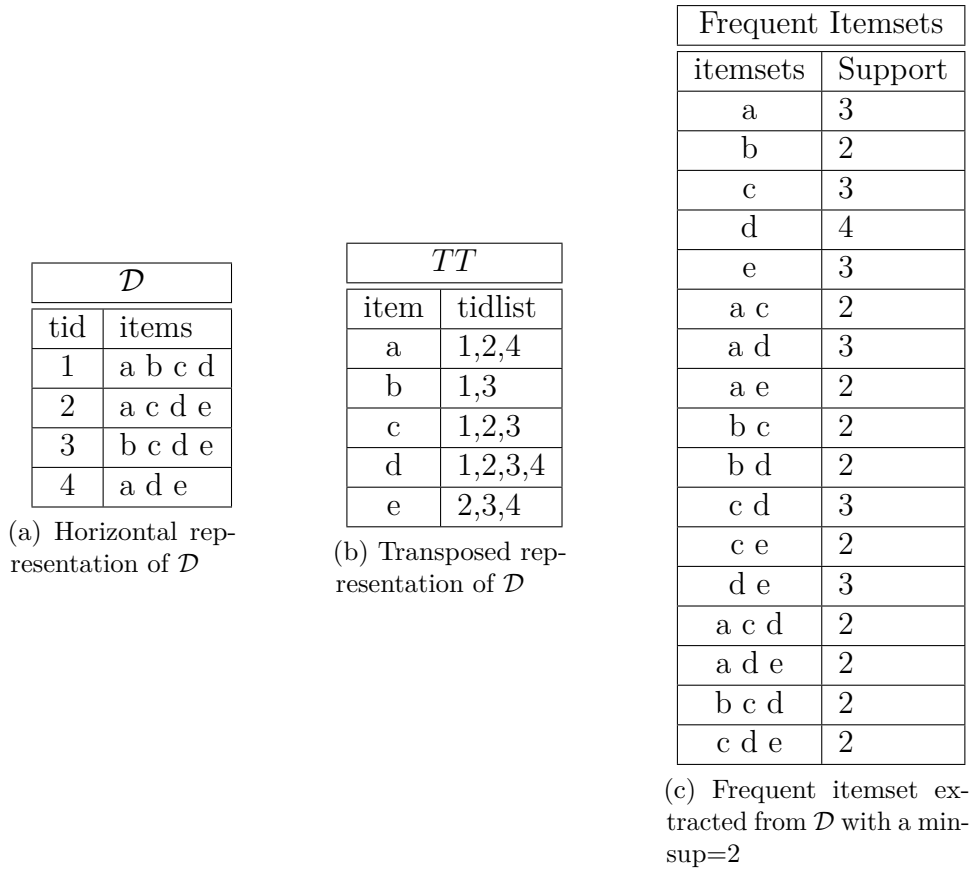
Frequent itemset mining is an exploratory data analysis method used to discover frequent co-occurrence among the items of a transactional dataset (attribute-value pairs). The support of an itemset, a set of items, is the number of transactions in which it appears. A set of items is considered frequent if its support is over a user-provided frequency threshold (minimum support). Frequent itemsets are commonly used to summarize large collection of data since they output the most frequent patterns, which can be interpreted as the most representative ones [16]. In a similar way, they can be leveraged to highlight patterns which do not respect the most common trend [17],[18]. They can hide interesting outliers which could worth be investigated and deepened [19],[20]. Frequent itemsets are often used as input for Association rules mining, a method to discover interesting relations between objects. They were first introduced analyzing retail transactions data from supermarkets. Each rule is organized on two members, respectively called antecedent and consequent. The rule concept is very straightforward and an example rule is: $\{bread, butter\} \rightarrow \{milk\}$. This rule means that customers who buy bread and butter usually buy also milk. Of course, the rules should be considered statistically significant just if supported by a sufficient support and confidence (i.e. how often the rule has been found to be true). Association rules and, in general, the extracted knowledge in terms of correlations, could be considered very valuable information. For instance, a whole category of classifier or recommendation systems are based on rules [21],[22].

In the following Section, a preliminary background on frequent itemset mining, useful to better understand the content of this work, will be introduced.

2.1 Frequent Itemset Mining - Preliminaries

Let \mathcal{I} be a set of items. A transactional dataset \mathcal{D} consists of a set of transactions $\{t_1, \dots, t_n\}$, where each transaction $t_i \in \mathcal{D}$ is a set of items (i.e., $t_i \subseteq \mathcal{I}$) and it is identified by a transaction identifier (tid_i). Figure 2.1a reports an example of a transactional dataset with 4 transactions.

An itemset I is defined as a set of items (i.e., $I \subseteq \mathcal{I}$) and it is characterized by a tidlist and a support value. The tidlist of an itemset I , denoted by $tidlist(I)$, is defined as the set of tids of the transactions in \mathcal{D} containing I .

Fig. 2.1 Running example dataset \mathcal{D}

When the average number of items per transactions is orders of magnitudes larger than the number of transactions, a transactional dataset can also be more effectively represented in a vertical format. In this representation, also called *transposed table* TT , each row consists of an item I and its list $tidlist(I)$. Figure 2.1b reports the transposed representation of the running example reported in Figure 2.1a.

The support of I in \mathcal{D} , denoted by $sup(I)$, is defined as the ratio between the number of transactions in \mathcal{D} containing I and the total number of transactions in \mathcal{D} (i.e., $|tidlist(I)|/|\mathcal{D}|$). For instance, the support of the itemset $\{acd\}$ in the running example dataset \mathcal{D} is $2/4$ and its tidlist is $\{1,2\}$. An itemset I is considered frequent if its support is greater than a user-provided minimum support threshold $minsup$. Figure 2.1c reports the frequent itemset extracted from \mathcal{D} with a minsup value equal to 2.

Given a transactional dataset \mathcal{D} and a minimum support threshold $minsup$, the frequent itemset mining [23] problem consists in extracting the complete set of frequent itemsets from \mathcal{D} .

The dimension of the search-space, which can be represented as a lattice with an empty set at the top and an itemset containing all the possible itemset at the bottom, scales exponentially with the number of items [24]. The main underlying property adopted by most of the algorithms to prune the search-space is the monotonicity of the support. Because of this property, if an itemset is infrequent, none of its supersets could be frequent. In Figure 2.2, it is shown the lattice related to our running example.

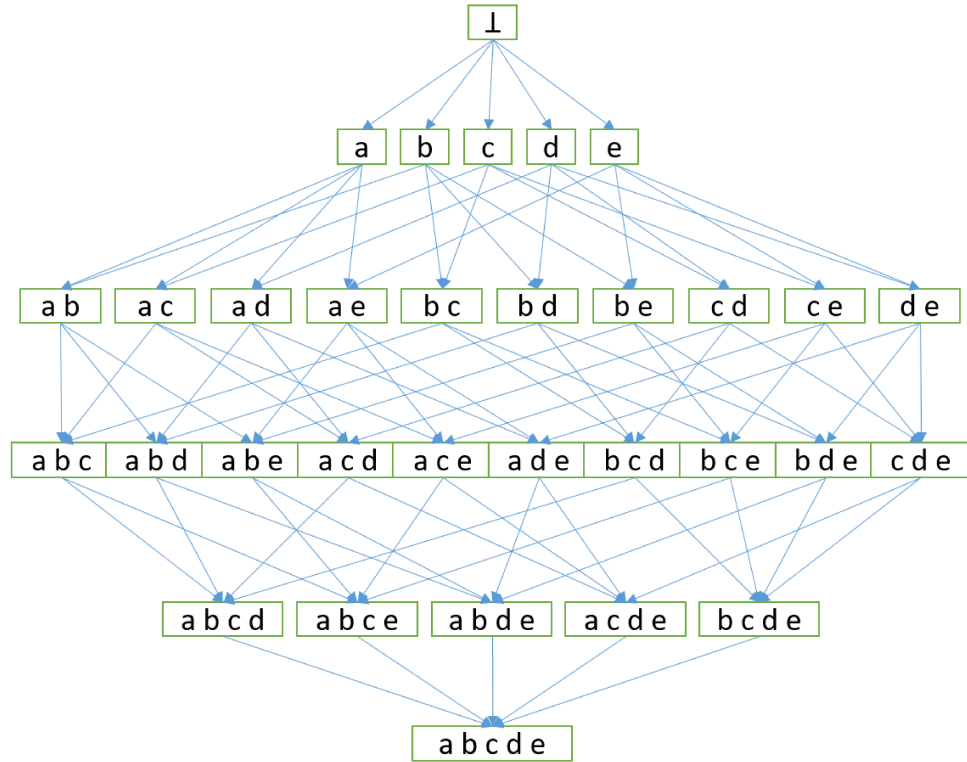
In this work, we focus also on a valuable subset of frequent itemsets called frequent closed itemsets [25]. Closed itemsets allow representing the same information of traditional frequent itemsets in a more compact form. An item or itemset I is closed in \mathcal{D} if none of the supersets of I has the same support count as I .

For instance, in our running example, given a $minsup = 2$, the itemset $\{ac\}$ is a frequent itemset (support=2), but it is not closed for the presence of the itemset $\{acd\}$ (support=2); the itemset $\{ad\}$ (support=3), instead, is closed.

2.2 Big Data and Distributed Frameworks

Today's shift towards horizontal scaling in hardware has highlighted the need of distributed data mining algorithms. Indeed, being able to analyze big data is a huge value from both an economic and social point of view. Unfortunately, traditional tools have demonstrated to be not reliable for dealing with such large amount of data. This subsection introduces the distributed frameworks which have allowed the design of scalable data mining and frequent itemset mining algorithms.

Starting from data storage, new solutions had to be developed to replace traditional relational database managements systems. We have firstly witnessed the development of distributed file systems such as Google File System [26] and its derivative Hadoop Distributed File System [5]. For the computational issues, already well-known parallel frameworks have shown their limitations due to

Fig. 2.2 Lattice representing the search-space of \mathcal{D}

fault tolerance and resiliency lacks. In the meanwhile, new processing models spread out. MapReduce [27] is the most popular example of a generic batch-oriented distributed paradigm. With its reliable and fault-tolerant architecture, it allows to exploit the resources of more commodity machines (nodes). The ratio behind the spread of the paradigm is that 'shifts the computation to the data'. In fact, taking advantage of the data locality, allows the nodes to process just the shard of the data they store.

A MapReduce application consists of two main phases. In the first phase, called "map", each shard of the dataset is processed locally by each node of the commodity clusters, which output one or more key-values couples. Map results are exchanged among the cluster nodes and aggregate the tuples per key: this is the "shuffle" phase. This operation, which is strongly optimized, is one of the killer feature which a MapReduce-like algorithm should strongly exploit (it is also the unique communication among the nodes of the commodity cluster).

Finally, the reduce phase is run for each unique key and iterates through all the associated values.

Designed to cope with very large datasets, the Java-based framework Hadoop [5] is the most widely adopted MapReduce implementation. It allows programmers not to concern about low level details and to focus just on the algorithm design.

However, Hadoop and MapReduce paradigm is not aimed for iterative processes. In this case, each iteration would require a complete read and transmission (shuffle phase) of the input dataset, which is critical when dealing with huge datasets. This issue motivated the development of a new in-memory distributed platform called Apache Spark [6]. This framework, when possible, allows machines to cache data and intermediate results in memory, instead of reloading it from the disk at each iteration. Spark has also introduced a new type of data collection called RDD (Resilient Distributed Dataset). Every RDD modification is done just by the generation of another RDD, keeping track of all the transformations in order to be able to regenerate data in case of failures. Furthermore, RDDs avoid on-disk materialization until not strictly mandatory, i.e. when an action requires a result to be returned to the driver program, saving resources in terms of communication and I/O costs. Spark supports both graph-based and streaming processes, demonstrating to be more flexible than Hadoop, still keeping full compatibility with the latter.

Because of the winning features of Hadoop and Spark, testified by their spread in the academic environment, in this dissertation we will focus onto these distributed frameworks, analyzing the best-in-class Hadoop and Spark-based works and utilizing their paradigm for further advancements of the state of the art.

However, Hadoop and Spark are not the only frameworks supporting the parallelization of Data mining algorithms. GraphLab [28], Google Pregel [29] and its open-source counterpart Giraph [30] are fault-tolerant, graph-based framework while SimSQL [31], for instance, exploits an SQL-based approach. Distributed systems are popular also because they became very easy to use: as already stated, Message Passing Interface (MPI) [32], one of the most adopted framework in academic environment, works efficiently only on very low level programming such as C.

2.2.1 Hadoop and Spark Machine Learning Libraries

In recent years the success of these distributed platforms was supported by the introduction of open source libraries of machine learning algorithms. Mahout [33] for Hadoop has represented one of the most popular collection of Machine Learning algorithms, containing implementations in the areas such as clustering, classification, recommendation systems, etc. All the current implementations are based on Hadoop MapReduce. MADlib [34], instead, provides a SQL toolkit of algorithms that run over Hadoop. Finally,

MLlib [35] is the Machine Learning library developed on Spark, and it is rapidly growing up. MLlib allows researchers to exploit Spark special features to implement all those applications that can benefit from them, e.g. fast iterative procedures.

Chapter 3

FIM and Big Data: motivations, challenges and state of the art

As already mentioned, existing data mining algorithm revealed to be very efficient on typical datasets but very resource intensive when the size of the input dataset grows up [36]. In general, applying data mining techniques to big data collections has often entailed to cope with computational costs that represent a critical bottleneck. For this reason, in the last years many distributed data mining algorithms have been developed and widely exploited in different application domains (e.g., network traffic data [37], healthcare [38], biological data [39], energy data [40], images [41], open linked data [42], document and data summarization [43–45]).

In this section, we will firstly introduce the reasons behind the need of scalable frequent itemset mining algorithms and the current migration towards the distributed computing frameworks (e.g., Apache Hadoop [5], Apache Spark [6]). Then, the most popular centralized approach will be introduced to better understand the inherent challenges of parallelization. Finally, this section will extensively describe the main issues related to the distribution of frequent itemset mining problem and how the best-in-class distributed frequent itemset mining approaches have addressed them.

The contents of this chapter have been presented in [46] and [47] and are organized as follows. Section 3.1 outlines the motivations behind the need of distributed frequent itemset mining algorithms. Section 3.2 provides a

brief description of the state-of-the-art centralized itemset mining algorithms. Section 3.3 describes the algorithmic strategies adopted so far to partition and parallelize the frequent itemset mining problem by means of the MapReduce paradigm, while Section 3.4 describes the state-of-the-art distributed algorithms and their implementations.

3.1 Motivations

Several traditional centralized mining algorithms have been proposed (detailed in Section 3.2). They are very efficient when the datasets can be completely loaded in main memory. However, they cannot cope with larger and more complex data. For this reason, in the last years, different distributed approaches have been introduced, able to perform the itemsets extraction even in cases related to large amount of data. This work is focused on the MapReduce-based approaches. In fact, Hadoop and Spark have been widely adopted in the research environment [48, 49, 1]. The reasons are partly related to the easier data management and better fault tolerance [50, 50, 51] but, above all, these frameworks allow the development of parallel algorithms by unexperienced users [48].

The need of distributed frequent itemset miner is motivated by different factors.

Input data size. The first, obviously, is the amount of data to process. This issue is strongly related to the data structures (e.g., FP-tree [52], Enumeration Tree [25], Prefix Tree [53], ...) leveraged by the algorithms to explore the search-space. Generally, bigger datasets lead to more complex data structures which require a larger amount of computational resources and memory to be explored and maintained¹. Hence, centralized approaches could easily fail to process very large datasets.

On the other hand, frequent itemset mining is a technique that is often leveraged to summarize large data collections, hard to be manually explored by

¹Please note that in the cases characterized by different data size but same data distribution and **relative** minimum support threshold, the data structures are very similar. In these case, the hardest part is related to the steps required to build the data structure (I/O costs) when the input size becomes challenging.

a domain expert. Therefore, in the cases related to big data collections there is even a greater need of reliable frequent itemset miners.

Minimum support threshold. The second issue is related to minimum support threshold, which directly mirrors the depth of the analysis. Even for datasets not belonging to big data environment, a very low support extraction could require a huge amount of resources. The lower it is, the more challenging in terms of resource the mining will be. It is likely that a frequent itemset miner is easily able to complete the itemsets extraction with a minimum support threshold and runs out of memory with a lower support. Even in this case, the motivations are related to the inner structure used by the algorithms to explore the search-space [24]. A low minimum support threshold leads to a deeper exploration of the search-space. The extreme case is the generation and testing of all the possible combinations of the items. The mining considers any possible items co-occurrence and it may happen that the output of the process exceeds the input data size (as clearly shown in Tables 2.1a and 2.1c). In addition, please note that the size and the complexity of these structure do not scale linearly with the minimum support threshold [23, 24]. For these reasons, this parameter is very important in order to evaluate the performance of a frequent itemset mining algorithm.

In [54] it is shown how low frequencies itemsets could be more interesting. A very low minimum support threshold might be also needed in the cases in which frequent itemset mining is just a step in a more comprehensive framework. In these cases it might be convenient to extract as many itemsets as possible. An example of this type of usage can be found in Section 6.5, where frequent itemsets are used to mine misleading generalized itemsets. The counter-effect of low-minsup itemset and association rule extraction is the quantity of generated itemset/rules. In these cases, many efforts have been spent by the community to automatically reduce the amount of patterns or rules generated by a low minsup value, with the introduction of different interestingness indexes and statistical measures. However, most of these measures [55–59] could be applied after the actual itemset mining. Besides, only a few guarantee the downward/upward closure property, allowing them to replace the support-based pruning to reduce the search-space [60–63]. In conclusion, there is still a clear need for techniques able to extract low support itemsets even with large amount of data.

Data distribution. As we will see in Chapters 4 and 5, also input data distribution has an impact on the search-space. A high average transaction length strongly impacts the complexity of the search-space, and, therefore, the data structure to explore and maintain [24]. A dense dataset tends to produce more frequent itemset because a larger number of items per transaction inherently leads to a higher number of co-occurrences.

It is clear how the large amount of input data to be processed is only one of the factors affecting the frequent itemset extraction, which is strongly influenced also by the depth of the analysis (i.e. minimum support threshold) and the data distribution.

3.2 Centralized algorithms

The search-space exploration strategies of the distributed approaches (described in Section 3.3) are often inspired by the solutions adopted by the centralized approaches. Hence, this section shortly introduces the main strategies of the centralized itemset mining algorithms. This introduction is useful to better understand the algorithmic choices behind the distributed algorithms.

The frequent itemset mining task is challenging in terms of execution time and memory consumption because the size of the search-space is exponential with the number of items of the input dataset [24]. Two main search-space exploration strategies have been proposed: (i) level-wise or breadth-first exploration of the candidate itemsets in the lattice and (ii) depth-first exploration of the lattice.

The most popular representative of the breadth-first strategy is Apriori [64]. Starting from single items, it iteratively generates and counts the support of the candidate itemsets of size $k+1$ from the frequent itemsets of size k . Specifically, at each iteration k , the supports of the candidate itemsets of length k are counted by performing a new scan of the input dataset. Then, the set of $k+1$ candidates are generated and tested against the whole dataset, in an iterative fashion. At each iteration, the search-space is pruned by exploiting the downward-closure property, which guarantees that all the supersets of an infrequent itemset are infrequent too. Precisely, the downward-closure property

allows pruning the set of candidate itemsets of length $k + 1$ by considering the frequent itemsets of length k . The Apriori algorithm is significantly affected by the density of the dataset. The higher the density of the dataset, the higher the number of frequent itemsets and hence the amount of candidate itemset stored in main memory. The problem becomes unfeasible when the number of candidate itemsets exceeds the size of the main memory.

More efficient and scalable solutions exploit the depth-first visit of the search-space. FP-Growth [52] is the most popular and it relies on a tree-based compressed representation of the input dataset. Briefly, the algorithm is divided in two main logical phases. In the first, the data structure is built while in the second the frequent itemsets are extracted, the problem is projected with respect to a prefix of items and the algorithm is recursively invoked on the subproblem, following a “divide and conquer” approach. In the first phase, the support of each single item is counted and only the frequent items are stored in the “frequent items table” (F-list), ranked by their support. This step allows to prune the search-space by avoiding the analysis of the itemsets obtained from infrequent items (which cannot be frequent because of the monotonicity of the support). Then, the FP-tree, the base data structure on which the algorithm relies, is built exploiting the input dataset and the F-list table. Specifically, each transaction is included in the FP-tree by adding or extending a path on the tree, exploiting common prefixes. Paths can overlap when transactions share items (i.e. when they share the same prefix). The FP-tree is a compact representation of the dataset and the compression with respect to the original dataset is proportional to the number of paths that overlap. The tree is built together with a Header table which stores, for each frequent item, its support and a pointer to the first node in the FP-tree carrying the same item name. Once the FP-tree associated with the input dataset is built, FP-growth scans the Header table and, for each frequent item or *prefix* p , generates the conditional pattern-base with respect to p (this set matches the projection with respect to p of the dataset transactions). On this set, the FP-growth algorithm is invoked again, following a depth-first exploration. Each iteration generates a new conditional FP-tree with respect to the incremental projection, until the resulting one is empty or contains only a single path. At this point, the search backtracks to the previous level of exploration until all the projections of the initial FP-tree are processed. Further details on FP-growth algorithm

can be found in [52]. FP-growth suits well dense datasets, because they can be effectively and compactly represented by means of the FP-tree data structure. Differently, with sparse datasets, the compressions benefits of the FP-tree are reduced because this would lead to a higher number of branches [15] (i.e., a large number of subproblems to generate and results to merge).

Another very popular depth-first approach is the Eclat algorithm [53]. It performs the mining from a vertical transposition of the dataset. In the vertical format, each transaction includes an item and the transaction identifiers (*tid*) in which it appears (*tidlist*). After the initial dataset transposition, the search-space is explored in a depth-first manner, similarly to FP-growth. The algorithm is based on equivalence classes (groups of candidate itemsets sharing a common prefix). An equivalence class of k -itemsets is a set of all k -itemsets having a prefix of $k-1$ items in common. Itemsets of the same equivalence class could be smartly merged to obtain the itemset containing the prefix and the two distinguishing items. The support of the itemset is obtained from the intersection of the *tidlists*. Prefix-based equivalence classes are mined independently, in a “divide and conquer” strategy. From each equivalence class it is possible to obtain all the itemsets sharing the prefix. The process starts with an empty prefix and the initial search sub-tree is actually the whole search-tree. Then the first item is selected and used to generate the corresponding equivalence class. After the mining of the itemsets containing the former item (itemsets), the prefix is expanded with another item.

Eclat is relatively robust to dense datasets. It is less effective with sparse distributions, because the depth-first search strategy may require generating and testing more (infrequent) candidate itemsets with respect to Apriori-like algorithms [65].

3.3 Itemset mining parallelization strategies

The parallelization of the mentioned data structures represents the main contribution behind the development of distributed and parallel frequent itemset mining algorithms. This set of techniques cannot be considered easily or *embarrassingly* parallelizable and do not fit parallel and/or distributed implementations. In distributed and parallel domains, an ideal approach assumes

to divide the problem into independent non-overlapping sub-problems, which can be assigned to commodity cluster nodes [66, 67]. In this way, (i) the resources are completely exploited and (ii) the communication costs, a concrete bottleneck in distributed environment, are reduced as much as possible.

In the FIM environment, the main task to be parallelized is the search-space exploration, which is achieved through ad-hoc data structures. Distributed FIM algorithms smartly split and distribute the processing of these data structures, most of them adopting a "divide and conquer" fashion. This technique overcomes the main memory issues. However, this split is often sub-optimal:

- In order to guarantee the independency of the single mining task, the set of resulting partitions could overlap ². The presence of overlapping partitions requires an increasing amount of memory in the commodity cluster, storing redundant data [33],[7] which can lead to redundant and useless itemsets [68],[7].
- In centralized algorithms, some pruning techniques are often used to limit the search-space exploration, saving time and resources. However, these pruning rules might assume a state centralized memory. In [7], we have addressed this issue, introducing a trade-off among the benefits related to a centralized memory ("state") and the ones related to the degree of parallelization (i.e. number of independent parallel tasks) (further details in Chapter 5).

The best-in-class MapReduce-based algorithms have addressed the challenges related to parallel frequent itemset mining by means of two main algorithmic approaches. They are significantly different because (i) they use different solutions to split the original problem in subproblems and (ii) make different assumptions about the data that can be stored in the main memory of each independent task.

Data split approach. It splits the problem in "similar" subproblems, executing the same function on different data chunks. Specifically, each subproblem computes the local supports of all candidate itemsets on one chunk on the input dataset (i.e., each subproblem works on the

²The overlapping degree is dependent from the data distribution

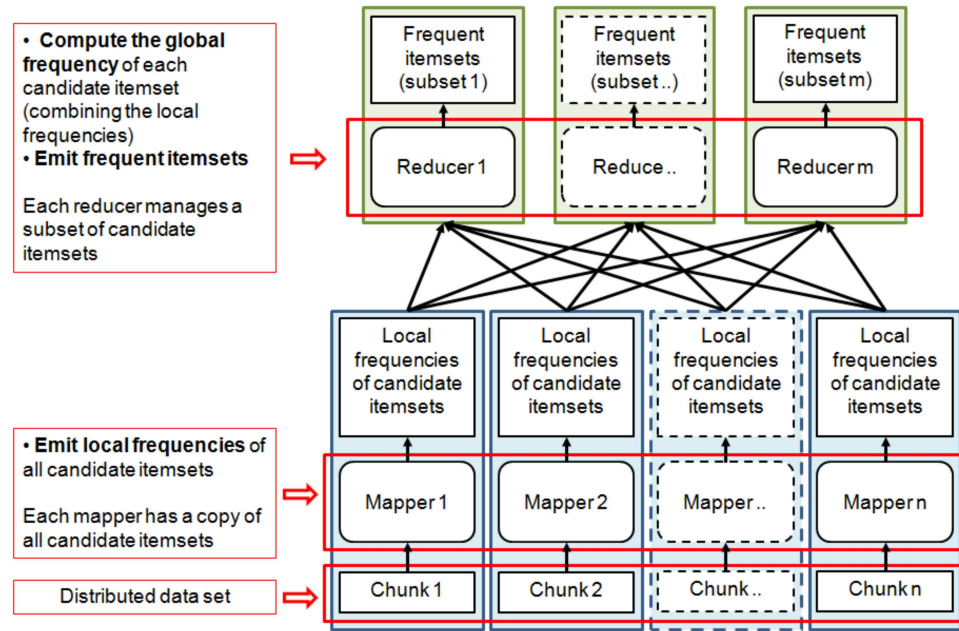


Fig. 3.1 Itemset mining parallelization: Data split approach

complete search-space but on a subset of the input data). Finally, the local results (i.e., the local supports of the candidate itemsets) emitted by each subproblem/task are merged to compute the global final result (global support of each itemset). The main assumptions of this approach are that (i) the problem can be split in “similar” subproblems working on different chunks of the input data and (ii) the set of candidate itemsets is small enough that it can be stored in the main memory of each task.

Search-space split approach. It splits the problem by assigning to each subproblem the visit of a subset of the search-space (i.e., each subproblem visits a part of the lattice). Specifically, this approach generates, from the input distributed dataset, a set of projected datasets, each one small enough to be stored in the main memory of a single task. Each projected dataset contains all the information that is needed to extract a subset of itemsets (i.e., each dataset contains all the information that is needed to explore a part of the lattice) without needing the contribution of the results of the other tasks. The final result is the union of the itemset subsets mined from each projected dataset.

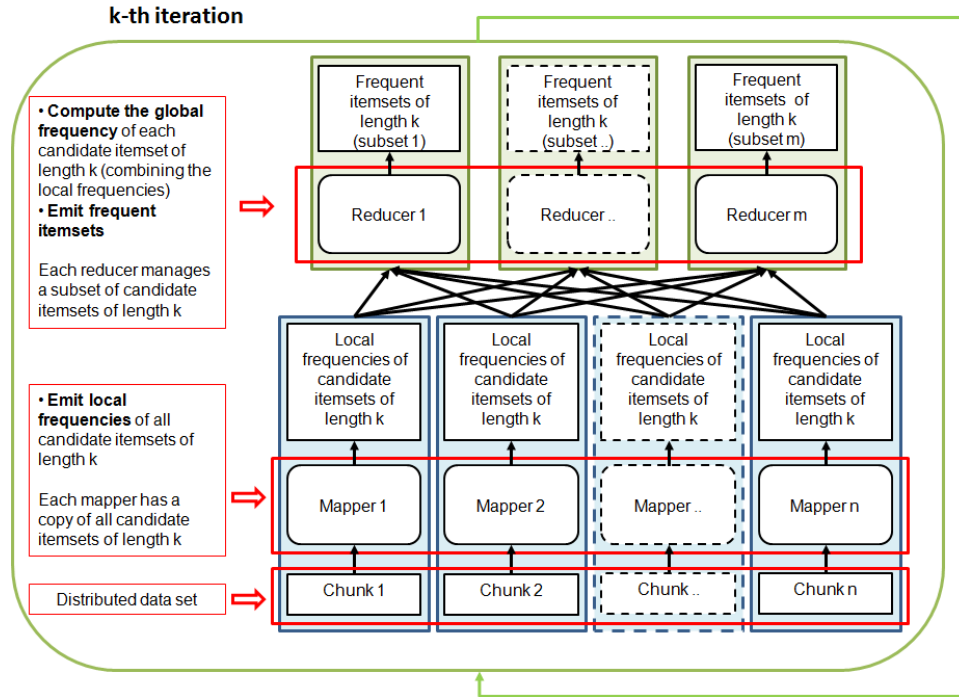


Fig. 3.2 Itemset mining parallelization: Iterative Data split approach

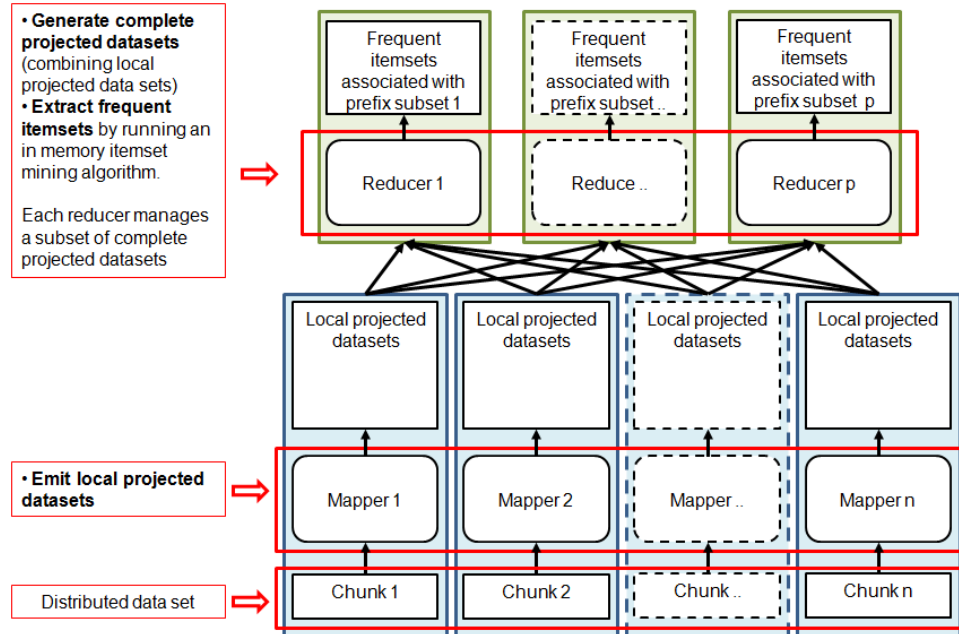


Fig. 3.3 Itemset mining parallelization: Search-space split approach

Figures 3.1 and 3.3 depict the first and the second parallelization strategies, respectively. In the data split approach (Figure 3.1), the map phase computes

the local supports of the candidate itemsets in its data chunk (i.e., each mapper runs a “local itemset mining extraction” on its data chunk). Then, the reduce phase merges the local supports of each candidate itemset to compute its global support. This solution requires each mapper to store a copy of the complete set of candidate itemsets (i.e., a copy of the lattice). This set must fit in the main memory of each mapper. Since the complete set of candidate itemsets is usually too large to be stored in the main memory of a single mapper, an iterative solution, inspired by the level-wise centralized itemset mining algorithms, is used. Figure 3.2 reports the iterative solution. At each iteration k only the subset of candidates of length k are considered and hence stored in the main memory of each mapper. This approach, thanks also to the exploitation of the apriori-principle to reduce the size of the candidate sets, allows obtaining subsets of candidate itemsets that can be loaded in the main memory of each mapper.

In the search-space split approach (Figure 3.3), the main idea is to create several independent projected dataset that can be mined in parallel in different tasks. The map phase is therefore used for dividing or mapping the initial dataset into several sub-shards which, if smartly aggregated, could be explored and mined independently. Precisely, from the local data chunks of the initial dataset, the mappers generate a set of local projected datasets. Each local projected dataset is the projection of the input chunk with respect to a prefix p .³ Then, the reduce phase merges the local projected datasets to generate the complete projected datasets (the transactions related to the same prefix p , in fact, could be contained in different data chunks). The aggregated projected datasets are provided as input to the reducers. Each reducer, then, runs a standard centralized itemset mining algorithm on the provide projected datasets, extracting the relative set of frequent itemsets. Hence, the main assumption, in this approach, is that each complete projected dataset must fit in the main memory of a single reducer.

Table 3.1 summarizes the main characteristics of the two parallelization approaches with respect to the following criteria: type of split of the problem, usage of main memory, communication costs, load balancing, and maximum parallelization (i.e. maximum number of mappers and reducers).

³Note that the projected datasets can overlap because the transactions associated with two distinct prefixes p_1 and p_2 can be overlapped.

Table 3.1 Comparison of the parallelization approaches.

Criterion	Iterative data split approach (Figure 3.2)	Search-space split approach (Figure 3.3)
Type of split/Split of the search-space	Each subproblem analyzes a different subset of the input data and computes the local supports of all the candidate itemsets of length k on its chunks of data. The final result is given by the merge of the local results.	Each subproblem analyzes a different subset of itemsets/a different part of the search-space. The final result is the union of the local results.
Usage of main memory	The candidate set of length k is stored in the main memory of a single task.	The complete projected dataset is stored in the main memory of a single task.
Communication cost	Number of candidate itemsets \times number of mappers \times number of iterations.	Sum of the sizes of the local projected datasets.
Load balancing	Load balancing is achieved by associating the same number of itemsets to each reducer.	The tasks could be significantly unbalanced depending on the characteristics of the projected datasets assigned to each node.
Maximum number of mappers	Number of chunks	Number of chunks
Maximum number of reducers	Number of candidate itemsets	Number of items

Type of split/Split of the search-space. The main difference between the two parallelization approaches is the strategy adopted to split the problem in subproblems. This choice has a significant impact on the other criteria.

Usage of main memory. The different usage of the main memory of the tasks impact on the reliability of the two approaches. The data split approach assumes that the candidate itemsets of length k can be stored in the main memory of each mapper. Hence, it is not able to scale on dense datasets characterized by large candidate sets. Differently, the search-space split approach assumes that each complete projected dataset can be stored in the main memory of a single task. Hence, this approach runs out of memory when large complete projected datasets are generated.

Communication costs. In a parallel MapReduce algorithm, communication costs are important, because the network can easily become the bottleneck if large amounts of data are sent on it. The communication costs are mainly related to the outputs of the mappers which are sent to the reducers on the network. For the data split approach the data that is sent on the network is linear with respect to the number of candidate itemsets, the number of mappers, and the number of iterations. Differently, for the search-space approach, the amount of data emitted by the mappers is equal to the size of the projected datasets.

Load balancing. The different split of the problem in subproblems significantly impacts on load balancing. For the data split approach, the execution time of each mapper is linear with respect to the number of input transactions and the execution time of each reducer is linear with respect to the number of assigned itemsets. Hence, the data split approach can easily achieve a good load balancing by assigning the same number of data chunks to each mapper and the same number of candidate itemsets to each reducer. Differently, the search-space split approach is potentially unbalanced. In fact, each subproblem is associated with a different subset of the lattice, related to a specific projected dataset and prefix, and, depending on the data distribution, the complexity of the subproblems can significantly vary. A smart assignment of a set of subproblems to each node would mitigate the unbalance. However, the complexity of the subproblems is hardly inferable during the initial assignment phase.

The two parallelization approaches are used to design efficient parallel implementations of well-known centralized itemset mining algorithms. Specifically, the data split approach is used to implement the parallel versions of level-wise algorithms (like Apriori [64]), whereas the search-space split approach is used to implement parallel versions of depth-first recursive approaches (like FP-growth [52] and Eclat [53]).

3.4 Distributed itemset mining algorithms

This section describes the algorithms, and available implementations, representing the state-of-the-art solutions in the parallel frequent itemset mining context. We considered the following algorithms: YAFIM [69], PFP [36], BigFIM [68], and DistEclat [68]. The only algorithm which is lacking a publicly available implementation is YAFIM. Among the considered algorithms, YAFIM belongs to the ones based on the data split approach, while PFP and DistEclat are based on the search-space split approach. Finally, BigFIM mixes the two strategies, aiming at exploiting the pros of them. For PFP we selected two popular implementations: Mahout PFP and MLib PFP, which are based on Hadoop and Spark, respectively. The description of the four selected algorithms and their implementations are reported in the following subsections.

3.4.1 YAFIM

YAFIM [69] is an Apriori distributed implementation developed in Spark. The iterative nature of the algorithm has always represented a challenge for its application in MapReduce-based Big Data frameworks. The reasons are the overhead caused by the launch of new MapReduce jobs and the requirement to read the input dataset from disk at each iteration. YAFIM exploits Spark RDDs to cope with these issues. Precisely, it assumes that all the dataset can be loaded into an RDD to speed up the counting operations. Hence, after the first phase in which all the transactions are loaded in an RDD, the algorithm starts the iterative Apriori algorithm organizing the candidates in a hash tree to speed up the search. Being strongly Apriori-based, it inherits the breadth-first strategy to explore and partition the search-space and the preference towards sparse data distributions. YAFIM exploits the Spark “broadcast variables abstraction” feature, which allows programmers to send subsets of shared data to each slave only once, rather than with every job that uses those subset of data. This implementation mitigates communication costs (reducing the inter job communication), while load balancing is not addressed.

3.4.2 Parallel FP-growth (PFP)

Parallel FP-growth [36], called PFP, is a distributed implementation of FP-growth that exploits the MapReduce paradigm to extract the k most frequent closed itemsets. It is included in the Mahout machine learning Library (version 0.9) and it is developed on Apache Hadoop. PFP is based on the search-space split parallelization strategy reported in Section 3.3. Specifically, the distributed algorithm is based on building independent FP-trees (i.e., projected datasets) that can be processed separately over different nodes.

The algorithm consists of 3 MapReduce jobs.

First job. It builds the F-list Table, which is used to select frequent items, in a MapReduce “Word Count” manner.

Second job. In the second job, the mappers project with respect to group of items (prefixes) all the transactions of the input dataset to generate the local projected contributions to the projected datasets. Then, the reducers aggregate the projections associated with the items of the same group and build

independent complete FP-trees from them. Each complete FP-tree is managed by one reducer, which runs a local main memory FP-growth algorithm on it and extracts the frequent itemsets associated with it.

Third job. Finally, the last MapReduce job selects the top k frequent closed itemsets.

The independent complete FP-trees can have different characteristics and this factor has a significant impact on the execution time of the mining tasks. As discussed in Section 3.3, this factor significantly impacts on load balancing. Specifically, when the independent complete FP-trees have different sizes and characteristics, the tasks are unbalanced because they addresses subproblems with different complexities. This problem could be potentially solved by splitting complex trees in sub-trees, each one associated with an independent subproblem of the initial one. However, defining a metric to split a tree in such a way to obtain sub-mining problems that are equivalent in terms of execution time is not easy. In fact, the execution time of the itemset mining process on an FP-Tree is not only related to its size (number of nodes) but also to other characteristics (e.g., number of branches and frequency of each node). Depending on the dataset characteristics, the communication costs can be very high, especially when the projected the datasets overlap significantly because in that case the overlapping part of the data is sent multiple times on the network.

Spark PFP [35] represents a pure transposition of PFP to Spark. It is included in MLlib, the Spark machine learning library. The algorithm implementation in Spark is very close to the Hadoop sibling. The main difference, in terms of addressed problem, is that MLlib PFP mines all the frequent itemsets, whereas Mahout PFP mines only the top k closed itemsets.

Both implementations, being strongly inspired by FP-growth, keep from the underlying centralized algorithm the features related to the search-space exploration (depth-first) and the ability to efficiently mine itemsets from dense datasets.

3.4.3 DistEclat and BigFIM

DistEclat [68] is a Hadoop-based frequent itemset mining algorithms inspired by the Eclat algorithm, whereas BigFIM [68] is a mixed two-phase algorithm that combines an Apriori-based approach with an Eclat-based one.

DistEclat is a frequent itemset miner developed on Apache Hadoop. It exploits a parallel version of the Eclat algorithm to extract a superset of closed itemsets

The algorithm mainly consists of two steps. The first step extracts k -sized prefixes (i.e., frequent itemsets of length k) with respect to which, in the second step, the algorithm builds independent projected subtrees, each one associated with an independent subproblem. Even in this case, the main idea is to mine these independent trees in different nodes, exploiting the search split parallelization approach discussed in Section 3.3.

The algorithm is organized in 3 MapReduce jobs.

First job. In the initial job, a MapReduce job transposes the dataset into a vertical representation.

Second job. In this MapReduce job, each mapper extracts a subset of the k -sized prefixes (k -sized itemsets) by running Eclat on the frequent items, and the related tidlists, assigned to it. The k -sized prefixes and the associated tidlists are then split in groups and assigned to the mappers of the last job.

Third job. Each mapper of the last MapReduce job runs the in main memory version of Eclat on its set of independent prefixes. The final set of frequent itemsets is obtained by merging the outputs of the last job.

The mining of the frequent itemsets in two different steps (i.e., mining of the itemsets of length k in the second job and mining of the other frequent itemsets in the last job) aims at improving the load balancing of the algorithm. Specifically, the split in two steps allows obtaining simpler sub-problems, which are potentially characterized by similar execution times. Hence, the application is overall well-balanced.

DistEclat is designed to be very fast but it assumes that all the tidlists of the frequent items should be stored in main memory. In the worst case, each mapper needs the complete dataset, in vertical format, to build all the 2-prefixes [68]. This impacts negatively on the scalability of DistEclat with

respect to the dataset size. The algorithm inherits from the centralized version the depth-first strategy to explore the search-space and the preference for dense datasets.

BigFIM is a Hadoop-based solution very similar to DistEclat. Analogously to DistEclat, BigFIM is organized in two steps: (i) extraction of the frequent itemsets of length less than or equal to the input parameter k and (ii) execution of Eclat on the sub-problems obtained splitting the search-space with respect to the k -itemsets. The difference lies in the first step, where BigFIM exploits an Apriori-based algorithm to extract frequent k -itemsets, i.e., it adopts the data split parallelization approach (Section 3.3). Even if BigFIM is slower than DistEclat, BigFIM is designed to run on larger datasets. The reason is related to the first step in which, exploiting an Apriori-based approach, the k -prefixes are extracted in a breadth-first fashion. Consequently, the nodes do not have to keep large tidlists in main memory but only the set of candidate itemsets to be counted. However, this is also the most critical issue in the application of the data split parallelization approach, because, depending on the dataset density, the set of candidate itemsets may not be stored in main memory.

Because of the two different techniques used by BigFIM in its two main steps (data split and then search-space split), in the first step BigFIM achieves the best performance with sparse datasets, while in the second phase it better fits dense data distributions.

DistEclat and BigFIM are the only algorithms specifically designed for addressing load balancing and communication cost by means of the prefix length parameter k . In particular, the choice of the length of the prefixes generated during the first step affects both load balancing and communication cost.

3.5 Relevant publications

D. Apiletti, E. Baralis, T. Cerquitelli, P. Garza, F. Pulvirenti and L. Venturini, "Frequent Itemsets Mining for Big Data: a comparative analysis," *Elsevier Big Data Research* - 2017, 9: 67-83.

D. Apiletti, P. Garza, and F. Pulvirenti, “ Review of Scalable Approaches for Frequent Itemset Mining,” in *East European Conference on Advances in Databases and Information Systems (ADBIS 2015)*.

Chapter 4

State of the art experimental evaluation and open issues

After the theoretical analysis, in this chapter we introduce and comment an exhaustive experimental comparisons between all the approaches introduced in Chapter 3.

The extensive evaluation campaign is useful to assess the reliability of the expectations related to the theoretical analysis. Specifically, we ran more than 300 experiments on 14 synthetic datasets and 2 real datasets to evaluate the execution time, load balancing, and communication costs of four state-of-the-art parallel itemset mining implementations.

The campaign allowed us to identify the strengths and weaknesses of the algorithms with respect to the input dataset features (e.g., data distribution, average transaction length, number of records), and specific parameter settings. Finally, we will comment and discuss the result, introducing open research directions for the parallelization of the itemset mining problem.

The contents of this chapter have been presented in [47] and are organized as follows. In Section 4.1 we benchmark the selected algorithms with a large set of experiments on both real and synthetic datasets. Algorithm performances are evaluated in terms of (i) efficiency (i.e., execution time and scalability) under different conditions (Sections 4.1.2-4.1.8), (ii) load balancing (Subsection 4.1.9), and (iii) communication costs (Subsection 4.1.10). Subsection 4.1.11 comments the experimental results while Section 4.2 summarizes the concrete and practical

lessons learned from our evaluation analysis. Finally, Section 4.3 discusses the open issues raised by the experimental validation of the theoretical analysis, highlighting some possible research directions to support a more effective and efficient data mining process on Big Data collections.

4.1 Experimental Campaign

4.1.1 Experimental setup

The experimental evaluation includes the following four algorithms, which are described in Section 3.4:

- the Parallel FP-Growth implementation provided in Mahout 0.9 (named Mahout PFP in the following) [33],
- the Parallel FP-Growth implementation provided in MLlib for Spark 1.3.0 (named MLlib PFP in the following) [35],
- the June 2015 implementation of BigFIM [70],
- the version of DistEclat downloaded from [70] on September 2015.

We recall that Mahout PFP extracts the top k frequent closed itemsets, BigFIM and DistEclat extract a superset of the frequent closed itemsets, while MLlib PFP extracts all the frequent itemsets. To perform a fair comparison, Mahout PFP is forced to output all the closed itemsets. Since the extraction of the complete set of frequent itemsets is usually more resource-intensive than dealing with only the set of frequent closed itemsets¹, the execution times of Mahout PFP, BigFIM and DistEclat may increase with respect to MLlib PFP. However, in our experiments, the numbers of frequent itemsets and closed itemsets are in the same order of magnitude. Therefore, the disadvantages related to the more intensive task performed by MLlib are mitigated.

We defined a common set of default parameter values for all experiments. Specific experiments with different settings are explicitly indicated. The default setting of each algorithm was chosen by taking into account the physical

¹We recall that the complete set of frequent itemsets can be obtained expanding and combining the closed itemsets by means of a post-processing step.

characteristics of the Hadoop cluster, to allow each approach to exploit the hardware and software configuration at its best.

- For Mahout PFP, the default value of k is set to the lowest value forcing Mahout PFP to mine all frequent closed itemsets.
- For MLlib PFP the number of partitions is set to 6,000. This value has shown to be the best tradeoff among performance and the capacity to complete the task without memory issues. In particular, with lower values of the number of partitions MLlib PFP cannot scale to very long transactions or very low *minsup*. Higher values, instead, do not lead to better scalability, while affecting performance.
- The default value of the prefix length parameter of both BigFIM and DistEclat is set to 2, which achieves a good tradeoff among efficiency and scalability of the two approaches.
- We did not define a default value of *minsup*, which is a common parameter of all algorithms, because it is highly related to the data distribution and the use case, so this parameter value is specifically discussed in each set of experiments.

We considered both synthetic and real datasets. The synthetic ones have been generated by means of the IBM dataset generator [71], commonly used for performance benchmarking in the itemset mining context. We tuned the following parameters of the IBM dataset generator to analyze the impact of different data distributions on the performance of the mining algorithms: T = average size of transactions, P = average length of maximal patterns, I = number of different items, C = correlation grade among patterns, and D = number of transactions. The full list of synthetic datasets is reported in Table 4.1, where the name of each dataset consists of pairs $\langle \text{parameter}, \text{value} \rangle$. Finally, two real datasets have been used to simulate real-life use cases. They are described in Section 4.1.8.

All the experiments, except the speedup analysis, were performed on a cluster of 5 nodes running the Cloudera Distribution of Apache Hadoop (CDH5.3.1) [72]. Each cluster node is a 2.67 GHz six-core Intel(R) Xeon(R) X5650 machine with 32 Gigabytes of main memory and SATA 7200-rpm hard disks. The dimension

Table 4.1 Synthetic datasets

ID	Name/IBM Generator parameter setting	Num. of different items	Avg. # items per transaction	Size (GB)
1	T10 -P5-I100k-C0.25- D10M	18001	10.2	0.5
2	T20 -P5-I100k-C0.25-D10M	18011	19.9	1.2
3	T30 -P5-I100k-C0.25-D10M	18011	29.9	1.8
4	T40 -P5-I100k-C0.25-D10M	18010	39.9	2.4
5	T50 -P5-I100k-C0.25-D10M	18014	49.9	3.0
6	T60 -P5-I100k-C0.25-D10M	18010	59.9	3.5
7	T70 -P5-I100k-C0.25-D10M	18016	69.9	4.1
8	T80 -P5-I100k-C0.25-D10M	18012	79.9	4.7
9	T90 -P5-I100k-C0.25-D10M	18014	89.9	5.3
10	T100 -P5-I100k-C0.25-D10M	18015	99.9	5.9
11	T10-P5-I100k-C0.25- D50M	18015	10.2	3.0
12	T10-P5-I100k-C0.25- D100M	18016	10.2	6.0
13	T10-P5-I100k-C0.25- D500M	18017	10.2	30.4
14	T10-P5-I100k-C0.25- D1000M	18017	10.2	60.9

of Yarn containers is set to 6 GB. This value leads to a full exploitation of the resources of our hardware, representing a good tradeoff between the amount of memory assigned to each task and the level of parallelism. Lower values would have increased the level of parallelism at the expense of the task completion, whereas higher values would have affected the parallelism, with very few distributed tasks.

For the speedup experiments we used a larger cluster of 30 nodes² with 2.5 TB of total RAM and 324 processing cores provided by Intel CPUs E5-2620 at 2.6GHz, running the same Cloudera Distribution of Apache Hadoop (CDH5.3.1) [72].

From a practical point of view, all the implementations revealed to be quite easy to deploy and use. Actually, the only requirement for all the implementations to be run was the Hadoop/Spark installation (from a single machine scenario to a large cluster). Only the MLlib PFP implementation requires few additional steps and some coding skills, since it is delivered as a library: users must develop their own class and compile it.

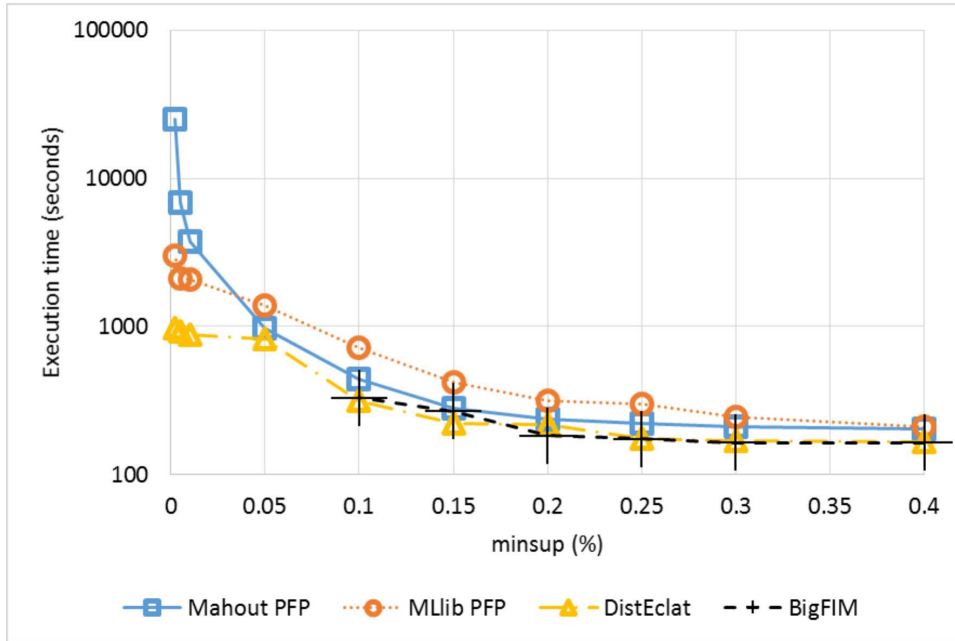


Fig. 4.1 Execution time for different *minsup* values (Dataset #1), average transaction length 10.

4.1.2 Impact of the minsup support threshold

The minimum support threshold (*minsup*) has a high impact on the complexity of the itemset mining task.

To avoid the bias due to a specific single data distribution, two different datasets have been considered: Dataset #1 and Dataset #3 (Table 4.1). They share the same average maximal pattern length (5), the number of different items (100 thousands), the correlation grade among patterns (0.25), and the number of transactions (10 million). The difference is in the average transaction length: 10 items for Dataset #1 and 30 items for Dataset #3. Being the other characteristics constant, longer transactions lead to a higher dataset density, which results into a larger number of frequent itemsets.

Figure 4.1 reports the execution time of the algorithms when varying the *minsup* threshold from 0.002% to 0.4% and considering Dataset #1. DistEclat is the fastest algorithm for all the considered *minsup* values. However, the improvement with respect to the other algorithms depends on the value of

²<http://bigdata.polito.it>

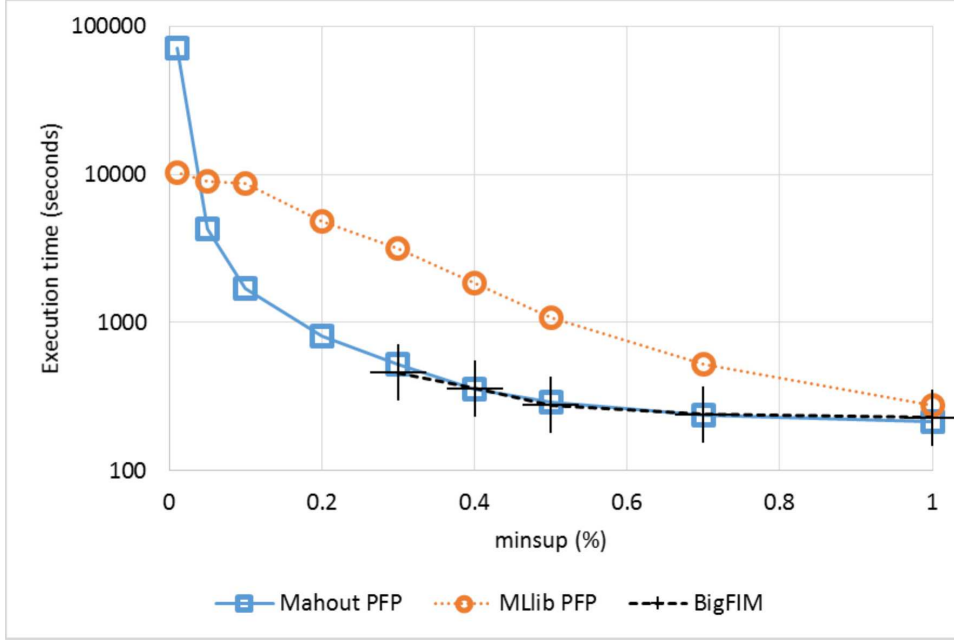


Fig. 4.2 Execution time for different *minsup* values (Dataset #3), average transaction length 30.

minsup. When *minsup* is greater than or equal to 0.2%, all the implementations show similar performances. The performance gap largely increases with *minsup* values lower than 0.05%. BigFIM is as fast as DistEclat when *minsup* is higher than 0.1%, but below this threshold BigFIM runs out of memory during the extraction of 2-itemsets.

In the second set of experiments, we analyzed the execution time of the algorithms for different minimum support values on Dataset #3, which is characterized by a higher average transaction length (3 times longer than Dataset #1), and a larger data size on disk (4 times bigger), with the same number of transactions (10 million). Since the mining task is more computationally intensive, *minsup* values lower than 0.01% were not considered in this set of experiments, as this has proven to be a limit for most algorithms due to memory exhaustion or too long experimental duration (days). Results are reported in Figure 4.2. MLib PFP is much slower than Mahout PFP for most *minsup* values (0.7% and below), and BigFIM, as in the previous experiment, achieves top-level performance, but cannot scale to low *minsup* values (the lowest is 0.3%), due to memory constraints during the *k*-itemset generation phase. Finally, DistEclat was not able to run because the size of the initial

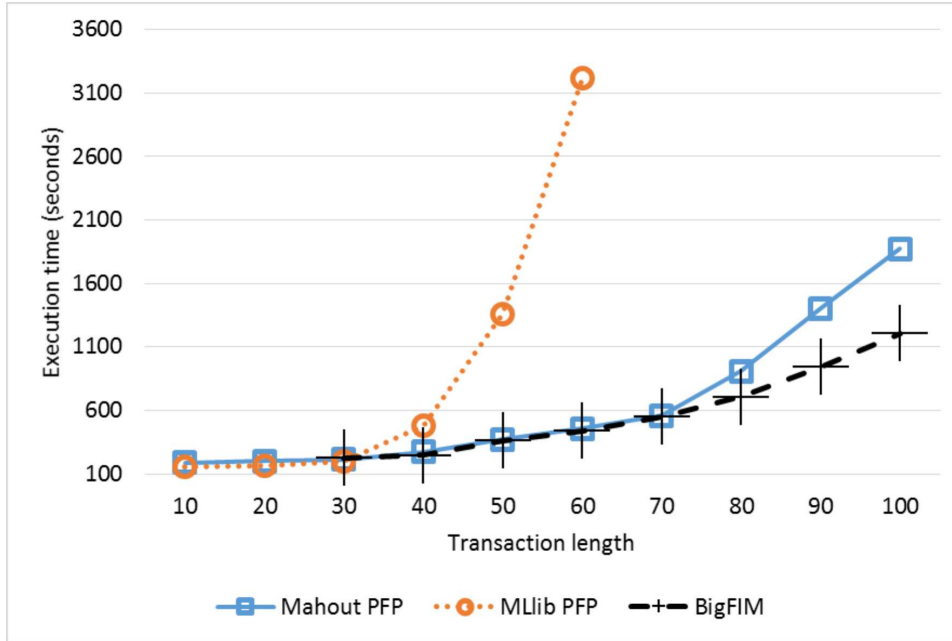


Fig. 4.3 Execution time with different average transaction lengths (Datasets #1–10, *minsup* 1%).

tidlists was already too big.

Overall, as expected, DistEclat is the fastest approach when it does not run out of memory. Mahout PFP is the most reliable implementation across almost all *minsup* values, even if it is not always the fastest, sometimes with large gaps behind the top performers. MLlib is a reasonable tradeoff choice, as it is constantly able to complete all the tasks in a reasonable time. Finally, BigFIM does not present advantages over the other approaches, being unable to reach low *minsup* values and to provide fast executions.

4.1.3 Impact of the average transaction length

We analyzed the effect of different average transaction lengths, from 10 to 100 items per transaction. We fixed the number of transactions to 10 million. To this aim, Datasets #1–10 were used (see Table 4.1). Longer transactions often lead to more dense datasets and a larger number of long frequent itemsets. This generally corresponds to more computationally intensive tasks. The execution times obtained are reported in Figure 4.3 and Figure 4.4, with a respective

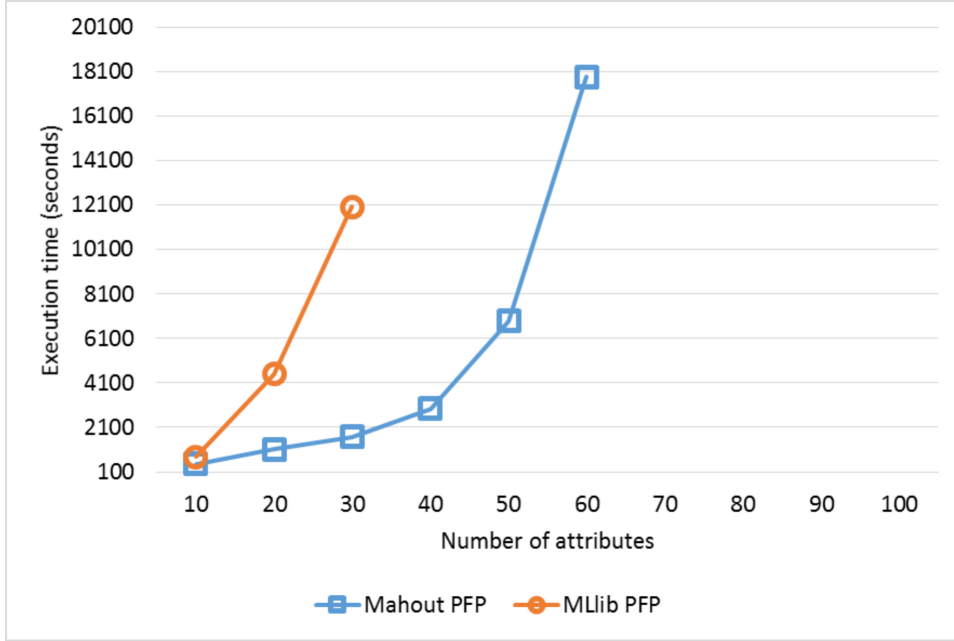


Fig. 4.4 Execution time with different average transaction lengths (Datasets #1–10, *minsup* 0.1%).

minsup value of 1% and 0.1%. In the experiment of Figure 4.3, BigFIM and DistEclat execution times for transaction length of 10 and 20 are not reported because, for these configurations, no 3-itemsets are extracted and hence the two algorithms crashed³. For higher transaction lengths, DistEclat is not included since it runs out of memory for values beyond 20 items per transaction. The other algorithms have similar execution times for short transactions, up to 30 items. For longer transactions, a clear trend is shown: (i) MLlib PFP is much slower than the others and it is not able to scale for longer transactions, as its execution times abruptly increase until it runs out of memory; (ii) Mahout PFP and BigFIM have a similar trend until 70 items per transactions, when Mahout PFP becomes slower than BigFIM.

The experiments of Figure 4.4, shows a very similar trend, with exception that also BigFIM is not able to run.

Overall, despite the Apriori-based initial phase, BigFIM proved to be the best scaling approach for very long transactions and a relatively high *minsup*. When the *minsup* is decreased only Mahout PFP is able to cope with the complexity

³Due to the absence of a specific test, BigFIM and DistEclat crash if no itemsets longer than the value of the prefix length parameter are mined.

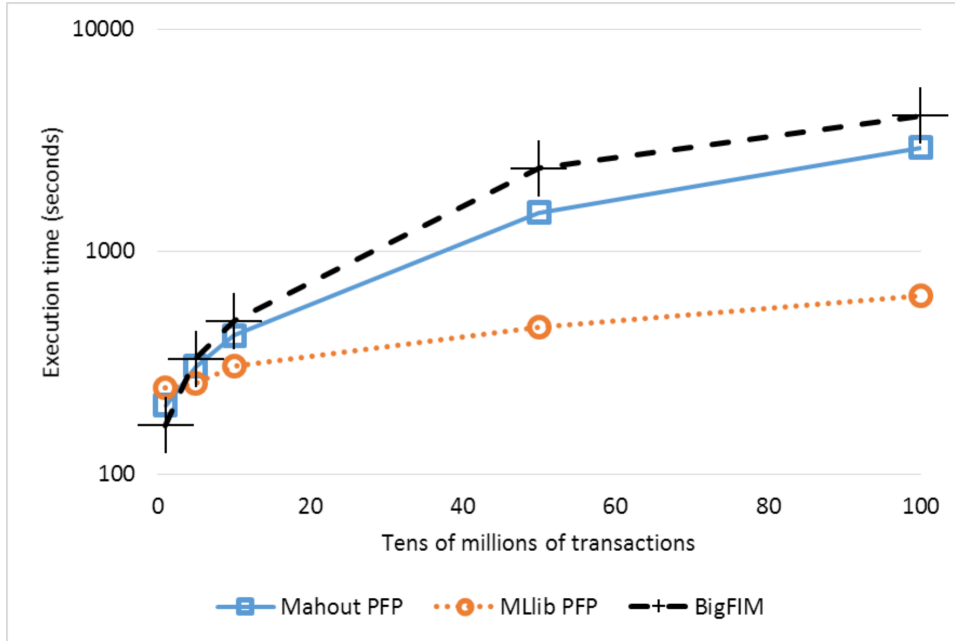


Fig. 4.5 Execution time with different numbers of transactions (Datasets #1, #11–14, *minsup* 0.4%).

of the task.

4.1.4 Impact of the number of transactions

We evaluated the effect of varying the number of transactions, i.e., the dataset size, without changing intrinsic data characteristics (e.g., transaction length or data distribution). The experiments have been performed on Datasets #1, #11–14 have been used (see Table 4.1), which have a number of transactions ranging from 10 million to 1 billion. The *minsup* is set to 0.4%, which is the highest value for which the mining leverages both phases of BigFIM, and it corresponds to the highest value used in the experiments of Section 4.1.2. Since in the experiment the relative minsup threshold is fixed, from the mining point of view, the search-space exploration is similar and not particularly challenging, as shown in Section 4.1.2. What really affects this experiment is the algorithms reliability dealing with such amounts of data.

As shown in Figure 4.5, all the considered algorithms scale almost linearly with respect to the dataset cardinality, with BigFIM being the slowest, closely

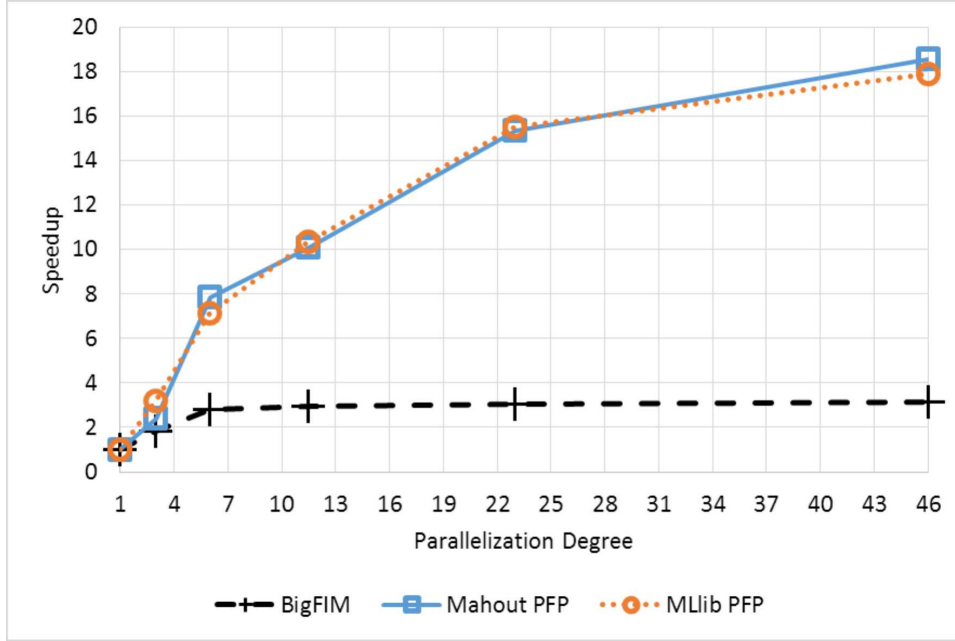


Fig. 4.6 Speedup with different parallelization degrees (Dataset #14, *minsup* 0.4%)

followed by Mahout PFP, and with MLib PFP being by far the fastest approach, with execution times reduced by almost an order of magnitude. PFP implementations are faster than BigFIM because they read from the disk the input dataset only twice. BigFIM pays the iterative disk reading activities during its initial Apriori phase when the number of records of the input dataset increases. Finally, DistEclat fails under its assumption that the tidlists of the entire dataset should be stored in each node, and it is not able to complete the extraction beyond 10 million transactions.

4.1.5 Scalability in terms of parallelization degree

We analyzed the speedup by running the same mining problem with increasing numbers of parallel tasks. The dataset selection and the *minsup* parameter choice are difficult since we need to identify a mining problem satisfying two conditions: (i) allowing all the executions to complete with any number of parallel tasks, and, at the same time, (ii) being very demanding so that the distributed framework is actually exploited. We selected *minsup* 0.4% and

Dataset #14 (see Table 4.1) to be light enough for condition (i) and demanding enough for condition (ii).

Figure 4.6 shows the speedup results. A parallelization degree equal to 1 corresponds to the minimal computational resource setting, i.e., the configuration with only two parallel independent tasks. Its execution time is the reference with respect to which the speedup is computed. Specifically, the speedup of a configuration with a parallelization degree equal to p is computed as

$$speedup(paral_degree = p) = \frac{Exec_Time(paral_degree = 1)}{Exec_Time(paral_degree = p)}$$

Ideally, the speedup should be equal to the parallelization degree p itself, i.e., increasing the number of resources (parallel tasks) of a factor p , should lead to a speedup equal to p .

In this experiment, it is clear that the FP-Growth-based implementations provide a better speedup. BigFIM, on the contrary, is not able to leverage a number of parallel tasks higher than 6. Because of the size of the dataset, DistEclat is not able to perform the mining.

4.1.6 Impact of framework and hardware configurations

We performed a set of experiments to test the behavior of the algorithms with different framework and hardware configurations to identify possible bottlenecks. We selected a set of configurations characterized by different combinations of (i) parallelization degree, (ii) computational power (cores per task) and (iii) memory (memory per task). The selected configurations are reported in Table 4.2. Conf. 1 is considered the reference configuration. The differences of the other configurations with respect to Conf. 1 are reported in bold in Table 4.2.

Conf. 1, Conf. 2, and Conf. 3 are used to evaluate the impact of the computational power (in terms of number of cores per task), Conf. 1 and Conf. 4 are used to evaluate the impact of the available memory, while Conf. 1, Conf. 5, and Conf. 6 are used to compare the impact of the previous features with respect to the parallelization degree. Experiments have been performed on dataset #1, with a fixed minsup set to 0.2%, and on dataset #5, with a

minsup value set to 1.5%.⁴ The main difference between the two datasets is the average transaction length (10 attributes per transaction in Dataset #1, 50 attributes per transaction in Dataset #5). In this way, it is possible to evaluate if the impact of hardware configuration is affected by data distribution. For DistEclat, in the experiments with Dataset #1, we were forced to reduce the dataset size to 1/10. In this way we were able to complete its experiments in all configurations (please note that the intra-algorithm comparison is still possible in percentage). As evidenced in Section 4.1.3, DistEclat does not suit large transactions length and, for this reason, we were not able to run any experiment with Dataset #5.

Table 4.2 Framework and Hardware configurations

Configuration name	Parallelization Degree	Number of cores per task	Memory per task (GB)
Conf. 1	5	1	1.5
Conf. 2	5	2	1.5
Conf. 3	5	3	1.5
Conf. 4	5	1	3
Conf. 5	2	1	1.5
Conf. 6	10	1	1.5

Figure 4.7 and 4.8 present the normalized execution time for each algorithm over different configurations on Dataset #1. For each algorithm, the normalized execution time is computed by dividing the execution time of each configuration by the execution time of the slowest configuration. Hence, for each algorithm, 100% is associated with the slowest configuration.

The comparison of Conf. 1, 2, and 3 shows that the number of cores per task does not impact on the execution time of the algorithms. Only in the second experiment (Figure 4.8), MLlib PFP seems to take advantage of the superior computational power. This means that the work assigned to each task, in the majority of the cases, can be performed by one single core. Hence, increasing the number of cores per task is not much effective.

Similarly, the main memory assigned to each task does not impact on the execution time of the algorithms (see Conf. 1 and 4). Specifically, the main memory per task impacts only on the size of the sub-problem that can be

⁴This support value is higher than that used in Section 4.1.3 to allow the execution of the experiments also for the BigFIM algorithm with all the selected hardware configurations.

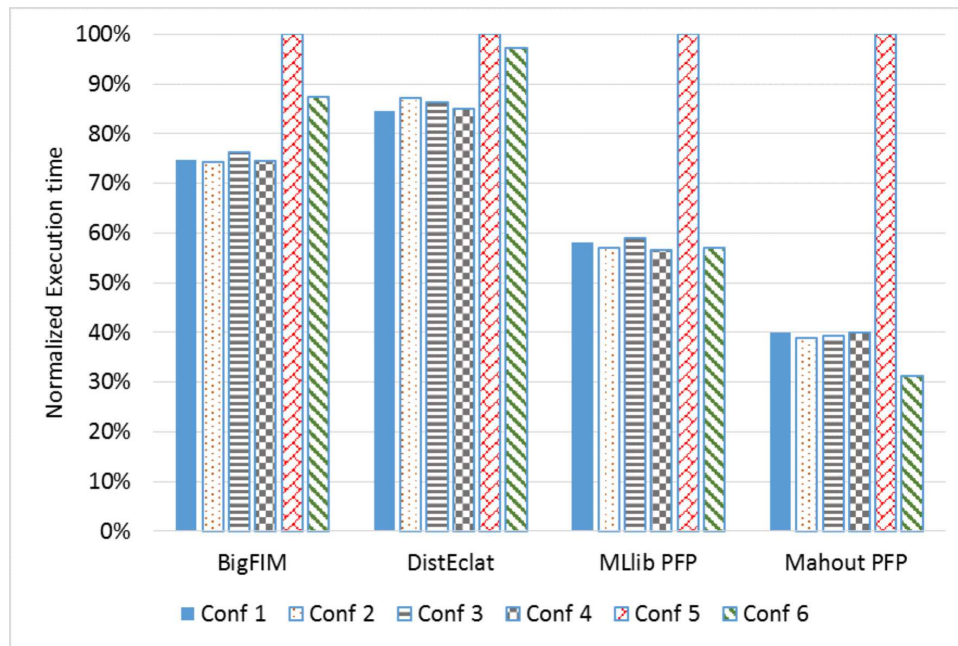


Fig. 4.7 Performances with different hardware configurations (Dataset #1, *minsup* 0.2%)

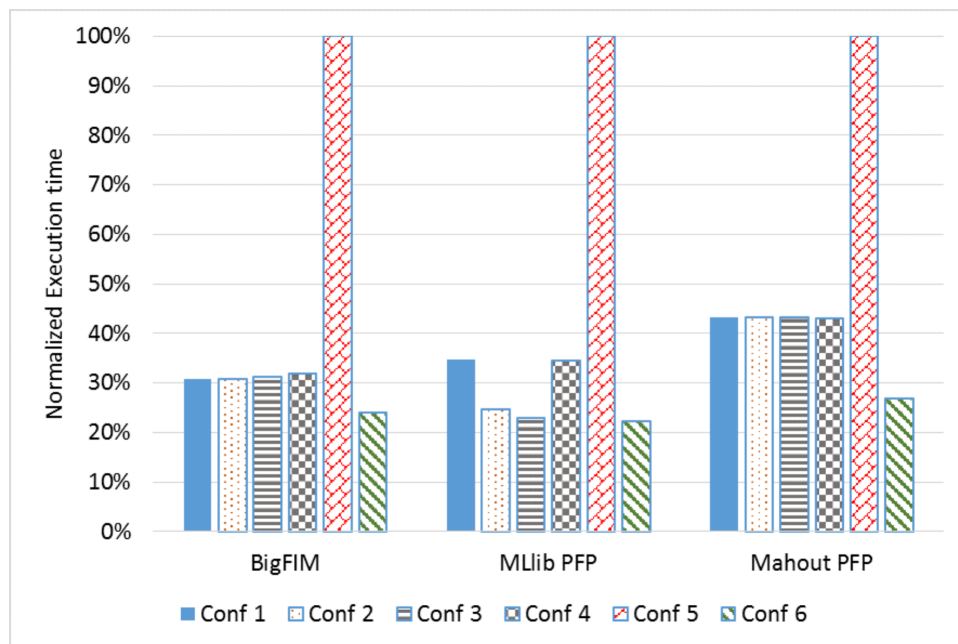


Fig. 4.8 Performances with different hardware configurations (Dataset #5, *minsup* 1.5%)

managed by each task, but not on its execution time. Hence, a proper setting of the main memory per task is required to be able to complete the execution and obtain the results, but not for its efficiency and performance. Finally, Configurations 1, 5, and 6 confirm that the parallelization degree is the most important factor affecting the execution time of the considered algorithms, as deeply investigated in Section 4.1.5, especially in the cases with a large amount of attributes per transactions Figure 4.8.

4.1.7 Execution time breakdown into phases

To investigate possible bottlenecks inside multi-phase algorithms, we compared the execution times related to each phase. Specifically, for each algorithm, we computed the percentage of time associated with the execution of each phase with respect to the total execution time of the algorithm.

We selected Dataset #1 and we set minsup to 0.15%, which allowed us to complete the full set of experiments with all algorithms.⁵

As reported in Figure 4.9, for BigFIM the length of the prefixes extracted in the first phase strongly affects the weight of that phase in the overall process. For DistEclat (Figure 4.10), instead, the difference is not that heavy.

The last phase of both algorithms (i.e. the top dotted part on the graphs), that is associated with the mining of the itemsets with a length greater than the prefix-length threshold, has a lower impact on the execution time of the algorithms, especially when a higher prefix threshold is set. These data, and the failures reported in the experiments of the previous subsections, indicate that the first two phases are the main bottlenecks for both algorithms. For BigFIM, each phase is strongly exposed to memory issues, as resumed in Table 4.3. The experiments demonstrate that the Apriori phase is particularly challenging. For DistEclat, instead, the very first stage is dedicated to the mining of 1-itemsets and it is mostly affected by high reading and communication costs. However, we have experienced some memory issues, which are probably related to the

⁵In this set of experiments, we used a smaller configuration of our cluster to guarantee network isolation. For this reason, we had to use a reduced version of Dataset #1 (1/10) for DistEclat, very sensitive to memory issues.

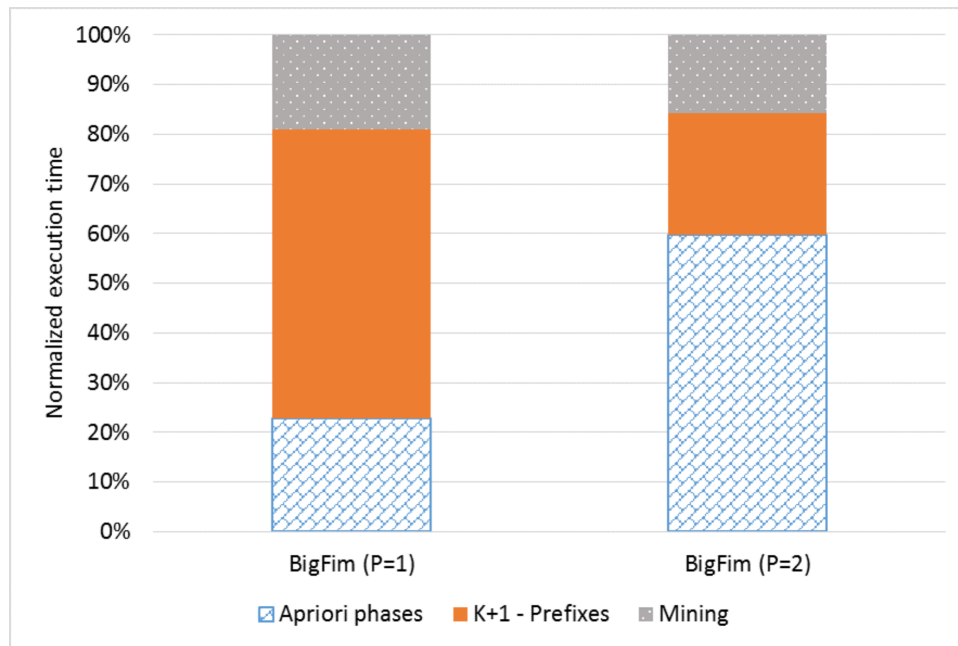


Fig. 4.9 BigFIM: Execution time of its phases

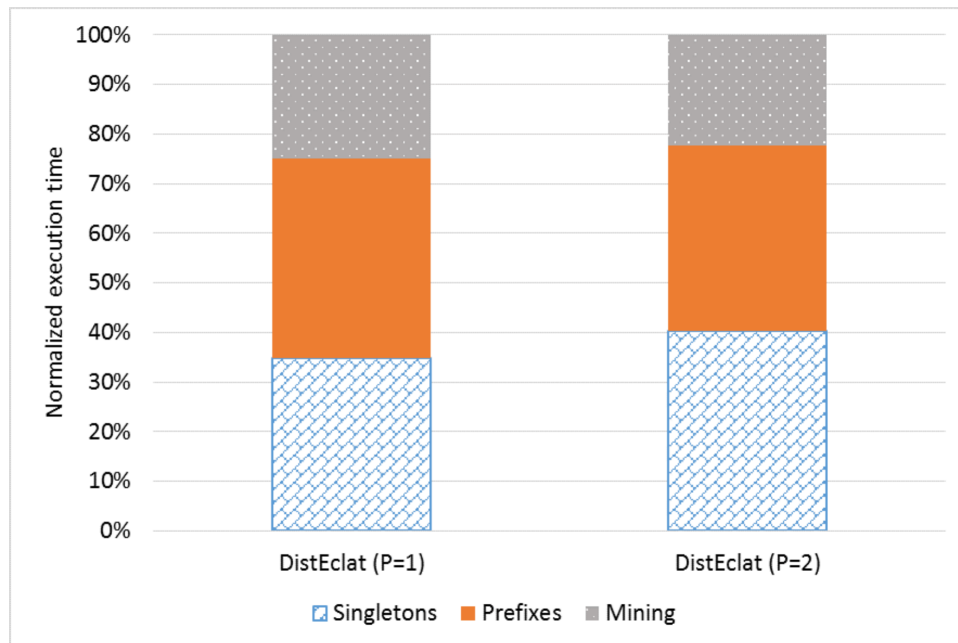


Fig. 4.10 DistEclat: Execution time of its phases

handling of the tidlists. The other stages, instead, are more likely to be affected by memory constraints.

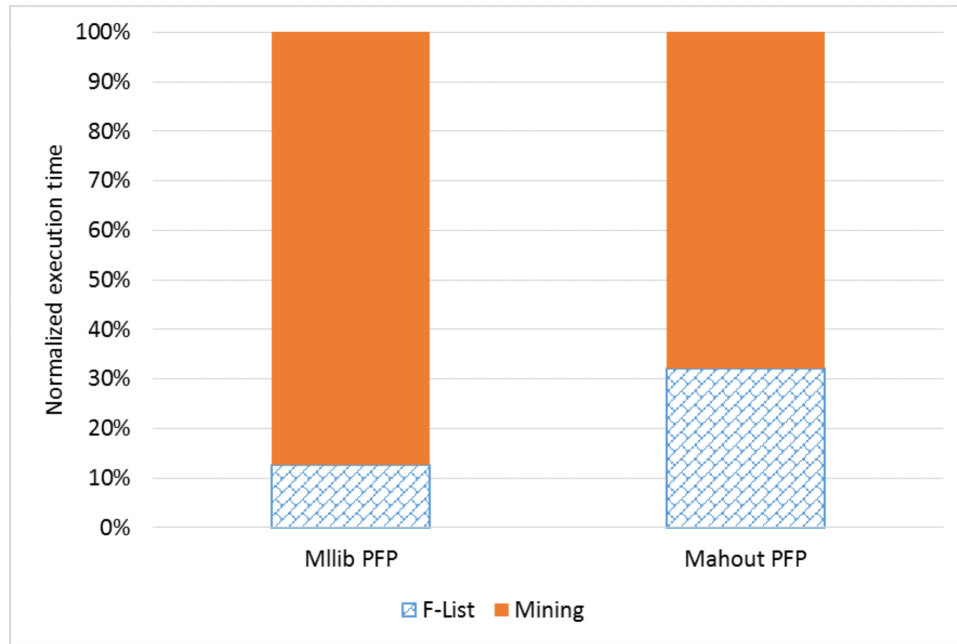


Fig. 4.11 Mahout and MLib PFP algorithms: Execution time of their phases

Figure 4.11 reports the results for the PFP implementations. Mahout PFP spends 1/3 of the time in the first phase, in which the F-list is generated, while MLib PFP is on the second phase for almost 90% of the time.⁶ The difference between the two approaches is motivated by the less elastic handling of the different jobs by Hadoop with respect to the Spark framework. Even if, especially for the Mahout PFP, the F-list generation could take a good amount of time, it is not a possible bottleneck of the whole mining. Firstly, it is a very flat WordCount-like application, characterized by high reading and communication costs, and secondly, it has never shown to be a point of failure in any previous experiment. From Figure 4.11, the bottleneck for the FP-growth-based algorithms is the itemset extraction phase (i.e., the second phase of both MLib PFP and Mahout PFP), strongly constrained by memory.

All the algorithms and the majority of their phases are strongly bottlenecked by memory issues. Memory availability is the main factor affecting the ability of each algorithm to complete the itemset extraction. Interestingly, we have seen that it does not affect the execution time performances (Subsection 4.1.6).

⁶Please note that we have forced the materialization of all the preliminary results with the Spark-based MLib PFP.

Table 4.3 Stage Bottlenecks

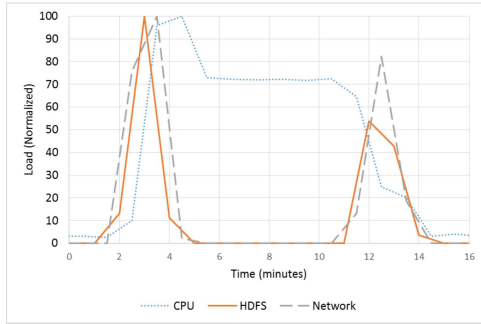
Algorithm	Phases	Bottleneck
FP-growth-based Algorithms	F-List	Reading and Communication Cost
	FP-Tree Mining	Memory
BigFIM	Apriori Phases	Memory
	K+1 Prefixes	Memory
	Eclat Mining	Memory
DistEclat	Singletons	Read. and Comm. Cost + Memory
	Prefixes	Memory
	Eclat Mining	Memory

We have also tried to track and measure the resource utilization in terms of disk usage (read and write phases of HDFS), network communication, and CPU usage. Please note that the values are normalized with respect to the maximum resource utilization. Specifically, Figures 4.12a and 4.12b report the achieved results for BigFIM and DistEclat, while Figures 4.13a and 4.13b show the results for the PFP-based implementations.

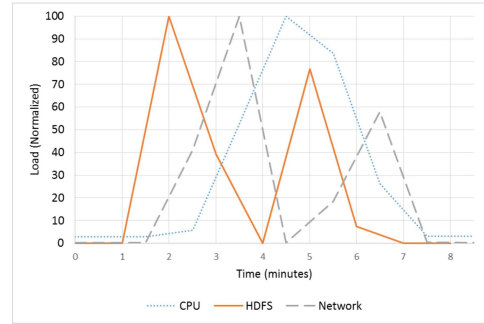
Figures 4.12a and 4.12b highlight two main peaks in resources utilization for BigFIM and DistEclat.⁷ For BigFIM the first peak is related to the Apriori phase and the k+1-prefixes generation, while the second is related to the depth-first mining. Similarly, for DistEclat the first peak is related to the singleton and prefixes generation while the second to the depth-first mining.

In Figure 4.13a it is shown the behavior in terms of resource utilization of Mahout PFP. The first peak in terms of HDFS and Network communication is related to the initial F-list generation. After that, the tree exploration starts and the CPU is more exploited. The last peaks are related to the aggregation job used to extract the top-k frequent closed itemsets. Figure 4.13b shows instead the MLlib PFP resource usage. Also the MLlib implementation of PFP is characterized by an initial peak in terms of HDFS operations followed by a peak in terms of CPU usage, associated with the intensive mining phase.

⁷For the sake of clarity we have used a prefix length of 1 to enhance the effect of the last mining phase.

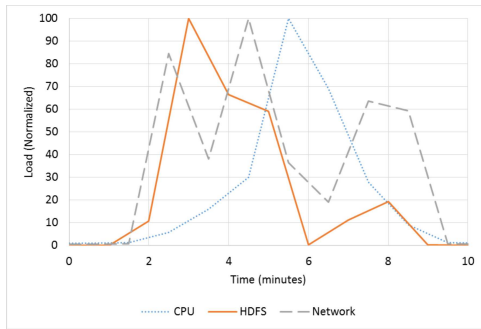


(a) BigFIM: Resource utilization

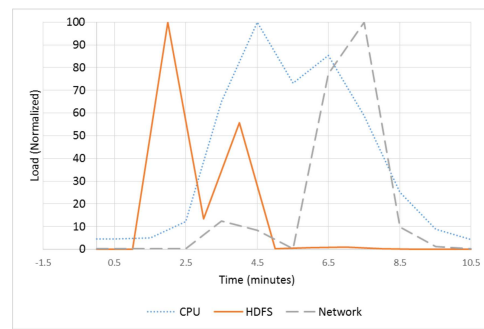


(b) DistEclat: Resource utilization

Fig. 4.12 Resource utilization of BigFIM and DistEclat



(a) Mahout PFP: Resource utilization



(b) MLlib PFP: Resource utilization

Fig. 4.13 Resource utilization of the PFP approaches

4.1.8 Real use cases

In the following, we analyze the performance of the mining algorithms in two real-life scenarios: (i) URL tagging of the Delicious dataset and (ii) network traffic flow analysis. The characteristics of the two datasets are reported in Table 4.4.

Table 4.4 Real-life use-cases dataset characteristics

ID	Name	Num. of different items	Avg. # items per transaction	Size (GB)
15	Delicious	57,372,977	4	44.5
16	Netlogs	160,941,600	15	0.61

URL tagging

We evaluated the selected algorithms on the Delicious dataset [73], which is a collection of web tags. Each record represents the tag assigned by a user to a URL and it consists of 4 attributes: date, user id (anonymized), tagged URL, and tag value. The transactional representation of the Delicious dataset includes one transaction for each record, where each transaction is a set of four pairs (attribute, value), i.e., one pair for each attribute. The dataset stores more than 3 years of web tags. It is very sparse because of the huge number of different URLs and tags. Additional characteristics of the dataset are reported in Table 4.5.

This experiment simulates the environment of a service provider that periodically analyzes the web tag data to extract frequent patterns: they represent the most frequent correlations among tags, URLs, users, and dates. Many different use cases can fit this description: tag prediction, topic classification, trend evolution, etc. Their evolution over time is also interesting. To this aim, the frequent itemset extraction has been executed cumulatively on temporally adjacent subsets of data, whose length is a quarter of year (i.e., first quarter, then first and second quarter, then first, second, and third quarter, and so on, as if the data were being collected quarterly and analyzed as a whole at the end of each quarter). The setting of *minsup* in a realistic use-case proved to be a critical choice. Too low values lead to millions of itemsets, which become useless as they exceed the human capacity to understand the results. However, too high *minsup* values would discard longer itemsets, which are more meaningful as they better highlight more complex correlations among the different attributes and values. Because of the high sparsity of the dataset, we identified the setting *minsup*=0.01% as the best trade-off.

Table 4.5 reports the cumulative number of transactions for the different periods of time (i.e., the cardinality of the input dataset) and the number of frequent itemsets extracted with a fixed *minsup* of 0.01%, while the execution times of the different algorithms are shown in Figure 4.14.

MLlib PFP consistently proves to be the fastest approach, with DistEclat following. However, while DistEclat is slightly faster than MLlib PFP only with the first, smallest dataset (up to Dec 2003, with 150 thousands transactions),

Table 4.5 Delicious dataset: cumulative number of transactions and frequent itemsets with $minsup$ 0.01%.

Up to year, month, quarter	Number of transactions	Number of frequent itemsets
2003 Dec, Q4	153,375	7197
2004 Mar, Q1	489,556	6013
2004 Jun, Q2	977,515	5268
2004 Sep, Q3	2,021,261	5084
2004 Dec, Q4	4,349,209	4714
2005 Mar, Q1	9,110,195	4099
2005 Jun, Q2	15,388,516	3766
2005 Sep, Q3	24,974,689	3402
2005 Dec, Q4	41,949,956	3090

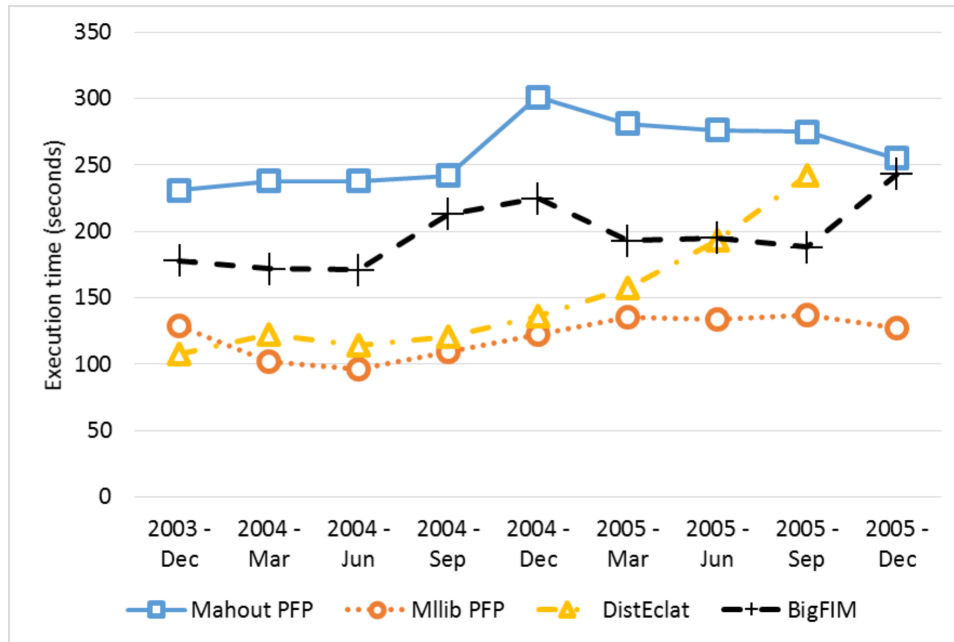


Fig. 4.14 Execution time for different periods of time on the Delicious dataset ($minsup=0.01\%$)

when the dataset size increases, DistEclat execution time does not scale. DistEclat eventually fails for the final 40-million-transaction dataset of Dec 2005, due to memory exhaustion. BigFIM and Mahout PFP consistently provide 2 to 3 times higher execution times. Apart from DistEclat, all algorithms complete the task with similar performance despite increasing the dataset cardinality from 150 thousand transactions to 41 million, thanks to the constant relative $minsup$ threshold which reduces the number of frequent itemsets for decreasing

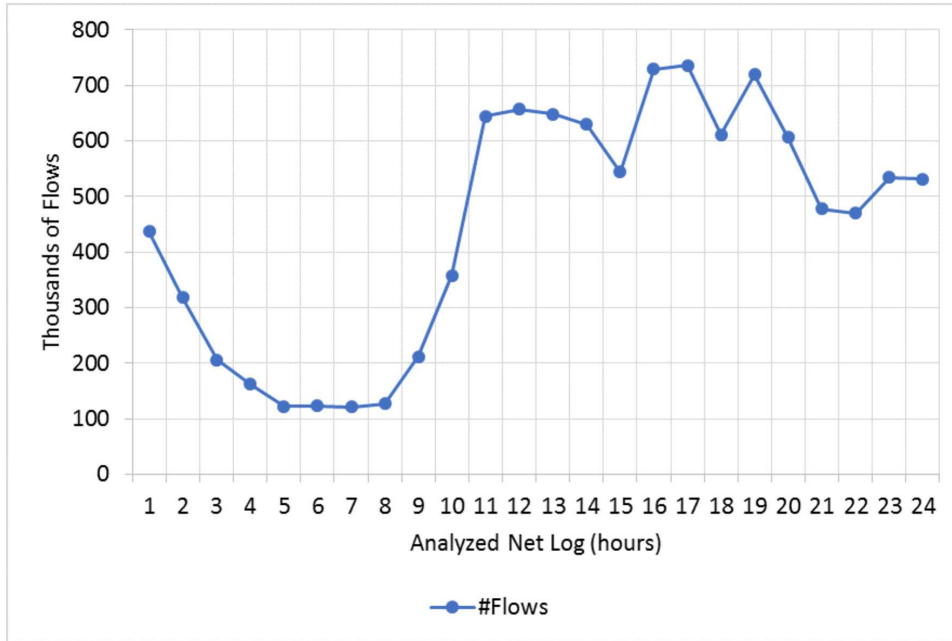


Fig. 4.15 Number of flows for each hour of the day.

density of the dataset. Hence, MLlib PFP is the best choice for this dataset characterized by short transactions (the transaction length is 4).

Network traffic flows

This use case entails the analysis of a network environment by using a network traffic log dataset, where each transaction represents a TCP flow. A network flow is a bidirectional communication between a client and a server. The dataset has been gathered through Tstat [74, 75], a popular internet traffic sniffer broadly used in literature [76, 77], by performing a one day capture in three different vantage points of a nation-wide Internet Service Provider in Italy. Each transaction of the dataset is associated with a flow and consists of pairs (*flow feature, value*). These features can be categorical (e.g., TCP Port, Window Scale) or numerical (e.g., RTT, Number of packets, Number of bytes). Numerical attributes have been discretized by using the same approach adopted in [77]. Finally, we have divided the set of flows (i.e., the set of transactions) in 1-hour slots, generating 24 sub-datasets. The number of flows in each sub-dataset is reported in Figure 4.15.

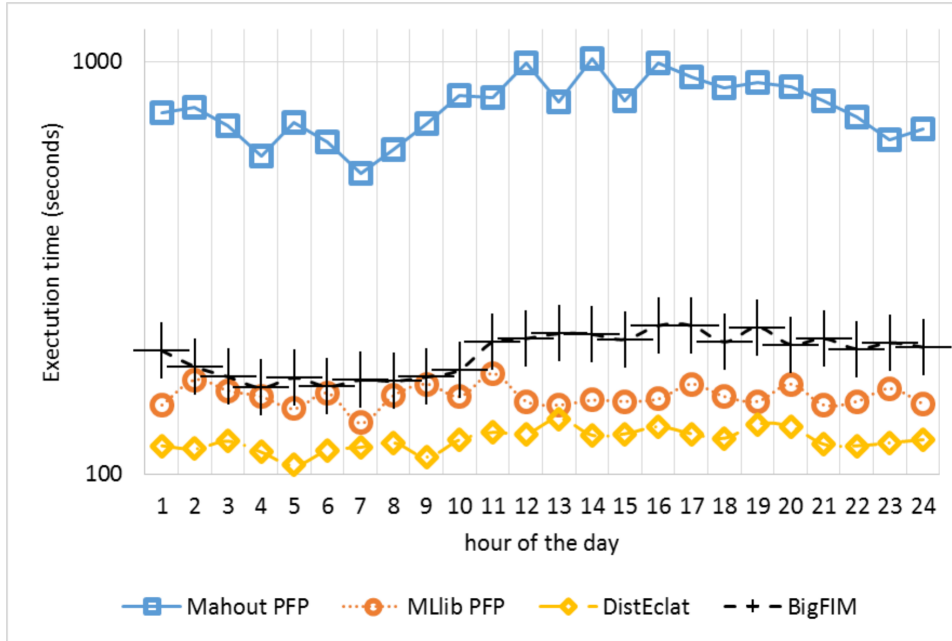


Fig. 4.16 Execution time of different hours of the day. (dataset 31, $minsup=1\%$)

Table 4.6 Network traffic flows: number of transactions and frequent itemsets with $minsup$ 0.1%.

Hour of the day	Number of transactions	Number of frequent itemsets
0.00	437,417	166,217
1.00	318,289	173,960
2.00	205,930	163,266
3.00	162,593	166,344
4.00	122,102	157,069
5.00	123,683	164,493
6.00	121,346	170,129
7.00	127,056	159,921
8.00	211,641	169,751
9.00	357,838	187,912
10.00	644,408	191,867
11.00	656,965	183,021
12.00	648,206	184,279
13.00	630,434	180,384
14.00	544,572	175,252
15.00	729,518	192,992
16.00	735,850	189,160
17.00	611,582	177,808
18.00	719,537	179,228
19.00	607,043	174,783
20.00	477,760	161,153
21.00	470,291	159,065
22.00	534,103	144,212
23.00	531,276	164,516

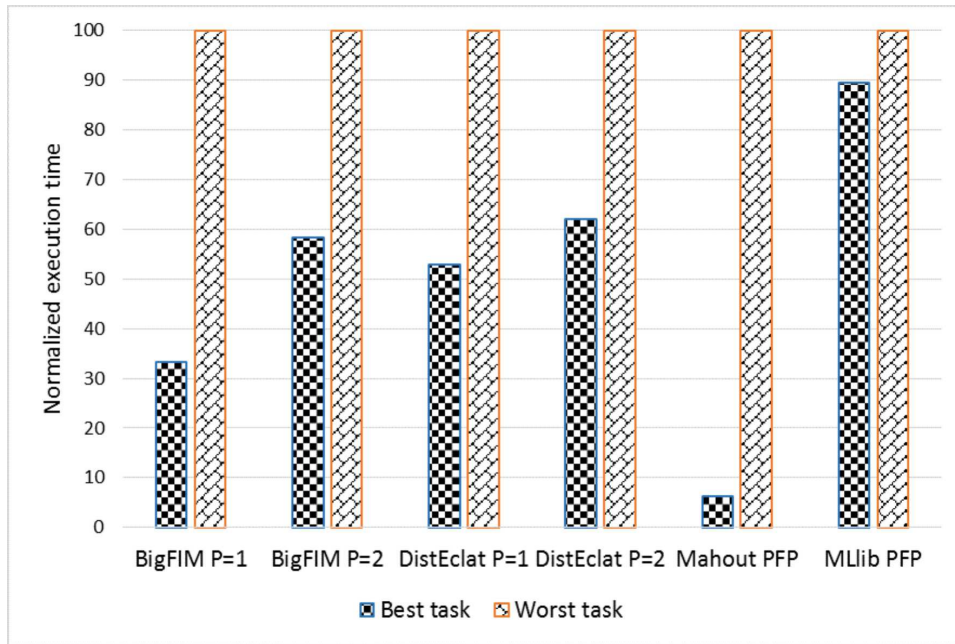


Fig. 4.17 Normalized execution time of the most unbalanced tasks.

In this use case, the network administrator is interested in performing hourly analysis to shape the hourly network traffic. Hence, we evaluated the performance of the four algorithms, comparing their execution time, on the 24 hourly sub-datasets. For all the 24 experiments *minsup* was set to 1%, which was the tradeoff value allowing all the algorithms to complete the extraction.

The results are reported in Figure 4.16, where the performance of the different approaches show a clear trend: DistEclat always achieves the lowest execution time, followed by MLib PFP and BigFIM. Mahout PFP is the slowest. The execution time is almost independent of the dataset cardinality, as it slightly changes throughout the day. The low dataset size (less than 1 Gigabyte overall) and cardinality (less than 1 million transactions) make this the ideal use case for DistEclat, which strongly exploits in-memory computation.

4.1.9 Load balancing

We analyzed load balancing on a 1-hour-long subset of the network log dataset (Table 4.4) with a fixed *minsup* of 1%. We consider the most unbalanced jobs of each algorithm and compare the execution times of the fastest and the

slowest tasks. To this aim, we are not interested in the absolute execution time, but rather in the normalized execution times, where the slowest task is assigned a value of 100, and the fastest task is compared to such value, as reported in Figure 4.17.

MLlib PFP achieves the best load balancing, with comparable execution times for all tasks throughout all nodes, whose difference is in the order of 10%. Mahout PFP, instead, shows the worst load balancing issues, with differences as high as 90%. The difference between MLlib PFP and Mahout PFP can be correlated to the granularity of the subproblems. The smaller the subproblems, the better the load balancing because their execution times are more similar. MLlib PFP allows specifying the number of partitions, i.e., of subproblems, which obviously impacts on the granularity of each subproblem. Hence, setting opportunely this parameter, a good load balancing result is achieved. Differently, Mahout PFP automatically sets the number of subproblems and the current heuristic used to set it does not seem to work well on the considered datasets (unbalanced subproblems are generated).

We included BigFIM and DistEclat with 2 different first-phase prefix sizes. For these algorithms, the experiment confirms that a configuration with longer prefixes leads to a more balanced mining tasks than a configuration with short-sized prefixes, as mentioned in Subsection 3.4.3.

4.1.10 Communication costs

To evaluate the communication cost, we measure the amount of data transmitted and received through the nodes network interfaces. This information has been retrieved by means of the utilities provided by the Cloudera Manager tool.

The experiments have been performed on Dataset #1 with a fixed *minsup* value of 0.1%, which was the lowest value for which all algorithms completed the extraction. Figure 4.18 reports, for each algorithm, the average value among transmitted and received traffic, compared to the total execution time. Firstly, the two measures do not seem to be correlated: higher communication costs are associated with low execution times for BigFIM and DistEclat, whereas MLlib reports both measures with high values. Mahout PFP has a communication cost 4 to 5 times lower than all the others, which exchange an average of

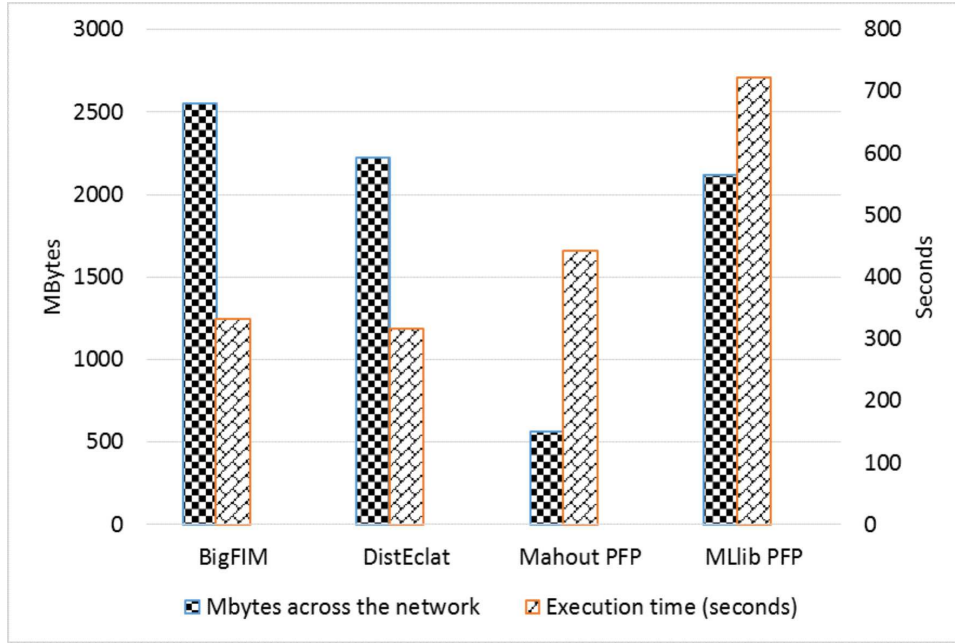


Fig. 4.18 Communication costs and performance for each algorithm, Datasets #1, *minsup* 0.1%. The graph reports an average between transmitted and received data.

2 Gigabytes of data. Mahout PFP average communication cost is around 0.5 Gigabytes, which is approximately the dataset size. The difference between DistEclat and BigFIM is not large because with only 2-length prefixes just an extra iteration is done by BigFIM. Even though Mahout PFP is the most communication-cost optimized implementation, the very low amount of data sent through the network is related to the adoption of compression techniques, which lead to higher execution times.

4.1.11 Discussion

The experiments confirm that the performance of the data-split-based algorithms (i.e., BigFIM in its first phase) is highly affected by the number of candidate itemsets, which must be stored in the temporary main memory of each task. Specifically, BigFIM crashes during its Apriori-based phase when low *minsup* values or dense datasets are considered, due to the large number of generated candidate itemsets. This issue does not affect the approaches based on the search split strategy (Mahout PFP and MLlib PFP), since they do not

need to store candidate itemsets as an intermediate result. Hence, Mahout PFP and MLlib PFP proved to be more suitable than BigFIM to process large dataset sizes, high-density datasets, and low *minsup* thresholds. DistEclat deserves a separate consideration: even if it is based on the search-space approach, it often runs out of memory, because in its initial job it needs to store the *tidlists* of all frequent items in main memory and this operation becomes easily unfeasible when large or dense datasets are considered.

Experiments also highlight the predominant importance of load balancing in the itemset mining problem, in particular when comparing BigFIM to Mahout PFP. Since the initial mining phase of BigFIM is based on the data split parallelization approach, it reads many times the input dataset (differently than Mahout PFP). Moreover, BigFIM is also characterized by greater communication costs than Mahout PFP. These two factors should impact significantly on the execution time of BigFIM. Instead, not only the execution time of BigFIM is comparable with that of Mahout PFP with 1000-million record datasets (Figure 4.5), but BigFIM is also even faster than Mahout PFP in specific cases, e.g., with datasets with an average number of items per transaction greater than 70 (Figure 4.3). The rationale of such results is the better load balancing of BigFIM with respect to Mahout PFP. Results highlight that load balancing seems to be predominant on the number of dataset reads (I/O costs) and communication costs in the parallelization of the itemset mining problem.

4.2 Lessons Learned

The reported experiments provide a wide view of the different behaviors of the algorithms in various experimental settings. With this section, we aim at supporting the reader in a conscious choice of the most suitable approach, depending on the use case at hand. Pursuing this target, we measured the real-life performance of the openly-available frequent-pattern mining implementations for the most popular distributed platforms (i.e., Hadoop and Spark). They have been tested on many different datasets characterized by different values of minimum support (*minsup*), transaction length (dimensionality), number of transactions (cardinality), and dataset density, besides two real-life use cases. Performance in terms of execution time, load balancing, and communication

cost have been evaluated: a one-table summary of the results is reported in Table 4.7. As a result of the described experience, the following general suggestions emerge:

- **High reliability.** Without prior knowledge of dataset density, dimensionality (average transaction length), and cardinality (number of transactions), **Mahout PFP** is the algorithm that best guarantees the mining task completion, at the expense of longer execution times. Mahout PFP is the only algorithm able to always reach the experimental limits.
- **High cardinality and low-dimensional data.** On most real-world use cases, with limited dimensionality (up to 60 items per transaction on average), **MLlib PFP** has proven to be the most reasonable tradeoff choice, with fast execution times and optimal scalability to very large datasets.
- **High-dimensional data.** For high-dimensional datasets, **BigFIM** resulted the fastest approach, but it cannot cope with *minsup* values as low as the others. In those cases, **Mahout PFP** represents the only option.
- **Limited dataset size.** When the dataset size is small with respect to the available memory, **DistEclat** has proven to be among the fastest approaches, and also to be able to reach the lowest experimental *minsup* values. DistEclat experiments showed that it cannot scale for large or high-dimensional datasets, but when it can complete the itemset extraction, it is very fast.

Table 4.7 Summary of the limits identified by the experimental evaluation of the algorithms (lowest *minsup*, maximum transaction length, largest dataset cardinality). The faster algorithm for each experiment is marked in bold.

	Section 4.1.2	Section 4.1.2	Section 4.1.3	Section 4.1.4
	<i>minsup</i>	<i>minsup</i>	transaction length	millions of transactions
Mahout PFP	0.002%	0.01%	100 (0.1%)	100
MLlib PFP	0.002%	0.01%	60	100
BigFIM	0.1%	0.3%	100 (1%)	100
DistEclat	0.002%	-	-	1

4.3 Open research issues

The comparative study presented in this review highlighted interesting research directions to enhance distributed itemset mining algorithms for Big Data.

Smarter load balancing techniques. The experimental evaluation allowed us to show that load balancing issues significantly affect distributed itemset mining performance, more than communication and I/O costs (e.g., reading the dataset many times). Specifically, the different complexity among the task-level sub-problems leads to load unbalance in the cluster (i.e., some sub-problems are more computationally expensive and time consuming than others causing inefficient resource usage). Load balancing improvements should be addressed in the design of new distributed frequent itemset mining algorithms. In that context, we believe that a new research direction to investigate is the definition of variable-length prefixes, with respect to which the mining sub-problems are defined, hence leading to a more balanced exploration of the search-space.

Self-tuning itemset mining frameworks. As discussed in this analysis, different algorithms have been proposed in literature to discover frequent itemsets. However, the efficient exploitation of each algorithm strongly depends on specific skills and expertise. The analyst is required to select the best method to efficiently deal with the underlying data characteristics, and manually configure it (e.g., from input parameters settings, such as the *minsup* threshold, the k parameter of BigFIM, etc., to distributed frameworks tuning). Thus, state-of-the-art algorithms may become ineffective because of the inefficient hand-picked choices of the inappropriate specific implementations, and cumbersome parameter-configuration sessions. The improvements in algorithm usability should be addressed by designing innovative self-tuning itemset mining frameworks, capable of intelligently selecting the most appropriate itemset extraction algorithm and automatically configuring it.

High-dimensional datasets. The performance analysis included a mining experiments on datasets with up to 100 dimensions. Even if Mahout PFP has outperformed the competitors, its performances are still very weak for low minimum support values. On the other hand, 100-features dataset certainly

do not represent a state-of-the-art high dimensional problem, which can be instead characterized by thousands of million of dimensions.

The state of the art review highlighted the concrete lack of a real scalable implementation which focus on the number of items per transaction. In Chapter 5, it will be introduced a High-Dimensional Map-Reduce-based frequent pattern miner developed to fill this gap.

4.4 Relevant publications

D. Apiletti, E. Baralis, T. Cerquitelli, P. Garza, F. Pulvirenti and L. Venturini, “Frequent Itemsets Mining for Big Data: a comparative analysis,” *Elsevier Big Data Research* - 2017, 9: 67-83.

Chapter 5

Frequent Itemset Mining for High-Dimensional data

Existing mining algorithms revealed to be very efficient on simple datasets but very resource intensive in Big Data contexts. In general, the application of data mining techniques to Big Data collections is characterized by the need of huge amount of resources. For this reason, we are witnessing the explosion of parallel and distributed approaches, typically based on distributed frameworks, such as Apache Hadoop [5] and Spark [6].

As clearly shown in Chapter 4, unfortunately, most of the scalable distributed techniques for frequent itemset mining have been designed to cope with datasets characterized by few items per transaction (low dimensionality, short transactions). Their design, on the contrary, focuses on very large datasets in terms of number of transactions. Currently, only single-machine implementations exist to address very long transactions, such as Carpenter [25], and no distributed implementations at all.

Nevertheless, many scientific applications, such as bioinformatics or networking, generate a large number of events characterized by a variety of features. Thus, high-dimensional datasets have been continuously generated. For instance, most gene expression datasets are characterized by a huge number of items (related to tens of thousands of genes) and a few records (one transaction per patient or tissue). Many applications in computer vision deal with high-dimensional data, such as face recognition. An increasing portion of big data is actually related

to geospatial data [78] and smart-cities. Some studies have built this type of large datasets measuring the occupancy of different car lanes: each transaction describes the occupancy rate in a captor location and in a given timestamp [79]. In the networking domain, instead, the heterogeneous environment provides many different datasets characterized by high-dimensional data, such as URL reputation, advertising, and social network datasets [80]. To effectively deal with those high-dimensional datasets, novel and distributed approaches are needed.

This work introduces PaMPa-HD [7], [8], a parallel MapReduce-based frequent closed itemset mining algorithm for high-dimensional datasets. PaMPa-HD relies on the Carpenter algorithm [25]. The PaMPa-HD design¹, through an ad-hoc synchronization technique, takes into account crucial design aspects, such as load balancing and robustness to memory-issues. Furthermore, different strategies have been proposed to easily tune up the parameter configuration. The algorithm has been thoroughly evaluated on real high dimensional datasets. PaMPa-HD outperforms the state-of-the-art distributed approaches in execution time and by supporting lower minimum support threshold.

The chapter is organized as follows: Section 5.1 briefly reintroduces the frequent (closed) itemset mining problem, Section 5.2 briefly describes the centralized version of Carpenter, and Section 5.3 presents the proposed PaMPa-HD algorithm. Section 5.4 describes the experimental evaluations proving the effectiveness of the proposed technique, Section 5.5 discusses possible applications of PaMPa-HD and, finally, Section 5.6 introduces future works and conclusions.

5.1 High-Dimensional Frequent itemset mining background

Since frequent itemset mining preliminaries were introduced far before in the dissertation, let us just recall and deepen the key concepts fundamental to better understand PaMPa-HD and its enumeration tree-based exploration strategy.

¹The source code of PaMPa-HD can be downloaded from <https://github.com/fpulvi/PaMPa-HD>

\mathcal{D}	
tid	items
1	a,b,c,l,o,s,v
2	a,d,e,h,l,p,r,v
3	a,c,e,h,o,q,t,v
4	a,f,v
5	a,b,d,f,g,l,q,s,t

(a) Horizontal representation of \mathcal{D}

TT	
item	tidlist
a	1,2,3,4,5
b	1,5
c	1,3
d	2,5
e	2,3
f	4,5
g	5
h	2,3
l	1,2,5
o	1,3
p	2
q	3,5
r	2
s	1,5
t	3,5
v	1,2,3,4

(b) Transposed representation of \mathcal{D}

$TT _{\{2,3\}}$	
item	tidlist
a	4,5
e	-
h	-
v	4

(c) $TT|_{\{2,3\}}$: example of conditional transposed table

Fig. 5.1 Running example dataset \mathcal{D}

The running example has been slightly modified from the one presented in Chapter 2 to better fit the use case.

As already mentioned, a transactional dataset can also be represented in a vertical format, which is usually more effective when the average number of items per transactions is orders of magnitudes larger than the number of transactions. This representation, called *transposed table* TT , assumes that each row consists of an item I and its list of transactions, i.e., $tidlist(\{I\})$. Let r be an arbitrary row of TT , $r.tidlist$ denotes the tidlist of row r . Figure 5.1b reports the transposed representation of the running example reported in Figure 5.1a.

Given a transposed table TT and a tidlist X , the conditional transposed table of TT on the tidlist X , denoted by $TT|_X$, is defined as a transposed table such that: (1) for each row $r_i \in TT$ such that $X \subseteq r_i.tidlist$ there exists one tuple $r'_i \in TT|_X$ and (2) r'_i contains all tids in $r_i.tidlist$ whose tid is higher than any tid in X . For example, consider the transposed table TT reported in

Figure 5.1b. The projection of TT on the tidlist $\{2,3\}$ is the transposed table reported in Figure 5.1c. Each transposed table $TT|_X$ is associated with an itemset composed by the items in $TT|_X$. For instance, the itemset associated with $TT|_{\{2,3\}}$ is $\{aehv\}$ (see Figure 5.1c).

5.2 The Carpenter algorithm

The most popular techniques to perform itemset mining (e.g., Apriori [64] and FP-growth [52]) adopt the itemset enumeration approach (see Section 3.2 for further discussion). However, itemset enumeration revealed to be ineffective with datasets with a high average number of items per transactions [25]. To tackle this problem, the Carpenter algorithm [25] was proposed. Specifically, Carpenter is a frequent itemset extraction algorithm devised to handle datasets characterized by a relatively small number of transactions but a huge number of items per transaction. To efficiently solve the itemset mining problem, Carpenter adopts an effective depth-first transaction enumeration approach based on the transposed representation of the input dataset. To illustrate the centralized version of Carpenter, we will use the running example dataset \mathcal{D} reported in Figure 5.1a, and more specifically, its transposed version (see Figure 5.1b). Recall that in the transposed representation each row of the table consists of an item i with its tidlist. For instance, the last row of Figure 5.1b shows that item v appears in transactions 1, 2, 3, 4.

Basically, Carpenter builds a transaction enumeration tree by exploiting a set of pruning rules which avoid the expansion of useless branch of the tree. In the tree, each node corresponds to a conditional transposed table $TT|_X$ and its related information (i.e., the tidlist X with respect to which the conditional transposed table is built and its associated itemset). The transaction enumeration tree, when pruning techniques are not applied, contains all the tid combinations (i.e., all the possible tidlists X). Figure 5.2 reports the transaction enumeration tree obtained by processing the running example dataset. To avoid the generation of duplicate tidlists, the transaction enumeration tree is built by exploring the tids in lexicographical order (e.g., $TT|_{\{1,2\}}$ is generated instead of $TT|_{\{2,1\}}$). Each node of the tree is associated with a conditional

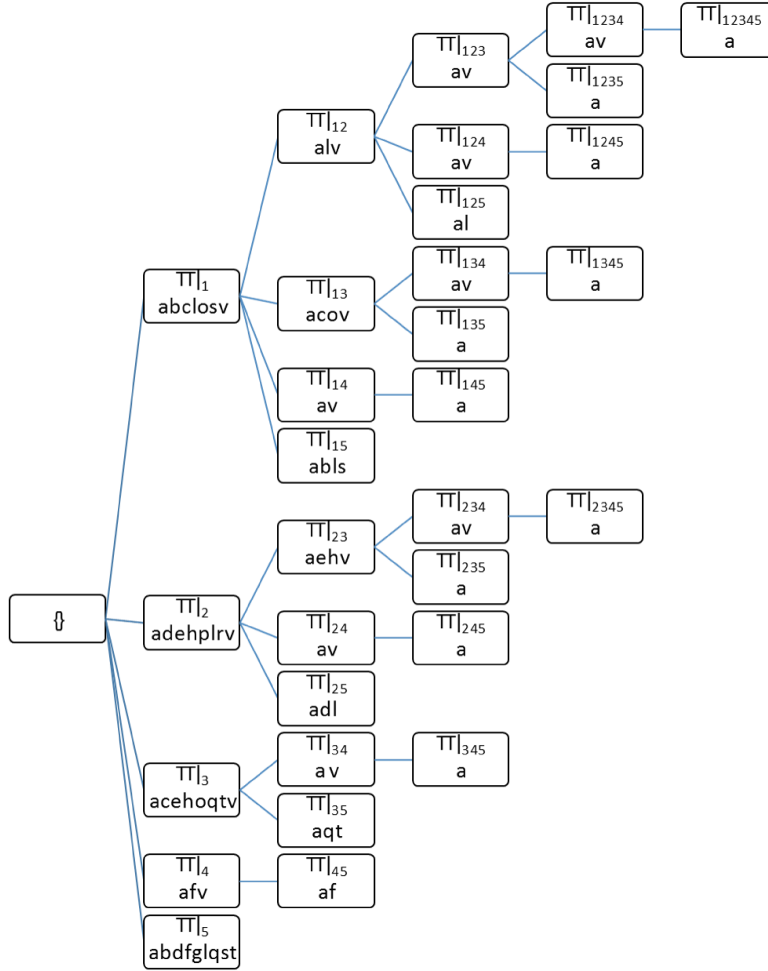


Fig. 5.2 The transaction enumeration tree of the running example dataset in Figure 5.1a. For the sake of clarity, no pruning rules are applied to the tree.

transposed table on a tidlist. For instance, the conditional transposed table $TT|_{\{2,3\}}$ in Figure 5.1c, matches the node $\{2,3\}$ in Figure 5.2.

Carpenter performs a depth first search (DFS) of the enumeration tree to mine the set of frequent closed itemsets. Referring to the tree in Figure 5.2, the depth first search would lead to the visit of the nodes in the following order: $\{1\}$, $\{1,2\}$, $\{1,2,3\}$, $\{1,2,3,4\}$, $\{1,2,3,4,5\}$, $\{1,2,3,5\}$, $\{\dots\}$. For each node,

Carpenter applies a procedure that decides if the itemset associated with that node is a frequent closed itemset or not. Specifically, for each node, Carpenter decides if the itemset associated with the current node is a frequent closed itemset by considering:

1. The tidlist X associated with the node, useful to enforce the depth-first exploration and to check the actual support of the itemset
2. The conditional transposed table $TT|_X$, used to obtain the itemset associated to the node and, through the remaining tids, determine how and if the node should be expanded
3. The set of itemsets found up to the current step of the tree search, used to avoid to process the same itemset twice (due to the enumeration tree architecture, the real support of the itemset is the one obtained the first time the itemset is processed in a depth-first exploration manner)
4. The enforced minimum support threshold ($minsup$), used to decide if the itemset is a frequent closed itemset

Based on the theorems reported in [25], if the itemset I associated with the current node is a frequent closed itemset then I is included in the frequent closed itemset set. Moreover, by exploiting the analysis performed on the current node, part of the remaining search space (i.e., part of the enumeration tree) can be pruned, to avoid the analysis of nodes that will never generate new closed itemsets. To this purpose, three pruning rules are applied on the enumeration tree, based on the evaluation performed on the current node and the associated transposed table $TT|_X$:

- **Pruning rule 1.** If the size of X , plus the number of distinct tids in the rows of $TT|_X$ does not reach the minimum support threshold, the subtree rooted in the current node is pruned.
- **Pruning rule 2.** If there is any tid tid_i that is present in all the tidlists of the rows of $TT|_X$, tid_i is deleted from $TT|_X$. The number of discarded tids is updated to compute the correct support of the itemset associated with the pruned version of $TT|_X$.
- **Pruning rule 3.** If the itemset associated with the current node has been already encountered during the depth first search, the subtree rooted

in the current node is pruned because it can never generate new closed itemsets.

The tree search continues in a depth first fashion moving on the next node of the enumeration tree. More specifically, let tid_l be the lowest tid in the tidlists of the current $TT|_X$, the next node to explore is the one associated with $X' = X \cup \{tid_l\}$.

Among the three rules mentioned above, pruning rule 3 assumes a global knowledge of the enumeration tree explored in a depth first manner. This, as detailed in section 5.3, is very challenging in a distributed environment that adopts a shared-nothing architecture, like the one we address in this work.

5.3 The PaMPa-HD algorithm

In this section we describe the new algorithm, called PaMPa-HD, proposed in this chapter. Specifically, we describe how PaMPa-HD parallelizes the itemset mining process and applies the pruning rules discussed in Section 5.2 in a parallel environment. Furthermore, we discuss how, through an ad-hoc synchronization phase, PaMPa-HD achieves a good load balancing and robustness to memory issues.

As discussed in the previous section, given the complete enumeration tree (see Figure 5.2), the centralized Carpenter algorithm extracts the whole set of closed itemsets by performing a depth first search (DFS) of the tree. Differently, in order to parallelize the mining process, the PaMPa-HD algorithm splits the depth first search process in a set of (partially) independent sub-processes, which autonomously evaluate sub-trees of the search space.

Specifically, the whole problem can be split by assigning each subtree rooted in $TT|_X$, where X is a single transaction id in the initial dataset, to an independent sub-process. Each sub-process applies the centralized version of Carpenter on its conditional transposed table $TT|_X$ and extracts a subset of the final closed itemsets. The subsets of closed itemsets mined by each sub-process are merged to compute the whole closed itemset result. Since the sub-processes are independent, they can be executed in parallel by means of a distributed computing platform, e.g., Hadoop. Figure 5.3 shows the application

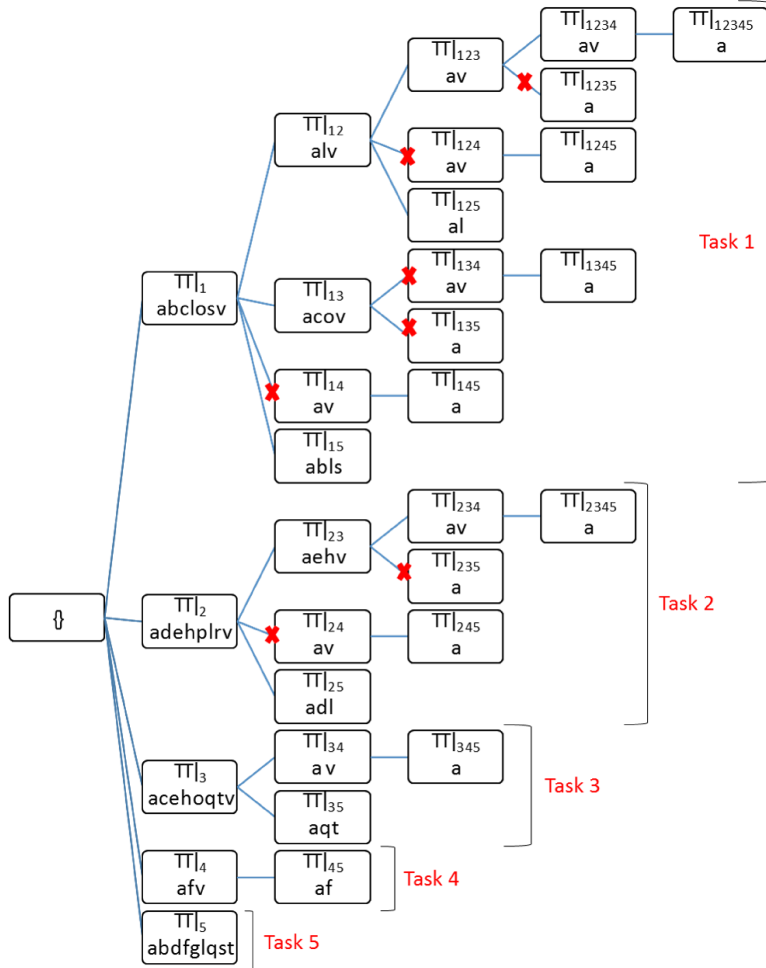


Fig. 5.3 Running toy example: each node expands a branch of the tree independently. For the sake of clarity, pruning rule 1 and 2 are not applied. The pruning rule 3 is applied only within the same task: the small crosses on the edges represent pruned nodes due to local pruning rule 3, e.g. the one on node $\{2\ 4\}$ represents the pruning of node $\{2\ 4\}$.

of the proposed approach on the running example. Specifically, five independent sub-processes are executed in the case of the running example, one for each row (transaction) of the original dataset. The crosses on the nodes represent the local pruning within each parallel task. Partitioning the enumeration tree in sub-trees allows processing bigger enumeration trees with respect to the

centralized version. However, this approach does not allow fully exploiting pruning rule 3 because each sub-process works independently and is not aware of the partial results (i.e., closed itemsets) already extracted by the other sub-processes. Hence, each sub-process can only prune part of its own search space by exploiting its “local” closed itemset list, while it cannot exploit the closed itemsets already mined by the other sub-processes. For instance, Task T2 in Figure 5.3 extracts the closed itemset av associated with node $TT|_{2,3,4}$. However, the same closed itemset is also mined by T1 while evaluating node $TT|_{1,2,3}$. In the centralized version of Carpenter, the duplicate version of av associated with node $TT|_{1,2,4}$ is not generated because $TT|_{1,2,4}$ follows $TT|_{1,2,3}$ in the depth first search, i.e., the tasks are serialized and not parallel.

Since pruning rule 3 has a high impact on the reduction of the search space, its inapplicability leads to a negative impact on the execution time of the distributed algorithm (see Section 5.4 for further details). To address this issue, we share partial results among the sub-processes. Each independent sub-process analyzes only a part of the search subspace. Then, when a maximum number of visited nodes is reached, the partial results are synchronized through a synchronization phase. Of course, the exploration of the tree finishes also when the subspace has been completely explored.

Specifically, the sync phase filters the partial results (i.e., nodes of the tree still to be analyzed and found closed itemsets) globally applying pruning rule 3. The pruning strategy consists of two phases. In the first one, all the transposed tables and the already found closed itemsets are analyzed. The transposed tables and the closed itemsets related to the same itemset are grouped together in a bucket. For instance, in our running example, each element of the bucket B_{av} can be:

- a frequent closed itemset av extracted during the subtree exploration of the node $TT_{3,4}$,
- a transposed table associated to the itemset av among the ones that still have to be expanded (nodes $TT_{1,2,3}$ and $TT_{2,3,4}$).

We remind the readers that, because of the independent nature of the Carpenter subprocesses, the elements related to the same itemset can be numerous, because obtained in different subprocesses. Please note that all the extracted closed

itemsets come together with the tidlist of the node in which they have been extracted.

In the second phase, in order to respect the depth-first pruning strategy of the rule 3, for each bucket it is kept only the oldest element (transposed table or closed itemset) based on a depth-first order. The depth-first sorting of the elements can be easily obtained comparing the tidlists of the elements of the bucket. Therefore, in our running example from the bucket B_{av} , it is kept the node $TT_{1,2,3}$ (See Figure 5.5) . The transposed tables which are not pruned in this phase are then expanded to continue the enumeration tree exploration.

Afterwards, a new set of sub-processes is defined from the filtered results, starting a new iteration of the algorithm. In the new iteration, the Carpenter tasks process also the frequent closed itemsets obtained in the previous iteration, which are used to enrich the local memory of the task and enhance the effectiveness of the local pruning. The Carpenter tasks process the remaining transposed tables, which are expanded, as before, until the maximum number of processed tables is reached. In order to enhance the effectiveness of the pruning rules related to the local Carpenter task, the tables are processed in a depth-first order. After that, as before, in the synchronization phase, pruning rule 3 is applied. The overall process is applied iteratively by instantiating new sub-processes and synchronizing their results, until there are no nodes left. The application of this approach to our running example is represented in Figure 5.4, in which the small crosses represent the pruning related to the local state memory; and in Figure 5.5, in which the bigger crosses represent the pruning related to the synchronization phase. The table related to the itemset av associated with the tidlist/node $\{2, 3, 4\}$ is pruned because the synchronization job discovers a previous table with the same itemset, i.e. the node associated with the transaction ids combination $\{1, 2, 3\}$. The use of this approach allows the parallel execution of the mining process, providing at the same time a very high reliability dealing with heavy enumeration trees, which can be split and pruned according to pruning rule 3. Of course, this architecture cannot deliver the same pruning efficiency characterizing the centralized implementation of Carpenter in which the complete tree depth-first exploration is known.

The introduction of the sync phase leads also to a better load balancing of the tasks. At each synchronization, the tables to process are redistributed

Algorithm 1 PaMPa-HD at a glance

```

1: procedure PAMPA-HD(minsup; initial TT)
2:   Job 1 Mapper: process each row of TT
                and send it to reducers, using as key values
                the tids of the tidlists
3:   Job 1 Reducer: aggregate  $TT|_x$  and run
                local Carpenter until expansion threshold is
                reached or memory is not enough
4:   Job 2 Mapper: process all the closed itemset
                or transposed tables from the previous job
                and send them to reducers
5:   Job 2 Reducer: for each itemset belonging
                to a table or a frequent closed, keep
                the eldest in a Depth First fashion
6:   Job 3 Mapper: process each closed itemset
                and  $TT|_x$  from the previous job.
                For the transposed tables run local Carpenter
                until expansion threshold is reached
7:   Job 3 Reducer: for each itemset belonging
                to a table or a frequent closed, keep
                the eldest in a Depth First fashion
8:   Repeat Job 3 until there are no more
                conditional tables
9: end procedure

```

among the tasks. Therefore, the task related to the first branches of the tree, which are the ones with more nodes than others, are divided into several subtasks. In this way, as shown Section 5.4, we achieve a better exploitation of the resources. As regards to the categorization introduced in Subsection 3.3, PaMPa-HD can be considered a search space-split approach since the search space is divided and explored within different tasks. Please note that the tasks are independent and output the correct set of frequent closed itemsets. The synchronization task has been introduced to delete the redundant results and prune the search space.

5.3.1 Implementation details

PaMPa-HD implementation uses the Hadoop MapReduce framework. The algorithm consists of three MapReduce jobs as shown in PaMPa-HD pseudocode (Algorithm 1).

The Job 1, whose pseudocode is reported in Algorithm 2, is developed to distribute the input dataset to the independent tasks, which will run a local and partial version of the Carpenter algorithm. The second job performs the synchronization of the partial results and exploits the pruning rules. At the end, the last job interleaves the Carpenter execution with the synchronization

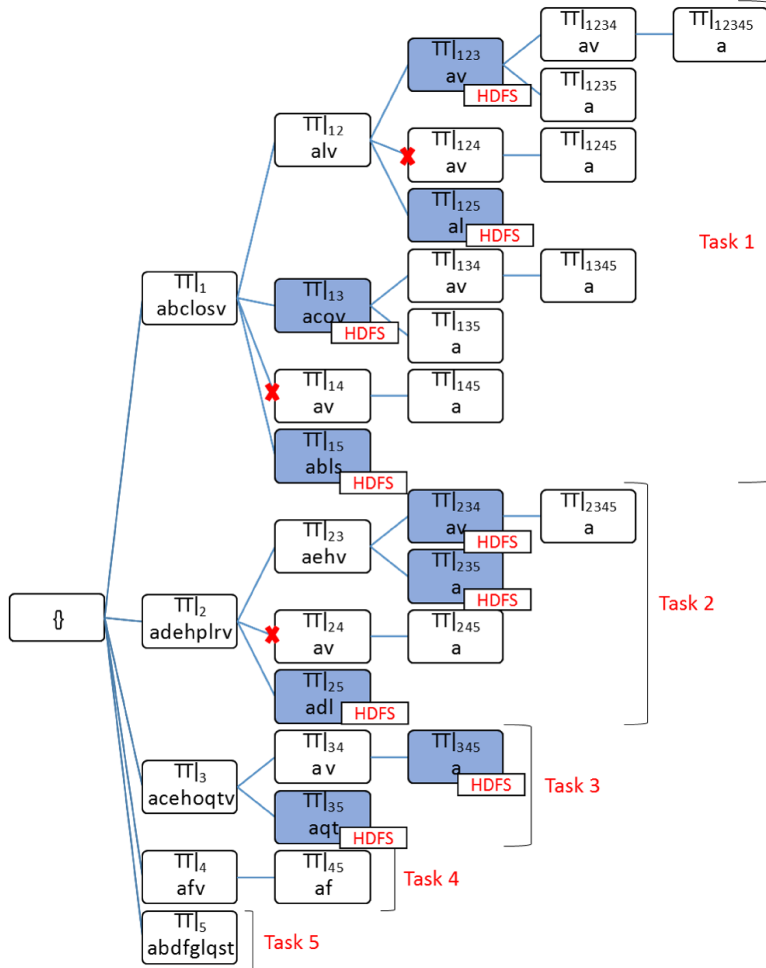


Fig. 5.4 Execution of PaMPa-HD on the running example dataset. For the sake of clarity, pruning rules 1 and 2 are not applied. The dark nodes represent the nodes that have been written to HDFS in order to apply the synchronization job.

phase.

Job 1 (Algorithm 2). Each mapper is fed with a transaction of the input dataset, which is supposed to be in a vertical representation, together with the minsup parameter. As detailed in Algorithm 2, each transaction is in the form $item, tidlist$. For each transaction, the mapper performs the following steps.

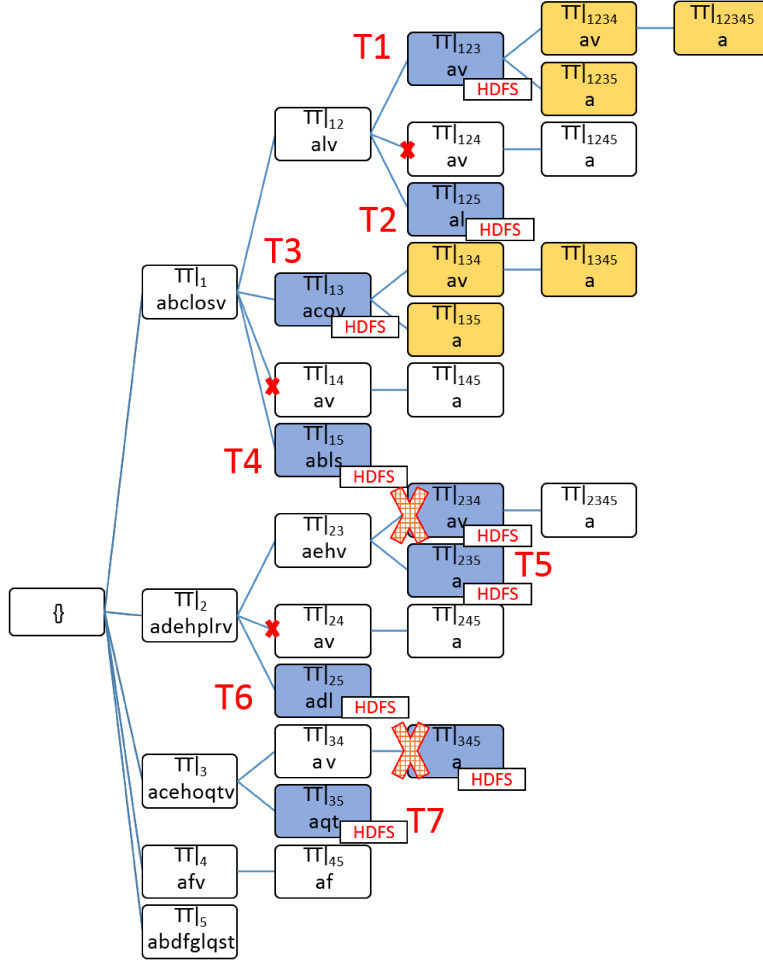


Fig. 5.5 Execution of PaMPa-HD on the running example dataset. For the sake of clarity, pruning rules 1 and 2 are not applied. The big checked crosses on nodes represent the nodes which have been removed by the synchronization job, e.g., the one on node $\{2\ 3\ 4\}$ represents the pruning of node $\{2\ 3\ 4\}$.

For each tid t_i of the input tidlist, given $TL_{greater}$ the set of tids $(t_{i+1}, t_{i+2}, \dots, t_n)$ greater than the considered tid t_i (lines 2-7 in Algorithm 2).

- If $|TL_{greater}| \geq minsup$, output a key-value pair $\langle key = t_i; value = TL_{greater}, item \rangle$, then analyze t_{i+1} of the tidlist.
- Else discard the tidlist.

For instance, if the input transaction is the tidlist of item b ($b, 1\ 2\ 3$) and minsup is 1, the mapper will output three pairs: $\langle \text{key}=1; \text{value}=2\ 3, b \rangle$, $\langle \text{key}=2; \text{value}=3, b \rangle$, $\langle \text{key}=3; \text{value}=b \rangle$.

After the map phase, the MapReduce shuffle and sort phase aggregates the $\langle \text{key}, \text{value} \rangle$ pairs and delivers to reducers the nodes of the first level of the tree, which represent the transposed tables projected on a single tid (lines 10-13 in Algorithm 2). The tables in Figure 5.6 illustrate the processing of a row of the initial Transposed representation of D . Given that each key matches a single transposed table TT_X , each reducer builds the transposed tables with the tidlists contained in the “value” fields. These independent transposed tables match the “projected datasets” definition in Subsection 3.3.

From this table, a local Carpenter routine is run (line 14 in Algorithm 2). Carpenter recursively processes a transposed table expanding it in a depth-first manner (see Section 5.2 for further details). However, the local Carpenter routine stops when the number of processed transposed tables is over the given maximum expansion threshold. This allows periodically performing the synchronization among the parallel tasks and hence enforcing pruning rule 3. All the intermediate results of the local invocation of the Carpenter routine are written to HDFS (lines 15-17 in Algorithm 2).

During the local Carpenter process, the found closed itemsets and the explored branches are stored in memory in order to apply a local pruning. The closed itemsets are emitted as output at the end of the task, together with the tidlist of the node of the tree in which they have been found (lines 18-20 in Algorithm 2). This information is required by the synchronization phase in order to establish which element is the eldest in a depth first exploration, i.e., which element is visited first in a depth first exploration (e.g. the node associated with tidlist $\{1, 2, 3, 5\}$ is eldest than the node associated with tidlist $\{2, 3, 4\}$ in a depth-first exploration order).

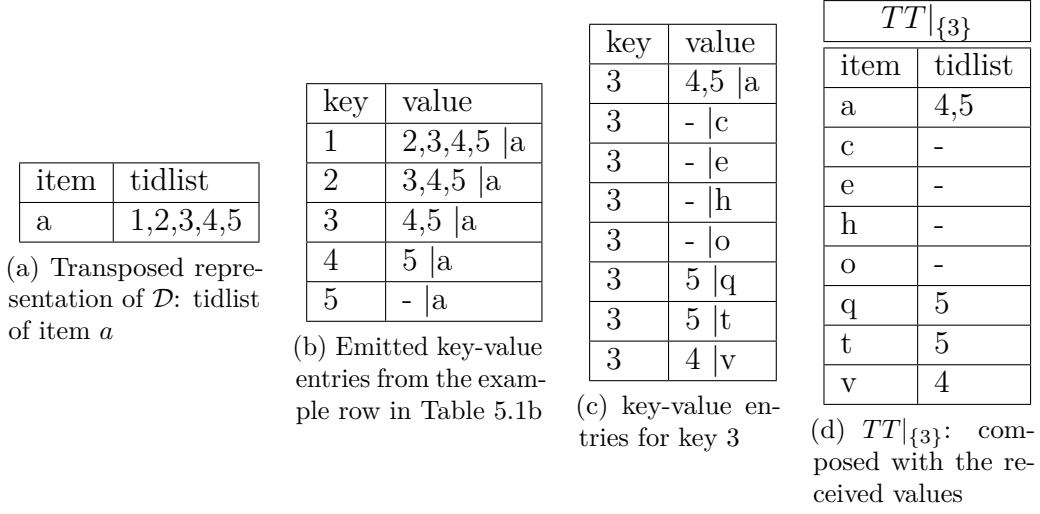


Fig. 5.6 Job 1 applied to the running example dataset ($minsup = 1$): local Carpenter algorithm is run from the Transposed Table 5.6d.

Algorithm 2 Dataset distribution and local and partial Carpenter execution (Job 1)

```

1: procedure MAPPER( $minsup; item_i; tidlist\ TL$ )
2:   for  $j = 0$  to  $|TL| - 1$  do
      tidlist  $TL_{greater}$  : set of tids greater than
      the considered tid  $t_j$ .
3:   if  $|TL_{greater}| \geq minsup$  then
4:     output  $\langle key = t_j; value = TL_{greater}, item \rangle$ 
5:   else Break
6:   end if
7: end for
8: end procedure
9: procedure REDUCER( $key = tid\ X, value = tidlists\ TL[ ]$ )
10:  Create new transposed table  $TT|_X$ 
11:  for each tidlist  $TL_i$  of  $TL[ ]$  do
12:    add  $TL_i$  to  $TT|_X$  (populate the transposed table)
13:  end for
14:  Run Carpenter( $minsup; TT|_X; max\_exp$ )
15:  for each transposed table  $I$  found but not processed do
16:    Output  $\langle itemset; tidlist + TransposedTable\ I\ rows \rangle$ 
17:  end for
18:  for each frequent closed itemset found do
19:    Output( $\langle itemset; tidlist + support \rangle$ )
20:  end for
21: end procedure

```

Job 2 (Algorithm 3). The synchronization phase is a straightforward MapReduce job in which mappers input is the output of the previous job: it

is composed of the closed frequent itemsets found in the previous Carpenter tasks and intermediate transposed tables that still have to be expanded. The itemsets are associated to their minsup and the tidlist related to the node of the tree in which they have been found; the transposed tables are associated to the table content, the corresponding itemset and the table tidlist.

- For each table, the mappers output a pair of the form:
 $\langle \text{key=itemset; value=tidlist, table_rows} \rangle$ (lines 2 - 5 of Algorithm 3);
- for each itemset, the mappers output a pair in the form:
 $\langle \text{key=itemset; value=tidlist, minsup} \rangle$ (lines 6 - 11 of Algorithm 3).

The shuffle and sort phase delivers to the reducers the pairs aggregated by keys. The reducers, which match the buckets introduced in Section 5.3, compare the entries and emit, for the same key or itemset, only the oldest version in a depth first exploration (lines 15 - 21 of Algorithm 3). For instance, referring to our running example in Figure 5.5, in the reducer related to the itemset *av* are collected the entries related to the nodes T_{123} and T_{234} . Since the tidlist 123 is previous than 234 in a depth-first exploration order, the reducer keeps and emits only the entry related to the node T_{123} . With this design, the redundant tables that can be obtained due to the independent nature of the Carpenter tasks, which can explore nodes related to the same itemsets, are discarded. This pruning is very similar to the one performed in centralized memory at the cost of a very MapReduce-like job (similar to a *WordCount* application).

Job 3 (Algorithm 4). This is a mixture of the two previous jobs. In the Map phase all the remaining tables are expanded by a local Carpenter routine. The Reduce phase, instead, applies the same kind of synchronization that is run in the synchronization job. The job has two types of input: transposed tables and frequent closed itemsets. The former are processed respecting a depth-first sorting and expanded until it is reached the maximum expansion threshold (line 5 of Algorithm 4). From that moment, the tables are not expanded but sent to the reducers (lines 6 - 8 of Algorithm 4). Please note that the tree exploration processing the initial transposed tables in a depth-first order is the same to a centralized architecture, enhancing the impact of pruning rule 3 (which strongly relies on this exploration manner). The latter (i.e. the frequent

closed itemsets of the previous PaMPa-HD job) are processed in the following way. If in memory there is already an oldest depth-first entry of the same itemset, the closed itemset is discarded. If there is not, it is saved into memory and used to improve the local pruning effectiveness (lines 2 - 3). At the end of the task, all the frequent closed itemsets found are sent to the reducers, where the redundant elements are pruned. This job is iterated until all the transposed tables have been processed.

Thanks to the introduction of a global synchronization phase (Job 2 and Job 3 in Algorithms 3 and 4), the proposed PaMPa-HD approach is able to apply pruning rule 3 and handle high-dimensional datasets, otherwise not manageable due to memory issues.

Algorithm 3 Synchronization Phase and exploitation of the pruning rule 3 (Job 2)

```

1: procedure MAPPER(Frequent Closed itemset;
   Transposed table)
2:   if Input I is a table then
3:     itemset  $\leftarrow$  ExtractItemset(I)
4:     tidlist  $\leftarrow$  ExtractTidlist(I)
5:     Output(< itemset; tidlist + table I rows >)
6:   else (i.e. input I is a frequent closed Itemset)
7:     itemset  $\leftarrow$  ExtractItemset(I)
8:     tidlist  $\leftarrow$  ExtractTidlist(I)
9:     support  $\leftarrow$  ExtractSupport(I)
10:    Output(< itemset; tidlist + support >)
11:   end if
12: end procedure
13: procedure REDUCER(key = itemset;
   value = itemsets & tables T[ ])
14:   oldest  $\leftarrow$  null
15:   for each itemset or table T of T[ ] do
16:     tidlist  $\leftarrow$  ExtractTidlist(T)
17:     if tidlist previous of oldest in a Depth-First Search then
18:       oldest  $\leftarrow$  T
19:     end if
20:   end for
21:   Output(< itemset + oldest >)
22: end procedure

```

Algorithm 4 Interleaving of the Carpenter execution and synchronization phase (Job 3)

```

1: procedure MAPPER(Frequent Closed itemset; Transposed table)
2:   if Input I is a frequent closed itemset then
3:     save I to local memory
4:   else (i.e. input I is a Transposed Table)
5:     Run Carpenter(minsup; TT|X; max_exp)
6:     for each transposed table I found but not processed do
7:       Output < itemset; tidlist + TransposedTable I rows >
8:     end for
9:   end if
10:  for each frequent closed itemset found do
11:    Output(< itemset; tidlist + support >)
12:  end for
13: end procedure
14: procedure REDUCER(key = itemset;
15:   value = itemsets & tables T[])
16:  oldest ← null
17:  for each itemset or table T of T[] do
18:    tidlist ← ExtractTidlist(T)
19:    if tidlist previous of oldest in a Depth-First Search then
20:      oldest ← T
21:    end if
22:  end for
23:  Output(< itemset + oldest >)
24: end procedure

```

5.4 Experiments

In this section, we present a set of experiments to evaluate the performance of the proposed algorithm. Firstly, we assess the impact on performance of the maximum expansion threshold (*max_exp*) parameter (Section 5.4.1). This phase is mandatory in order to tune-up the parameter configuration to compare the proposed approach with the state-of-the-art algorithms. Because the tuning of the parameter is not trivial, we discuss and experimentally evaluate some self-tuning strategies to automatically set the *max_exp* parameter and improve the performance (Section 5.4.2).

Next, we evaluate the speed of the proposed algorithm, comparing it with the state-of-the-art distributed approaches (Section 5.4.3). Finally, we experimentally analyze the impact of (i) the number of transactions of the input dataset (Section 5.4.4), (ii) the number of parallel tasks (Section 6.6.3), and (iii) the communication costs and load balancing behavior (Section 5.4.6).

Experiments have been performed on two real-world datasets. The first is the PEMS-SF dataset [81], which describes the occupancy rate of different car lanes of San Francisco bay area freeways (15 months of daily data from the California Department of Transportation [82]). Each transaction represents the daily traffic rates of 963 lanes, sampled every 10 minutes. It is characterized by 440 rows and 138,672 attributes ($6 \times 24 \times 963$), and it has been discretized in equi-width bins, each representing 0.1% occupancy rate.

As mentioned, PaMPa-HD design is focused on scaling up in terms of number of attributes, being able to cope with high-dimensional datasets. For this reason, we have used a 100-rows version of the PEMS-SF dataset for all the experiments. However, we have used the full dataset and several down-sampled versions (in terms of number of rows) to measure the impact of the number of transactions on the performance of the algorithm (Section 5.4.4).

The second dataset is the Kent Ridge Breast Cancer [83], which contains gene expression data. It is characterized by 97 rows that represent patient samples, and 24,482 attributes related to genes. The attributes are numeric (integers and floating point). Data have been discretized with an equal-depth partitioning using 20 buckets (similarly to [25]). The discretized versions of the real datasets are publicly available at <http://dbdmg.polito.it/PaMPa-HD/>.

Table 5.1 Datasets

Dataset	Number of transactions	Number of different items	Number of items per transaction
PEMS-SF Dataset	440	8,685,087	138,672
Kent Ridge Breast Cancer Dataset	97	489,640	24,492

PaMPa-HD is implemented in Java 1.7.0_60 using the Hadoop MapReduce API. The experiments were performed on two different configurations. The first, *Configuration 1*, consists of a cluster of 5 nodes running the Cloudera Distribution of Apache Hadoop (CDH5.3.1). Each cluster node is a 2.67 GHz six-core Intel(R) Xeon(R) X5650 machine with 32 Gbyte of main memory. The configuration assumes 17 contemporary independent Yarn containers (tasks) of

6 GB of memory. *Configuration 2* consists of a larger shared Hadoop cluster of 30 nodes with 2.5 TB of total RAM and 324 processing cores provided by Intel CPUs E5- 2620 at 2.6GHz, running the same Cloudera Distribution of Apache Hadoop (CDH5.3.1). We were able to work with 80 contemporary independent Yarn containers (tasks), each one characterized by 4GB of main memory.

5.4.1 Impact of the maximum expansion threshold

In this section we analyze the impact of the maximum expansion threshold (max_exp) parameter, which indicates the maximum number of nodes to be explored before a preemptive stop of each distributed sub-process is forced. This parameter, as already discussed in Section 5.3, strongly affects the enumeration tree exploration, forcing each parallel task to stop before completing the visit of its sub-tree and send the partial results to the synchronization phase. This approach allows the algorithm to globally apply pruning rule 3 and reduce the search space. Low values of max_exp threshold increase the load balancing, because the global problem is split into simpler and less memory-demanding sub-problems, and, above all, facilitate the global application of pruning rule 3, hence a smaller subspace is searched. However, higher values allow a more efficient execution, by limiting the start and stop of distributed tasks (similarly to the context switch penalty) and the synchronization overheads. Above all, higher values enhance the pruning effect of the state centralized memory. In order to assess the impact of the expansion threshold parameter, we have performed two sets of experiments. In the first one we perform the mining on the PEMS-SF (100 transactions) dataset with $minsup = 10$, by varying max_exp from 100 to 100,000,000. The $minsup$ value has been empirically selected to highlight the different performance related to different values (trivial mining would be overwhelmed by overhead costs of the MapReduce framework). In Figure 5.7 are shown the results in terms of execution time and number of iterations (i.e., the number of jobs)². It is clear how the max_exp parameter can influence the performance, with wall-clock times that can be doubled with different configurations. The best performance in terms of execution time is

²Please note that in all the experiments, for the sake of clarity, the confidence intervals (obtained after a sufficient number of executions and with complementary level of significance of 95%) are omitted from the graphs.

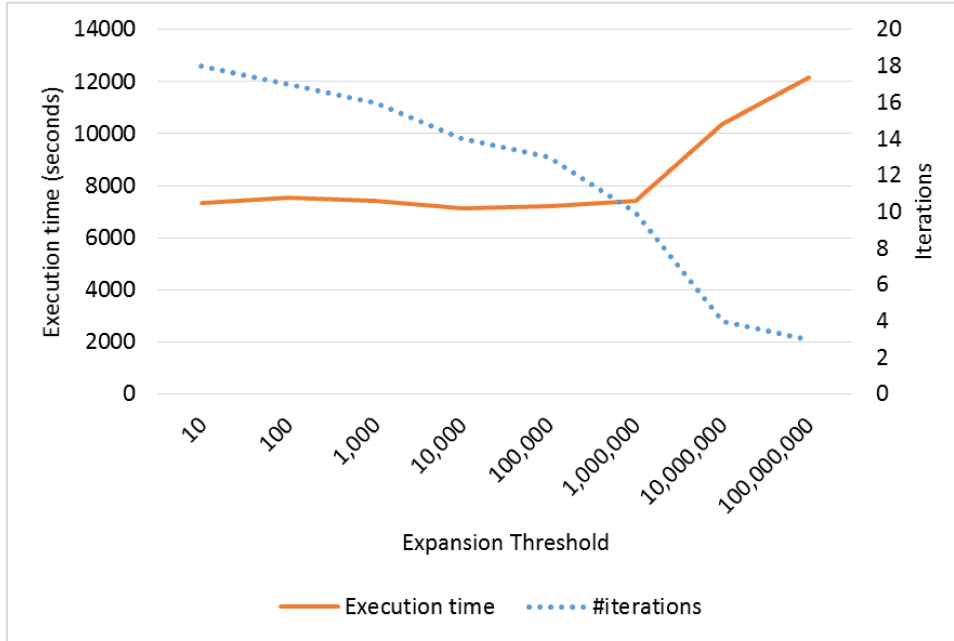


Fig. 5.7 Execution time and number of iterations for different max_exp values on PEMS-SF dataset with $minsup=10$ and Configuration 1.

achieved with a maximum expansion threshold equal to 10,000 nodes. With lower values, the execution times are slightly longer, while there is an evident performance degradation with higher max_exp values.

The same experiment is repeated with the Breast Cancer dataset and a $minsup$ value of 5. As shown in Figure 5.8, even in this case, the best performances are achieved with max_exp equal to 10,000. In this case, differences are more significant with lower max_exp values, although with a non-negligible performance degradation with higher values.

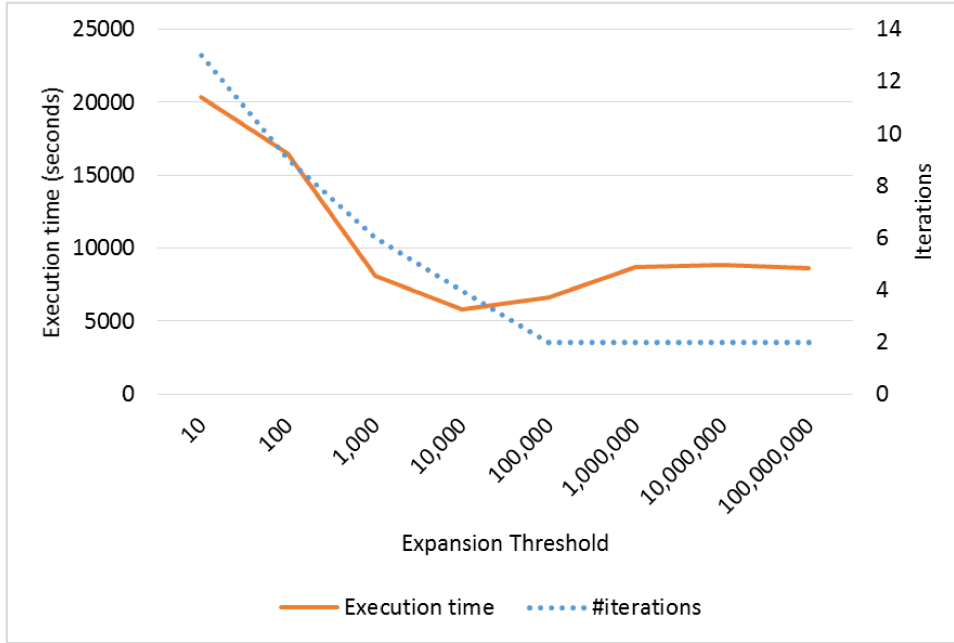


Fig. 5.8 Execution time and number of iterations for different max_exp values on Breast Cancer dataset with $minsup=5$ and Configuration 1.

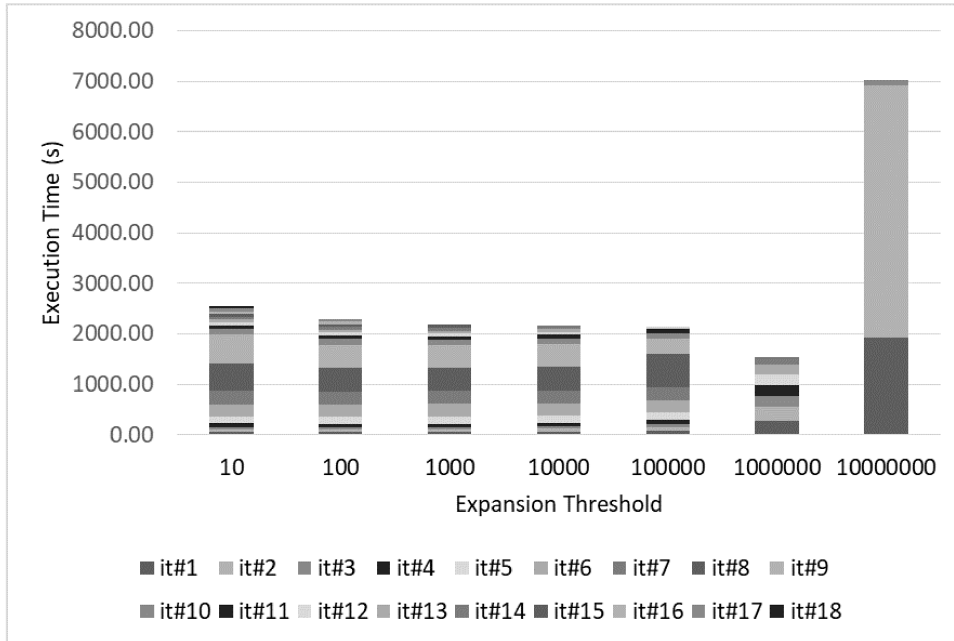


Fig. 5.9 Execution time divided per iteration for different max_exp values on PEMS-SF dataset with $minsup=10$ and Configuration 2.

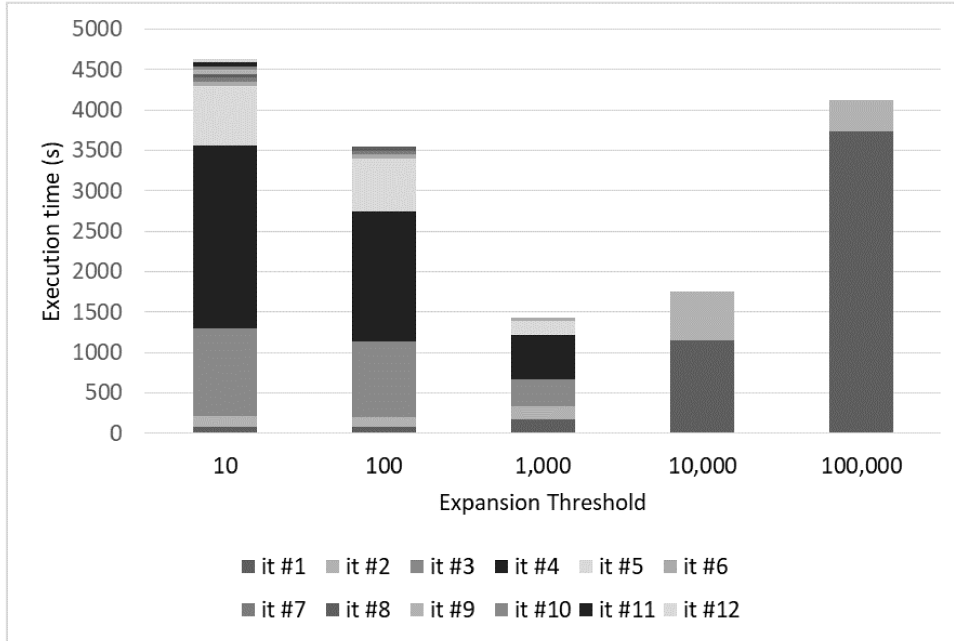


Fig. 5.10 Execution time divided per iteration for different max_exp values on Breast Cancer dataset with $minsup=5$ and Configuration 2.

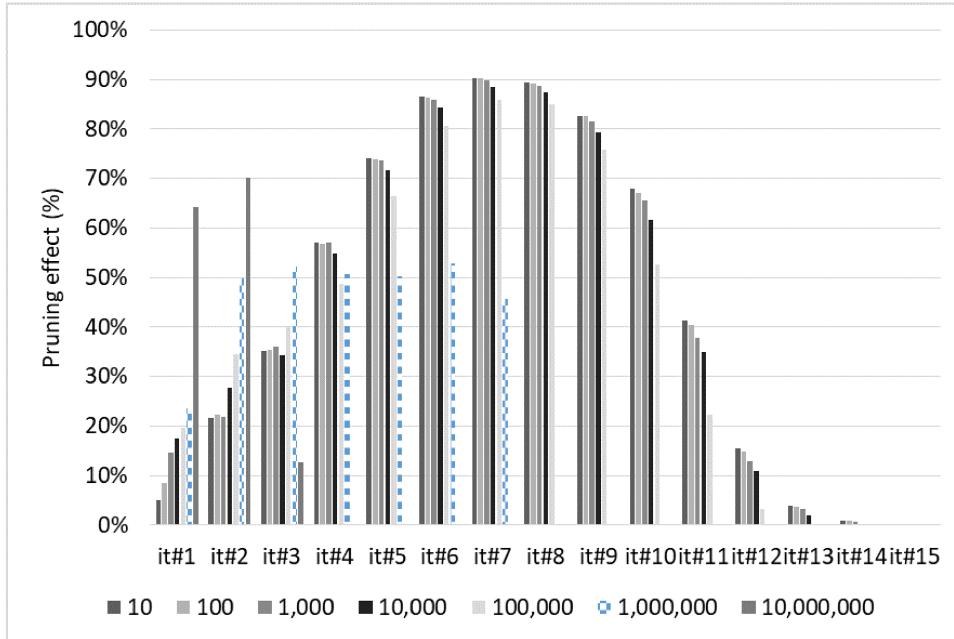


Fig. 5.11 Pruning impact in terms of redundant tables and itemsets produced in each iteration, PEMS-SF dataset with $minsup=10$ and Configuration 2.

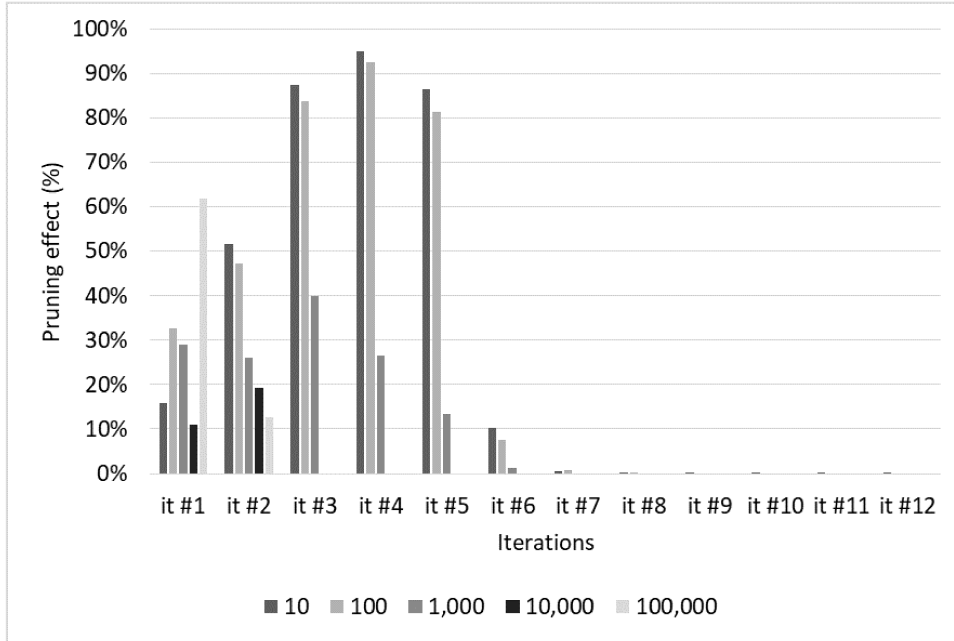


Fig. 5.12 Pruning impact in terms of redundant tables and itemsets produced in each iteration, Breast Cancer dataset with $minsup=5$ and Configuration 2.

Table 5.2 Load Balancing

	Task execution time Breast Cancer		Task execution time PEMS-SF	
	Min	Max	Min	Max
Maximum expansion threshold				
100,000,000	7 m	2h 16m 17s	44s	2h 20m 28s
10	6m 21s	45m 16s	6s	2m 24s

The max_exp choice has a non-negligible impact on the performances of the algorithm. However, as demonstrated by the curves in Figures 5.7 and 5.8, it is very dependent on the distribution of the data and on the tree exploration. It is clear how the benefits of a more effective centralized pruning due to higher max_exp are enhanced for dense datasets such as PEMS-SF. For this dataset, for a large range of max_exp values, the benefits of the additional synchronization are almost completely mitigated by the weaker task level pruning impact and the additional iterations overhead. The motivation is related to the impact of max_exp on the number of synchronization phases and the pruning effectiveness of pruning rule 3. When max_exp increases, the pruning at task level increases as well, while the number of synchronizations

decreases together with their related overhead due the HDFS interactions (the temporary itemsets and related data are stored in HDFS). However, limiting the number of synchronizations has a negative impact on the global pruning effectiveness of pruning rule 3, that is applied less frequently and hence the probability of extracting multiple times the same (useless) itemsets increases. For PEMS-SF (the denser dataset), the overhead given by the synchronization operations is balanced by pruning rule 3 for a large range of values of *max_exp* (up to 1.000.000), because of the enhanced impact of the task level pruning in such a dense dataset. Differently, for Breast Cancer (the sparser dataset), the negative impact of the synchronization phase overhead is initially higher than the positive impact of the application of pruning rule 3 (this is true up to 10.000). The main reason is that, since the dataset is sparse, pruning rule 3 is less effective when short "iterations" are performed (few itemsets are mined and hence the pruning impact of rule 3 is limited).

We run the same experiments with Configuration 2. In Figures 5.9 and 5.10 we reported the performance of the algorithm with respect to the expansion threshold parameter, highlighting the length (execution time) of each iteration of the mining. It is clear how the length of the last iterations is strongly reduced with respect to the central ones. Figures 5.11 and 5.12, instead, plot the pruning impact of the synchronization phase, i.e. the number of elements (tables or closed itemsets) that are deleted. These elements are redundant and their generation is caused by the parallelization which decreases the effect of the centralized pruning. The higher the pruning effect, the more useless elements are produced and, hence, discarded in the synchronization phase. From the trend it is clear how large maximum expansion threshold value configurations are characterized by a greater number of deleted elements between the iterations. On the contrary, low values and frequent synchronization lead to less redundant elements to be deleted and a better optimization of the whole process at the cost of a higher number of iterations. Interestingly, the best configurations for both datasets are the ones related to the steadiest pruning effect along all the iterations. This is particularly evident for PEMS-SF dataset in Figure 5.11 (scattered bars). The value of *max_exp* impacts also on the load balancing of the distributed computation among different nodes. With low values of *max_exp*, each task explores a smaller enumeration sub-tree, decreasing the size difference among the sub-trees analyzed by different tasks, thus improving

the load balancing. Table 5.2 reports the minimum and the maximum execution time of the mining tasks executed in parallel for both datasets, Configuration 1 and for two extreme values of max_exp . The load balance is better for the lowest value of max_exp .

In the next subsection we introduce and motivate some tuning strategies related to max_exp .

5.4.2 Self-tuning strategies

This section introduces some heuristic strategies related to the max_exp parameter. The aim of this experiment is to identify a heuristic technique able to improve the performances of the algorithm and easily configure the algorithm parameter. The heuristic consists in the automatic modification, inside the mining process, of the max_exp parameter, without requiring the user to manually tune it. To introduce the techniques, we provide motivations behind their design in the following. Because of the enumeration tree structure, the first tables of the tree are the most populated. Each node, in fact, is generated from its parent node as a projection of the parent transposed table on a tid. In addition, the first nodes are, in the average, the ones generating more sub-branches. By construction, their transposed table tidlists are, by definition, longer than the ones of their children nodes. This increases the probability that the table could be expanded. For these reasons, the tables of the initial mining phase are the ones requiring more resources and time to be processed. On the other hand, the number of nodes to be processed by each local Carpenter iteration tends to increase with the number of iterations. Still, this factor is mitigated by (i) the decreasing size of the tables and (ii) the eventual end of some branches expansion (i.e. when there are not more tids in the node transposed table). These reasons motivated us to introduce four strategies (Table 5.3) that assume a maximum expansion threshold which is increased with the number of iterations. These strategies start with very low values in the initial iterations (i.e. when the nodes require a longer processing time) and increase max_exp during the mining phases.

Strategy #1 is the simplest: max_exp is increased with a factor of X at each iteration. For instance, if max_exp is set to 10, and X is set to 100

at the second iteration it is raised to 1000 and so on. In addition to this straightforward approach, we leverage information about (i) the execution time of each iteration and the (ii) pruning effect (i.e. the percentage of transposed tables / nodes that are pruned in the synchronization job).

The aim of the *strategy #2* is balancing the execution times among the iterations, trying to avoid a set of very short final jobs. Specifically, *strategy #2* increases, at each iteration, the *max_exp* parameter with a factor of $X^{T_{old}/T_{new}}$, where T_{new} and T_{old} are, respectively, the execution times of the previous two jobs.

For *strategy #3*, we analyzed the pruning impact of the synchronization phase (i.e. the percentage of pruned table due to redundancy). An increasing percentage of pruned tables means that there are a lot of useless tables that are generated. Hence, this could suggest to limit the growth of the *max_exp* parameter. However, the pruning effect is an information which cannot be easily interpreted. In fact, an increasing trend of the pruning percentage is also normal, since the number of nodes that are processed increases exponentially. Given that our intuition is to rise the *max_exp* among the iterations, in *strategy #3*, we increase the *max_exp* parameter with a factor $X^{Pr_{old}/Pr_{new}}$, given Pr_{new} and Pr_{old} the relative number of pruned tables in the previous two jobs. In this way, when the pruning impact increases ($Pr_{new} \geq Pr_{old}$), the growth of *max_exp* is slowed.

Finally, *strategy #4* is inspired by the congestion control of TCP/IP (a data transmission protocol used by many Internet applications [84]). This strategy, called “Slow Start”, assumes two ways for growing the window size (i.e. the number of packets that are sent without congestion issues): an exponential one and a linear one. In the first phase, the window size is increased exponentially until it reaches a threshold (“ssthresh”, which is calculated from some empirical parameters such as Round Trip Time value). From that moment, the growth of the window becomes linear, until a data loss occurs. In *strategy #4*, the *max_exp* is handled like the congestion window size.

In our case, we just inherit the two growth factor approach. Therefore, our “slow start” strategy consists in increasing the *max_exp* of a factor of X ($X \geq 10$) until the last iteration reaches an execution time greater than a given threshold. After that, the growth is more stable, increasing the parameter of

Table 5.3 Strategies

Strategy #1(X)	Constant growth of the parameter	Increasing at each iteration with a factor of X
Strategy #2(X)	Job balancing via execution time analysis	Increasing at each iteration with a factor of $X^{T_{old}/T_{new}}$
Strategy #3(X)	Job balancing via pruning impact analysis	Increasing at each iteration with a factor of $X^{Pr_{old}/Pr_{new}}$
Strategy #4	Slow start	Fast increase with a factor of X , slow increase with a factor of 10

Table 5.4 Best strategies performance

Configurations	PEMS-SF	BreastCancer
Configuration 1	Strategy 1 ($X = 10$, -6,48%)	Strategy 1 ($X = 10,000$ -19,03%)
Configuration 2	Fixed Max_exp (1,000,000)	Strategy 1 ($X = 10$, -25,12%)

a factor of 10. Please note that we have fixed the threshold to the execution time of the first two jobs (Job 1 and Job 2). These jobs, for the architecture of our algorithm, consists of the very first Carpenter iteration. They are quite different than the others since the first Mapper phase builds the initial projected transposed tables (first level of the tree) from the input file. This choice is consistent with our initial aim, which is to normalize the execution times of the last iterations which are often shorter than the first ones.

For Configuration 1, *Strategy #1* is the one achieving the best performances for both datasets. Table 5.4 reports the best performance for each configuration, in terms of relative performance difference with the best results obtained with a fixed *max_exp* parameter. As shown in Table 5.4, the results among the datasets and the configurations are quite different. It is clear how the higher parallelization degree decreases the effect of the centralized pruning. For this reason, the mining with Configuration 2 should be synchronized more frequently with respect to Configuration 1. Breast Cancer data distribution better fits the growth of the parameter, as shown by the better results with

respect to the PEMS-SF dataset. The benefits of the growth of the *max_exp* parameter with PEMS-SF dataset are, indeed, limited. The reason behind this behavior is related to the data distribution. With PEMS-SF dataset, the mining process generates more intermediate results. In this scenario, a more frequent synchronization phase delivers more benefits with respect to the Breast Cancer dataset. The identified best parameter configurations will be used to compare PaMPa-HD with other distributed approaches.

5.4.3 Execution time

Here we analyze the efficiency of PaMPa-HD by comparing it with three distributed state-of-the-art frequent itemset mining algorithms:

1. Parallel FP-growth [36] available in Mahout 0.9 [85], based on the FP-growth algorithm [52]
2. DistEclat [68], based on the Eclat algorithm [53]
3. BigFIM [68], inspired from the Apriori [64] and DistEclat

This set of algorithms represents the most cited implementations of frequent itemset mining distributed algorithms. All of them are Hadoop-based and are designed to extract the frequent closed itemsets (DistEclat and BigFIM actually extract a superset of the frequent closed itemsets). The parallel implementation of these algorithms has been aimed to scale in the number of transactions of the input dataset. Therefore, they are not specifically developed to deal with high-dimensional datasets as PaMPa-HD. The algorithms have been already discussed in detail in Section 3.4.

Even in this case, the frameworks are compared over the two real dataset (PEMS-SF and Breast Cancer datasets) The experiments are aimed to analyze the performance of PaMPa-HD with respect to the best-in-class approaches in high-dimensional use-cases. The first set of experiments has been performed with the 100-rows version PEMS-SF dataset [81] and minsup values 35 to 5.³

³The algorithms parameters, which will be introduced in Subsection 4.1.1, has been set in the following manner. PFP has been set to obtain all the closed itemsets; the prefix length of the first phase of BigFIM and DistEclat, instead, has been set to 3, as suggested by the original paper [68], when possible (i.e. when there were enough 3-itemsets to execute also the second phase of the mining).

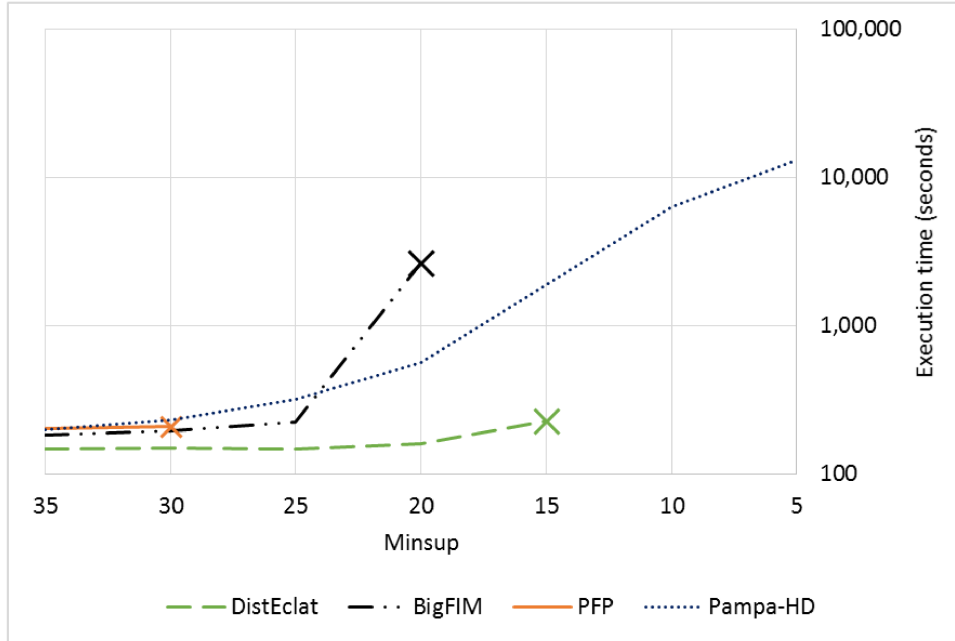


Fig. 5.13 Execution time for different Minsup values on the PEMS-SF dataset (100-rows) and Configuration 1.

As shown in Figure 5.13, in which minsup axis is reversed to improve readability, PaMPa-HD is the only algorithm able to complete all the mining task to a minsup value of 5 rows or 5%. All the approaches show similar behaviors with high minsup values (from 30 to 35). With a minsup of 25, PFP shows a strong performance degradation, being not able to complete the mining. In a similar way, BigFIM shows a performance degradation with a minsup of 20, running out of memory with a minsup of 15. DistEclat, instead, shows very interesting execution time until running out of memory with a minsup of 10. PaMPa-HD, even if slower than DistEclat with minsup values from 25 to 15, is able to complete all the tasks.

The second set of experiments are performed with the Breast Cancer dataset [83]. As reported in Figure 5.14 (even in this case, minsup axis is reversed to improve readability, the minsup is absolute), PaMPa-HD is the most reliable and fast approach. This time, BigFIM is not able to cope even with the highest minsup values, while PFP shows very slow execution times and runs out of memory with a minsup value of 6. DistEclat is able to achieve good performances but is always slower than PaMPa-HD (with a minsup value equal to 4, it is not able to complete the mining within several days

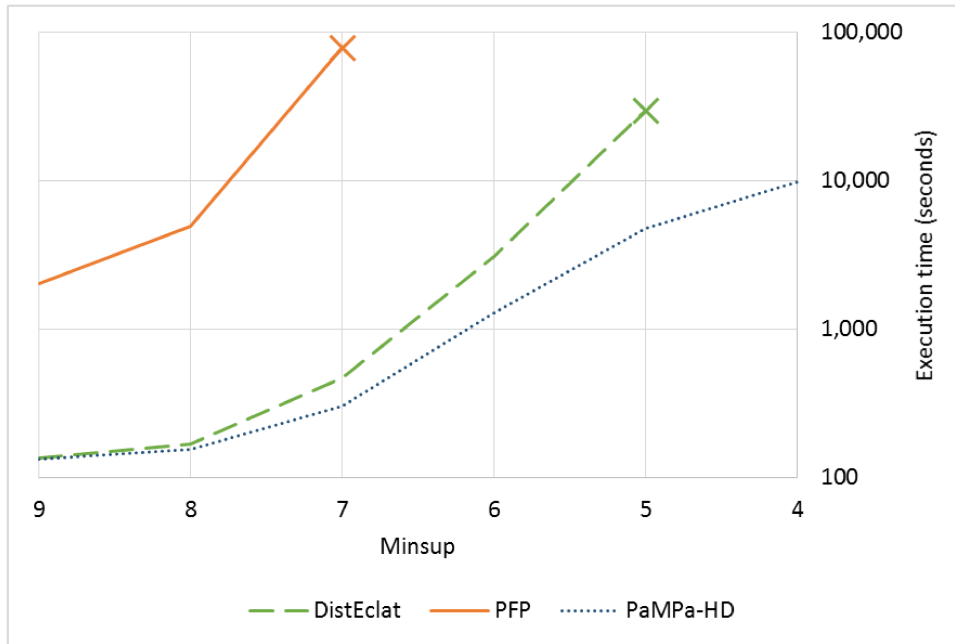


Fig. 5.14 Execution time for different Minsup values on the Breast Cancer dataset and Configuration 1.

of computation). We repeated the same experiments with Configuration 2. The results (see Figures 5.15 and 5.16) are similar to the previous ones, with PaMPa-HD demonstrating to be the most reliable solution. Actually, it is the only approach able to benefit of the higher parallelization degree. In fact, PFP does not show any improvement and it has been interrupted after 12 hours of processing. BigFIM and DistEclat performance are worsened by the less amount of memory available for each process.

From these results, we have seen how traditional best-in-class approaches such as BigFIM, DistEclat and PFP are not suitable for high-dimensional datasets. They are slow and/or not reliable when coping with the curse of dimensionality. In some cases characterized by relatively high minsup thresholds, some of the state of the art approaches perform slightly better than PaMPa-HD, even if they are not specifically designed for high dimensional data. This is due to the fact that high support thresholds limit the number of frequent items, hence the dimensionality of the problem decreases, limiting the advantages of PaMPa-HD. Specifically, the issue with PaMPa-HD is that its design includes an interleaving synchronization job allowing to prune redundant itemsets. When the minsup is high, the benefits of this additional phase are less effective

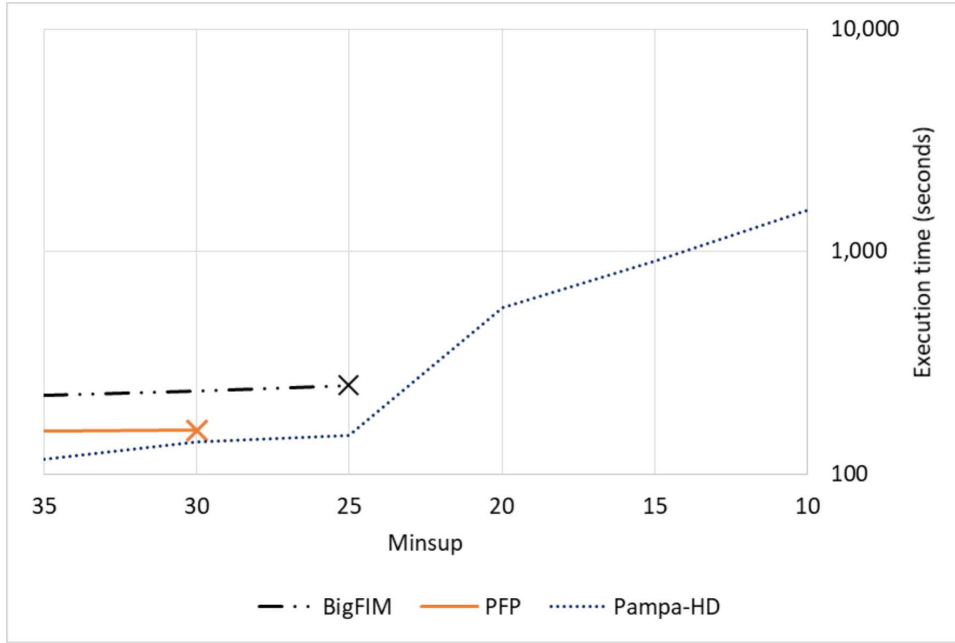


Fig. 5.15 Execution time for different Minsup values on the PEMS-SF dataset and Configuration 2.

than the cons related to the I/O costs and the iterative architecture. This is more evident with PEMS-SF, due to its density and the production of more intermediate tables. For lower minsup values, PaMPa-HD demonstrated to be most suitable approach with datasets characterized by a high number of items and a small number of rows. After the comparison with the state of the art distributed frequent itemset mining algorithms, the next subsections will experimentally analyze the behavior of PaMPa-HD with respect to the number of transactions, number of independent tasks, communication costs and load balancing.

5.4.4 Impact of the number of transactions

This set of experiments measures the impact of the number of transactions on PaMPa-HD performances. To this aim, the PEMS-SF datasets will be used in three versions (100-rows, 200-rows and full). The algorithm is very sensitive to this factor: the reasons are related to its inner structure. In fact, the enumeration tree, for construction, is strongly affected by the number of rows. A higher number of rows leads to:

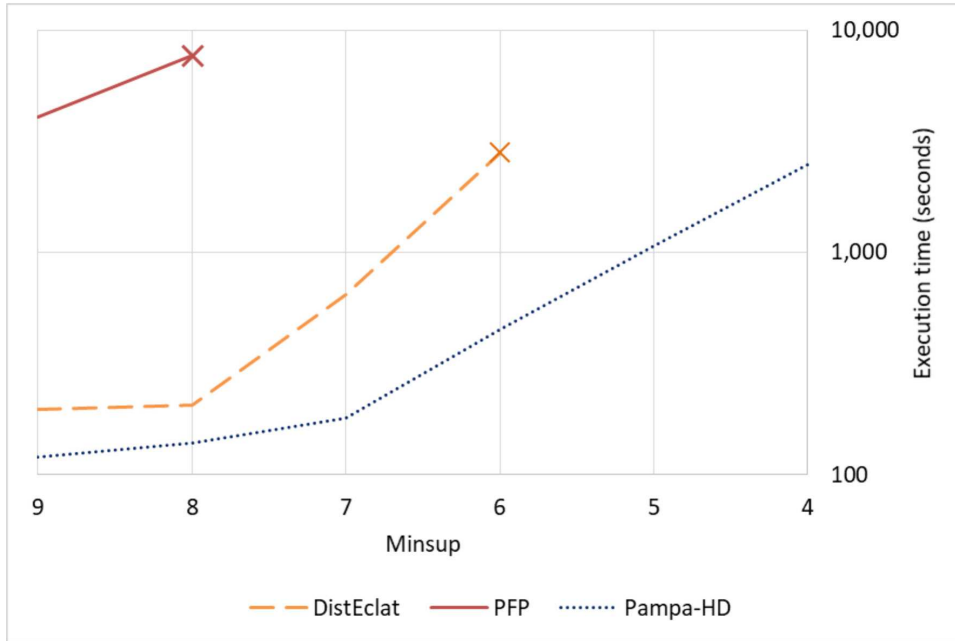


Fig. 5.16 Execution time for different Minsup values on the Breast Cancer dataset and Configuration 2.

1. A higher number of branches. As shown in the example in Figure 5.2, from the root of the tree, it is generated a new branch for each tid (transaction-id) of the dataset.
2. Longer and wider branches. Since each branch explores its research subspace in a depth-first order, exploring any combination of tids, each branch would result with a greater number of sub-levels (longer) and a greater number of sub-branches (wider)

Therefore, the mining processes related to the 100-rows version and to the 200-rows or the full version of PEMS-SF dataset are strongly different. With a number of rows incremented by, respectively, 200% and more than 400%, the mining of the augmented versions of PEMS-SF dataset is very challenging for the enumeration-tree based PaMPa-HD. The performance degradation is resumed in Figures 5.17 and 5.18, where, for instance, with a minsup of 35%, the execution times related to the 100-rows and the full version of the PEMS-SF dataset differ of almost two orders of magnitude.

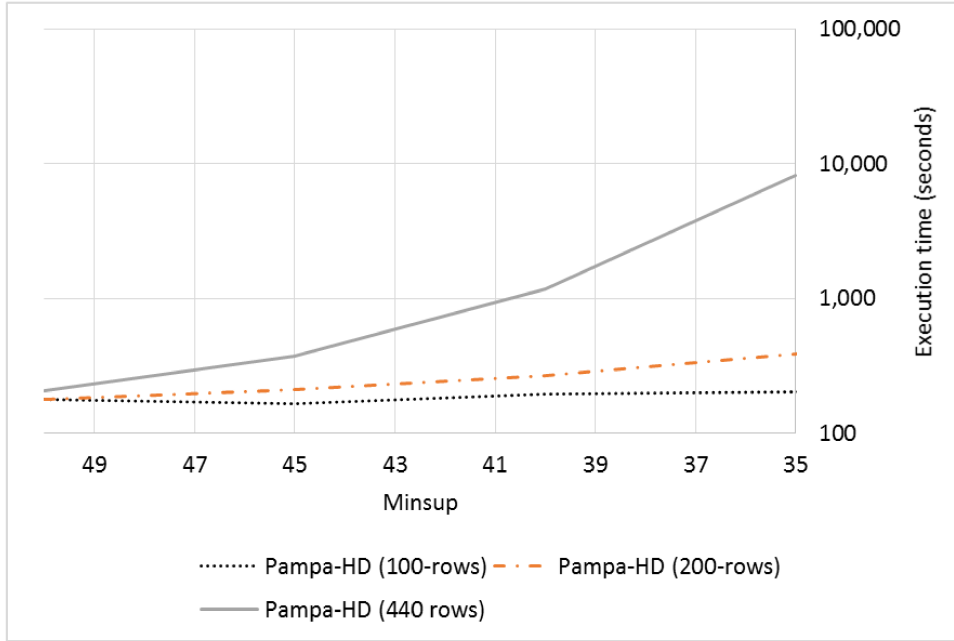


Fig. 5.17 Execution times for different versions of PEMS-SF for PaMPa-HD.

The behavior and the difficulties of PaMPa-HD with datasets with an incremental number of rows, is, unfortunately, predictable. This algorithmic problem represents a challenging and interesting open issues for further developments.

5.4.5 Impact of the parallelization degree

The impact of the number of independent tasks involved in the algorithm execution is a non-trivial issue. Adding a task to the computation would not only deliver more resources such as memory or CPU, but it also leads to split the chunk of the enumeration tree that is explored by each task. On the one hand, this means to reduce the search space to explore, lightening the task load. On the other hand, this reduces the state centralized memory and the impact of the related pruning. It can be interpreted as a trade-off between the benefits of the parallelism against the state. In Figure 5.19 and Figure 5.20, it is reported the behavior of PaMPa-HD with a mining process on the datasets PEMS-SF and Breast Cancer. The minsup values, respectively of 20 and 6, have been chosen in order to highlight the performance differences among the different degree of parallelism and datasets. Interestingly, the mining on PEMS-SF dataset is less sensitive to the number of reducers, with the greatest drop in

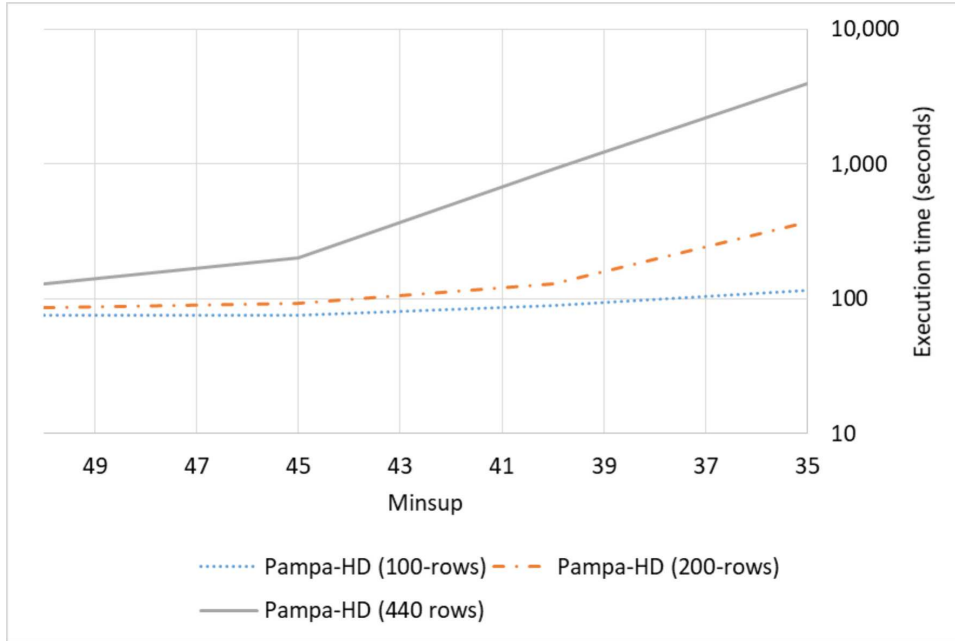


Fig. 5.18 Execution times for different versions of PEMS-SF for PaMPa-HD and Configuration 2.

terms of execution time when the computation passes from 5 to 20 nodes. The experiment of Breast Cancer instead, Figure 5.20, shows a stronger performance gain. As before, the behavior is related to the dataset data distribution which causes the PEMS-SF mining process generating more intermediate tables. In this case, the advantages related to additional independent nodes into the mining is mitigated by the loss of state in the local pruning phase inside the nodes. With additional nodes, each node is pushed to a smaller exploration of the search space, decreasing the effectiveness of the local pruning. These specific results recall a very popular open issue in distributed environments. In problems characterized by any kind of "state" benefit (in this case, the local pruning inside the tasks), a higher degree of parallelism does not lead to better performance a priori.

5.4.6 Load Balancing and communication costs

The last analyses are related to the load balancing and the communication costs of the algorithm. These issues represent very important factor in such a distributed environment. Communication costs are among the main bottlenecks

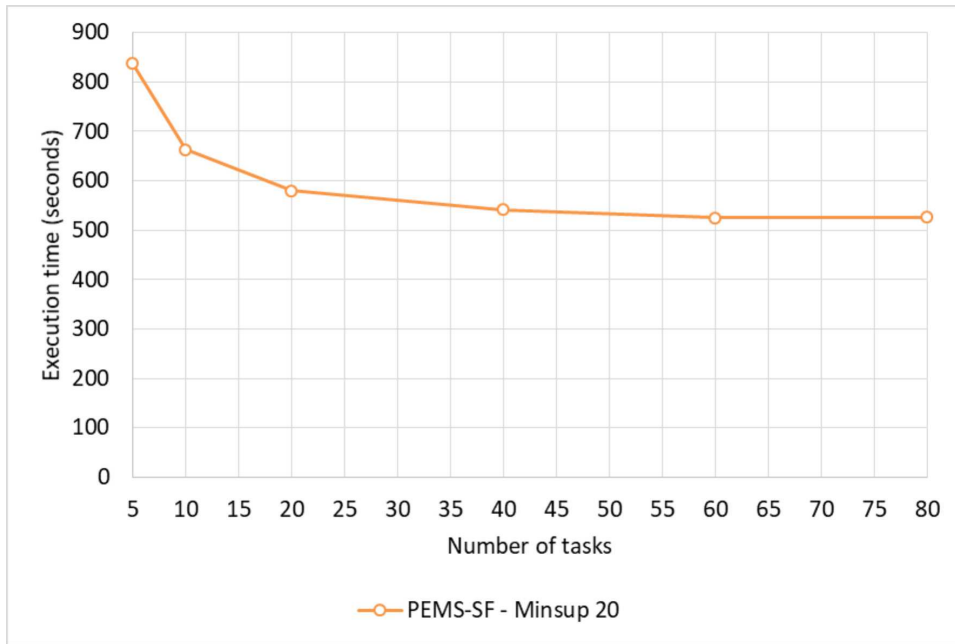


Fig. 5.19 Execution times for PEMS-SF dataset with different number of parallel tasks based on Configuration 2.

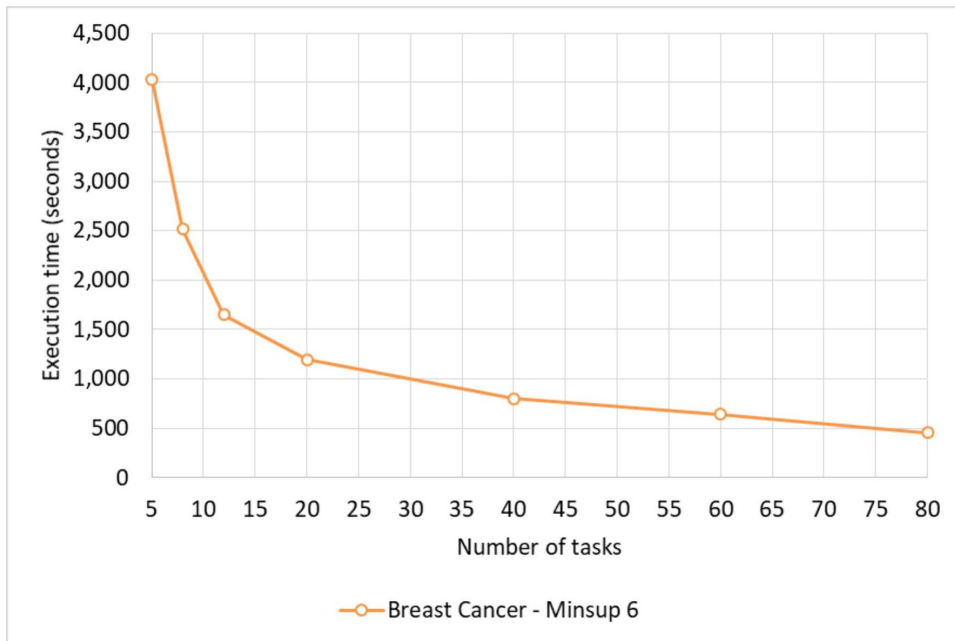


Fig. 5.20 Execution times for Breast Cancer dataset with different number of parallel tasks based on Configuration 2.

for the performance of parallel algorithms [86]. A bad-balanced load among the independent tasks leads to few long tasks that block the whole job.

PaMPa-HD, being based on the Carpenter algorithm, mainly consists on the exploration of an enumeration tree. The basic idea behind the parallelization is to explore the main branches of the tree independently within parallel tasks (Figure 5.3). For this reason, each task needs the information (i.e. transposed tables) related to its branch expansion. The ideal behavior of a distributed algorithm would be to distribute the least amount of data, avoiding redundant information as much as possible. The reason is that network communications are very costly in a Big Data scenario. Unfortunately, the structure of the enumeration tree of PaMPa-HD assumes that some pieces of data of the initial dataset is sent to more than one task. For instance, some data related to nodes $TT|_2$ and $TT|_3$ are the same, because from node $TT|_2$ will be generated the node $TT|_{2,3}$. This is an issue related to the inner structure of the algorithm and a full independence of the initial data for each branch cannot be reached.

In addition, the architecture of the algorithm, with its synchronization phase, increases the I/O costs. In order to prune some useless tables and improve the performance, the mining process is divided in more phases writing the partial results into HDFS. However, as we have already seen when studying the impact of *max_exp* (Figure 5.7 and Figure 5.8), in some cases additional synchronization phases lead to better execution times, despite their related overhead.

We measured the resource utilization in terms of disk usage (read and write phases of HDFS), network communication, and CPU usage. Please note that the values are normalized with respect to the maximum resource utilization. Specifically, Figure 5.21 and 5.22 report the achieved results for the two datasets in an insulated hardware configuration. The spikes are related to the shuffle phases, in which the redundant tables and closed itemsets are removed. The flat part of the curve between the spikes is longer in the case of the Breast Cancer dataset because of the adopted strategy. Its mining has been executed with a more aggressive increasing of the *max_exp* parameter (steps of 10 for PEMS-SF dataset, 10,000 for Breast Cancer dataset), which leads to a very long period without synchronization phases. As regards CPU utilization (Figure 5.22) the degradation is due to the completion of some of the tasks. The higher *max_exp*, as already mentioned, has the counter effect of decreasing the load balance. The trend is, in fact, more flat for the mining of PEMS-SF dataset (Figure 5.21), characterized by more frequent synchronizations.

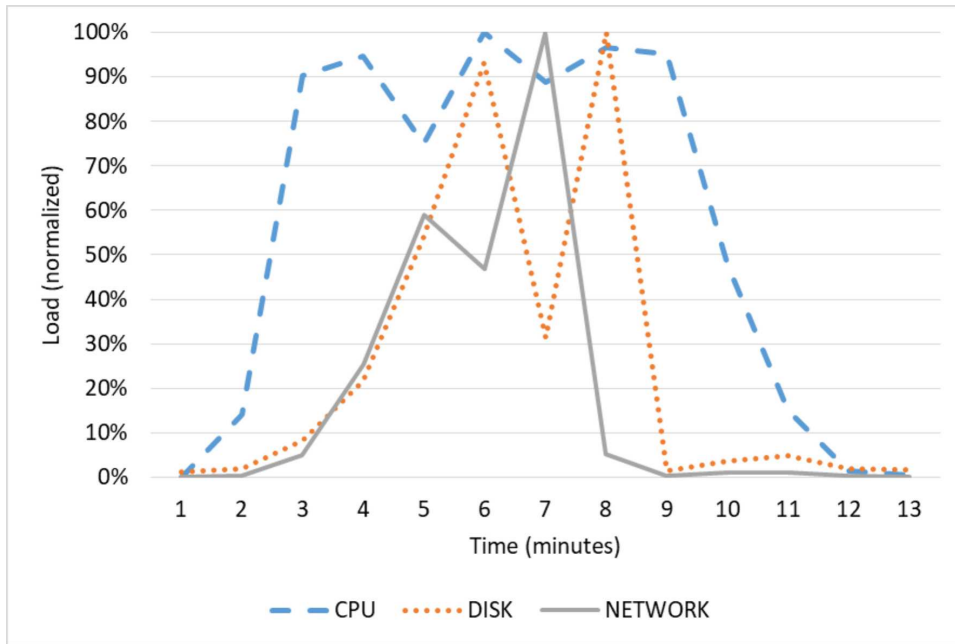


Fig. 5.21 Resource utilization, PEMS-Cancer dataset, minsup=25.

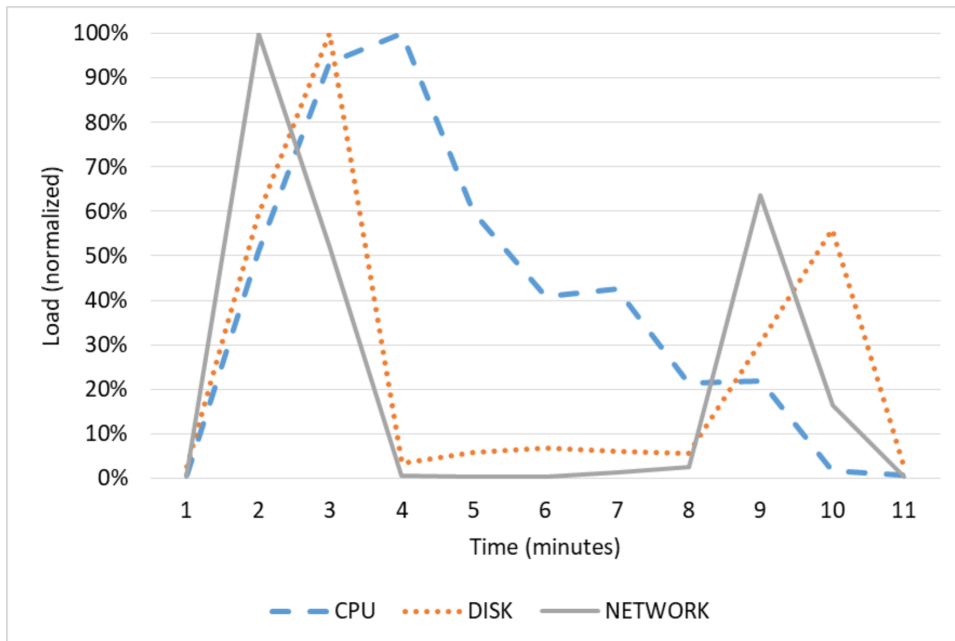


Fig. 5.22 Resource utilization, Breast Cancer dataset, minsup=7.

The load balancing is evaluated by comparing the execution time of the fastest and slowest tasks related to the iteration job in which this difference is strongest. The most unbalanced phase of the job is, not surprisingly, the

Table 5.5 Load Balancing, Configuration 1

Dataset	Slowest Task Execution time	Fastest Task Execution time
PEMS-SF (minsup = 20)	3mins 58 sec	3mins 37sec
Breast Cancer (minsup = 6)	20mins 33sec	8mins 42sec

mapper phase of the Job 3. This job is iterated until the mining is complete and it is the one more affected by the increase of the *max_exp* parameter (iterations characterized by high *max_exp* value are likely characterized by long and unbalanced task). The difference among the fastest and the slowest mapper is shown in Table 5.5. It is clear that the mining on PEMS-SF dataset is more balanced among the independent tasks. Even in this case, the reason is the different increment value in the Strategy #1 (10 for PEMS-SF dataset, 10,000 for Breast Cancer dataset). A slower *max_exp* increasing leads to more balanced tasks.

5.5 Applications

Since PaMPa-HD is able to process extremely high-dimensional datasets, it enriches the set of algorithm able to deal with datasets characterized by a very large variety of features (e.g. [87], [88]). Consequently, many fields of applications which exploits frequent itemset to discover hidden correlations and association rules [89] could benefit of it. The first example is bioinformatics [90] and health environments: researchers in this domain often cope with data structures defined by a large number of attributes, which matches gene expressions, and a relatively small number of transactions, which typically represent medical patients or tissue samples. Furthermore, smart cities and computer vision applications are two important domains which can benefit from our distributed algorithm, thanks to their heterogeneous nature. Another field of application is the networking domain. Some examples of interesting high-dimensional dataset are URL reputation, advertisements, social networks and search engines. One of the most interesting applications, which we plan to investigate in the future, is related to internet traffic measurements. Currently, the market offers an interesting variety of internet packet sniffers like [74], [91].

Collected datasets, which include traffic flows in which the item are flow attributes ([37], [92], [93]), represent already a very promising application domain for data mining techniques, where PaMPa-HD can be efficiently exploited

5.6 Conclusion

This chapter introduced PaMPa-HD, a novel frequent closed itemset mining algorithm able to efficiently parallelize the itemset extraction from extremely high-dimensional datasets. Experimental results show its good scalability and its efficient performance in dealing with real-world datasets characterized by up to 8 million different items and, above all, an average number of items per transaction over hundreds of thousands, on a small commodity cluster of 5 nodes. PaMPa-HD outperforms state-of-the-art algorithms, by showing a better scalability than all popular distributed approaches, such as PFP, DistEclat and BigFIM.

Further developments of the algorithm can be related to the analysis of the trade-off between the benefits of the scalability and the ones related to the local state. In addition, future works could analyze the introduction of better load balancing mechanisms. The increasing *max_exp* parameter introduced by the self-tuning strategies leads to a degradation of the load balancing between the parallel tasks of the job. As shown in Table 5.2, higher *max_exp* values decrease load balancing (i.e. only few tasks running), wasting the resources assigned to the tasks that are already complete. Forcing the synchronization phase after a fixed period of time would limit the amount of time in which the resources are not completely exploited. From the algorithmic point of view, this is not a loss, since the tables are expanded in a depth-first fashion. The last tables, hence, are the ones with highest probability to be pruned. This future development, therefore, would analyze the choice of the *time-out* which forces the synchronization phase.

5.7 Relevant publications

D. Apiletti, E. Baralis, T. Cerquitelli, P. Garza, P. Michiardi, and F. Pulvirenti, “Pampa-hd: A parallel MapReduce-based frequent pattern miner for high-dimensional data,” in *IEEE ICDM Workshop on High Dimensional Data Mining (HDM)*, Atlantic City, NJ, USA, 2015.

D. Apiletti, E. Baralis, T. Cerquitelli, P. Garza, P. Michiardi, and F. Pulvirenti, “A parallel MapReduce algorithm to efficiently support itemset mining on high dimensional data,” *Elsevier Big Data Research* -2017, 10: 53-69.

Chapter 6

Frequent Itemset Mining in Distributed Scalable Frameworks

This chapter of the dissertation presents a concrete example of contextual application of distributed frequent itemset mining. Precisely, the introduced works concern a research problem in which distributed frequent itemset mining is integrated in a wider data mining framework to extract a specific type of itemsets called *misleading generalized itemsets* [10–12].

The framework was initially designed to analyze network traffic logs [9] and provide users with a variety of network analytics services. In this field, in fact, communication profiling, anomaly or security threat detection, and recurrent pattern discovery are very important issues. In a following work, the framework has been extended to support the analysis of traffic law infractions committed by the citizens of Turin, an important business and cultural center in northern Italy. In this case, the target of the analysis is to improve the efficiency of public services, the transparency of public administrations, and the awareness of the degree of civilization of urban people.

This is not the first attempt to take advantage of centralized and distributed data mining techniques to extract actionable insights in real-life scenarios, especially for network traffic analysis. Several approaches address the discovery of significant correlations among data [93, 94], the extraction of knowledge

useful for prediction [95], and the clustering of network data with similar properties [96]. Due to the continuous growth in network speed, petabytes of data may be transferred through a network every day, stressing the limits of existing data mining techniques and setting new horizons for the design of innovative data mining approaches.

The Chapter is organized as follows. Section 6.1 presents NEMiCo (Network Mining in the Cloud), the cited data mining system focused on efficiently discovering interesting knowledge from large network datasets by means of distributed approaches. After that, in Section 6.2, we will introduce an instance of the framework, named MGI-CLOUD (Misleading Generalized Itemset miner in the CLOUD), developed to mine misleading generalized itemsets. Section 6.3 overviews most relevant previous works while Section 6.4 states the problem addressed in this work. Section 6.5 presents the MGI-CLOUD architecture while an experimental evaluation of our approach is reported in Section 6.6. Finally, Section 6.7 draws conclusions and discusses future research directions.

6.1 The NEMiCo architecture

NEMiCo consists of a series of distributed MapReduce jobs related to different steps of the knowledge discovery process. It ranges from network data acquisition to knowledge exploitation, as we will detail in the next chapters. In Figure 6.1 are shown the building blocks of the NEMiCo architecture. To effectively support analysts in discovering different and interesting kinds of knowledge, a broad variety of data mining algorithms can be integrated in the system such as exploratory techniques (e.g., association rules, clustering) and prediction ones (e.g., classification and regression algorithms).

In this job pipeline, each job takes as input the result of one or more preceding jobs, performing a specific step of the data mining process. (each job is performed by one or more MapReduce tasks running on a Hadoop cluster).

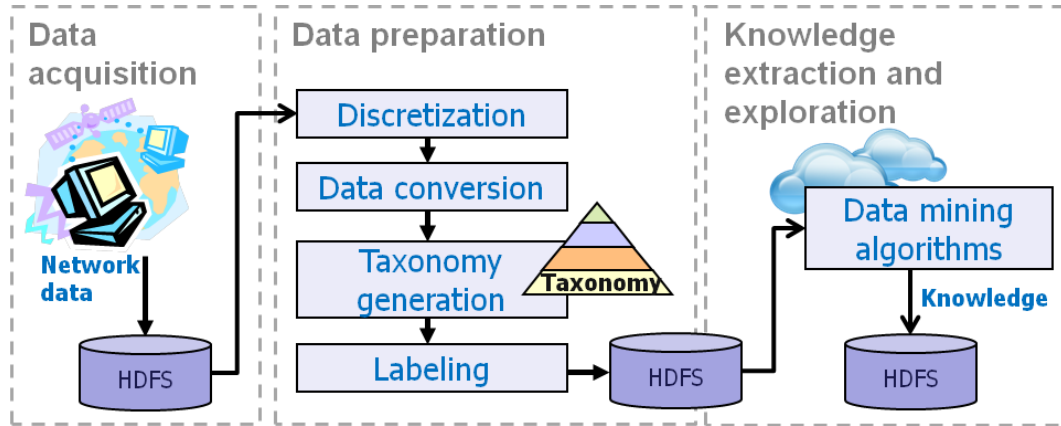


Fig. 6.1 Architecture of NEMiCo

6.1.1 Data acquisition and preprocessing

NEMiCo exploits passive traffic sniffing to acquire massive amounts of network traffic measurements and stores them in HDFS distributed file system. More details about the specific use case data preparation will be provided in Section 6.2.

To suit the raw data to each of the subsequent data mining step, different data preprocessing steps are applied to the input data. A brief description of the main data preparation steps is given below.

Discretization. Discretization concerns the transformation of continuous values into discrete ones. Since some data mining algorithms are unable to cope with continuously valued data, measurement values are discretized prior to running the algorithms. The discretization step can be performed either automatically by using established techniques [97] or semi-automatically by partitioning continuous value ranges into appropriate bins based on the prior knowledge about the measurement domains.

Data conversion. Data conversion entails the transformation of the raw data into the data format expected by the data mining algorithms to apply. It happens that algorithms are designed to handle only a subset of specific format. For example, most association rule mining algorithms are designed to cope with transactional data [97]. Hence, applying association rule mining algorithms requires the acquired data to be tailored to the transactional data format.

Taxonomy generation. The data mining process can be driven by semantics-based models (e.g., taxonomies or ontologies). These models, when available, are used to enrich the source data with multiple-level or multi-faceted information that would result in additional knowledge as output. For instance, a taxonomy, as shown in this Chapter for the use-cases taken into account, consists of set of 'is-a' hierarchies built over the data attributes. These structures are exploited to aggregate specific data values (e.g., the TCP ports) into meaningful higher-level categories. NEMiCO supports both the automatic taxonomy inference over a subset of specific network data attributes (e.g., port number, packet number) and the semi-automatic taxonomy construction.

Labeling. Supervised data mining techniques (e.g., classification) require the labeling of one data attribute as class label. Hence, if the data mining process comprises supervised analyses domain-experts have to specify the class attribute.

The current implementation of NEMiCO includes all the described activities as parallel map jobs.

6.1.2 Knowledge extraction and exploration

Knowledge extraction entails the application of data mining algorithms to find implicit, previously unknown, and potentially useful information from large volumes of network data. NEMiCO comprises novel data mining algorithms that contribute to a paradigm-shift in distributed data mining. The analytics algorithms entail (i) discovering underlying correlations among traffic data (e.g., multiple-level associations among data equipped with taxonomies), (ii) grouping traffic flows with similar properties (e.g., clustering), and (iii) extracting models useful for prediction (e.g., classification, regression).

As already mentioned, the current implementation of NEMiCO comprises Hadoop-based data mining algorithms focused on the extraction of interesting and multiple-level correlations among network data [10]. The next Section will describe the application of such comprehensive framework to the Network traffic and Smart Cities environments.

6.2 Misleading Generalized Itemsets

In this second part of the chapter, as already mentioned, we will extend the discussed distributed network data mining framework to focus on an established pattern mining technique called generalized itemset extraction [98]. The obtained architecture framework has been named MGI-CLOUD (Misleading Generalized Itemset miner in the CLOUD). This technique has already been applied to data coming from several application domains (e.g., market basket analysis [98], network traffic data analysis [99] and genetic data mining [100]). Generalized itemset mining entails discovering correlations among data at different abstraction levels. By exploiting a taxonomy (i.e., a set of is-a hierarchies) built over the analyzed data, frequent generalized itemsets, which represent recurrent co-occurrences among data items at different granularity levels, are extracted. These patterns are worth to be considered by domain experts to transform huge amounts of raw data into useful and actionable knowledge. However, a subset of peculiar high-level patterns should be analyzed separately during manual result inspection. More specifically, each generalized itemset has a correlation type which indicates the strength of the correlation between the corresponding items. Misleading Generalized Itemsets (MGIs) [101] are generalized itemsets whose correlations type is in contrast to those of most of their low-level descendant itemsets. These high-level patterns are worth considering for in-depth analysis because they are likely to represent misleading and thus potentially interesting situations. In [101] MGI extraction is performed in main memory on top of frequent level-sharing itemsets. Unfortunately, when coping with large datasets and low minsup values, a large number of itemsets is often generated thus MGI extraction becomes a challenging task. For this reason, we have introduced a distributed architecture to mine MGIs.

The remainder part of this Chapter presents MGI-CLOUD (Misleading Generalized Itemset miner in the CLOUD), an instance of the more general framework NEMICO designed to efficiently mine MGIs on a distributed computing model. The experimental results show the effectiveness and efficiency of the MGI-CLOUD architecture as well as they demonstrate its applicability to the analyzed use-cases.

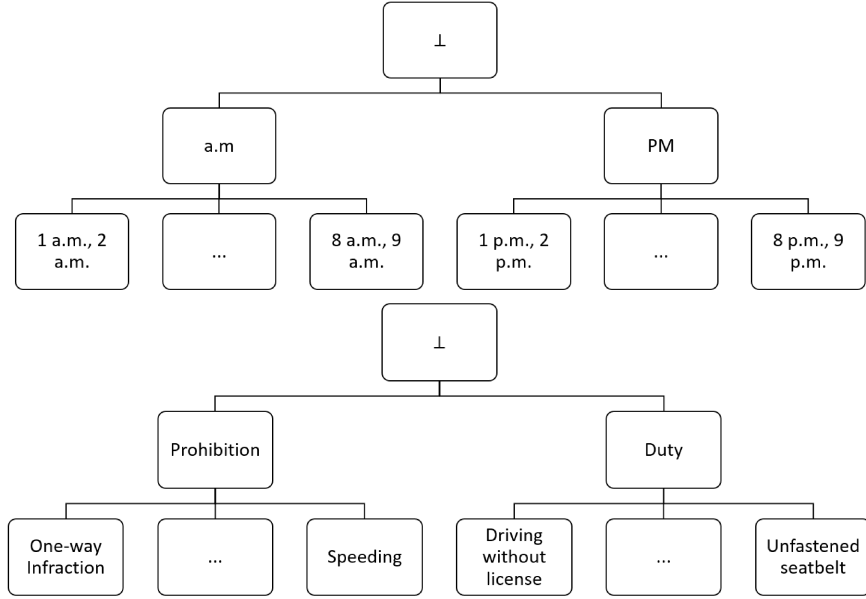
6.3 Related work

As largely introduced in the previous chapters, a relevant research effort has been devoted to large-scale itemset mining based on the MapReduce paradigm. This chapter, instead, introduces and investigates the applicability of a generalized pattern mining technique on the MapReduce platform.

The frequent generalized itemset and association rule mining problems [98] have largely been studied by the data mining community. The firstly proposed approach [98] generates itemsets by considering for each item all its ancestors in the taxonomy. To avoid generating all the possible itemsets, the authors in [102, 103] proposed to push (analyst-provided) constraints into the mining process. In parallel, many algorithm optimizations and variations have been proposed [104–106]. For example, the approach presented in [104] proposes an optimization strategy based on a top-down hierarchy traversal, while in [105] the authors propose to mine closed and maximal generalized itemsets. More recently, a new type of generalized pattern, called Misleading Generalized Itemset (MGI), has been proposed [101]. MGIs are high-level (generalized) itemsets for which a relevant subset of frequent descendants have a correlation type in contrast to their common ancestor. MGIs are worth considering separately from traditional itemsets if their low-level contrasting correlations cover almost the same portion of data as the high-level itemset, because the information provided by traditional high-level patterns becomes misleading. This chapter, hence, describes how to perform MGI mining on the MapReduce platform. Furthermore, it evaluates the MGIs extracted big data acquired in smart city and networking environments.

6.4 Preliminary concepts and problem statement

As largely mentioned in the previous chapters, a transactional dataset \mathcal{D} consists of a set of transactions/records, where each transaction is a set of items [23]. Each item could be seen as a pair (*attribute*, *value*). A taxonomy Γ built over the source dataset \mathcal{D} aggregates the data items into higher-level concepts (i.e., the generalized items). Table 6.1 and Figure 6.2 report two

Fig. 6.2 Example taxonomy built over items in \mathcal{D}

representative examples of relational dataset and taxonomy from one of the data collection (*AperTo dataset.*) which will be used to measure the effectiveness of our technique. This open dataset collects information about traffic law infractions and will be used as running examples.

Table 6.1 Example dataset \mathcal{D} after discretization.

Rid	Infraction name	time stamp
1	One-way infraction	[8 a.m.,9 a.m.]
2	One-way infraction	[8 a.m.,9 a.m.]
3	Speeding	[8 a.m.,9 a.m.]
4	Driving without license	[9 a.m.,10 a.m.]
5	Driving without license	[9 a.m.,10 a.m.]
6	Unfastened seat belt	[4 p.m.,5 p.m.]
7	One-way infraction	[8 a.m.,9 a.m.]

A k -itemset is a set of k (generalized) items. For example, $\{(Time, a.m.), (Infraction\ name, One-way\ infraction)\}$ is a 2-itemset, which indicates that the two items co-occur (possibly at different abstraction levels) in the source data. A generalized itemset I is said to cover a given record $r_i \in D$ if all of its (generalized) items are either contained in r_i or ancestors of items in r_i . I 's support in D is defined as the ratio between the number of records in D that

Table 6.2 Misleading Generalized Itemsets mined from \mathcal{D} . $\min_sup = 10\%$, $\max_neg_cor = 0.70$, $\min_pos_cor = 0.80$, and $\max_NOD = 80\%$.

Frequent itemset (level ≥ 2) [correlation type (Kulc value)]	Frequent descendants [correlation type (Kulc value)]	Not overlapping degree (%)
{ (a.m.), (Prohibition) } [positive (5/6=0.83)]	{ ([8 a.m., 9 a.m.], (One-way infraction)) } [positive (7/8=0.88)] { ([8 a.m., 9 a.m.], (Speeding)) } [[negative (5/8=0.63)]	75
{ (a.m.), (Duty) } [negative (1/2=0.50)]	{ ([9 a.m., 10 a.m.], (Driving without license)) } [positive (1)]	0
{ (p.m.), (Duty) } [negative (2/3=0.66)]	{ ([4 p.m., 5 p.m.], (Unfastened seat belt)) } [positive (1)]	0

are covered by I and the total number of records in D [98, 104, 101]. Given a set of generalized itemsets \mathcal{I} , we also define the coverage of \mathcal{I} with respect to D , hereafter denoted as $cov(\mathcal{I}, D)$, as the ratio between the number of records in D that are covered by any itemset in \mathcal{I} and the total number of records in D . Finally, given two generalized k -itemsets I_1 and I_2 , I_1 is said to be a descendant of I_2 , i.e. $I_1 \in \text{Desc}[I_2, \Gamma]$ if for every item $i_j \in I_1$ there exists an item $i_k \in I_2$ such that either $i_j = i_k$ or i_j is a descendant of i_k with respect to the given taxonomy.

Similar to [104, 107], we target the correlations among items at same abstraction level, i.e. the itemsets that exclusively contain items with the same level. Such patterns are denoted by *level-sharing itemsets* [104]. The itemset correlation measures the strength of the correlation between its items. Similar to [107], in this work we evaluate the correlation of a k -itemset I by means of the Kulczynsky (Kulc) correlation measure [108], defined as $kulc(I) = \frac{1}{k} \sum_{i=1}^k \frac{sup(I, D)}{sup(i_j, D)}$, where $sup(I, D)$ is I 's support in D and i_j is the j -th item in I . Kulc values range from 0 to 1. By properly setting maximum negative and minimum positive Kulc thresholds, hereafter denoted by \max_neg_cor and \min_pos_cor , the itemsets may be classified as negatively correlated, uncorrelated, or positively correlated itemsets according to their correlation value.

Let \mathcal{LSI} be the set of all frequent level-sharing itemsets in \mathcal{D} according to a minimum support threshold \min_sup . Given a frequent level-sharing itemset $X \in \mathcal{LSI}$ of level $l \geq 2$, let $\text{Desc}^*[X, \Gamma]$ be the subset of corresponding level- $(l-1)$ X 's descendants for which the correlation type is in contrast to those of X . A Misleading Generalized Itemset (MGI) is a pattern in the

form $X \triangleright \mathcal{E}$, where $X \in \mathcal{LSGI}$ and $\mathcal{E} = \text{Desc}^*[X, \Gamma]$ [101]. For example, from the dataset in Table 6.1, by enforcing the parameters in the following way:

- $\text{min_sup} = 10\%$
- $\text{max_neg_cor} = 0.70$
- $\text{min_pos_cor} = 0.80$

the MGI: $\{(\text{Time}, \text{a.m.}), (\text{Infraction name}, \text{Prohibition})\} \triangleright \{(\text{Time}, [8 \text{ a.m.}, 9 \text{ a.m.}]), (\text{Infraction name}, \text{Speeding})\}$ is mined. In fact, $\{(\text{Time}: \text{a.m.}), (\text{Infraction name}: \text{Prohibition})\}$ has a positive correlation (0.83), whereas its descendant itemset $\{(\text{Time}: [8 \text{ a.m.}, 9 \text{ a.m.}]), (\text{Infraction name}: \text{Speeding})\}$ is negatively correlated (0.63). To measure the degree of interest of a MGI $X \triangleright \mathcal{E}$ with respect to its corresponding traditional itemset version (X), the Not Overlapping Degree (NOD) measure has been defined in [101]. The NOD of an MGI $X \triangleright \mathcal{E}$ is defined as $\frac{\text{sup}(X, \mathcal{D}) - \text{cov}(\mathcal{E}, \mathcal{D})}{\text{sup}(X, \mathcal{D})}$. It expresses the relative difference between the support of the ancestor itemset X and the coverage of its low-level contrasting correlations in \mathcal{E} . The NOD values range from 0 to 1. The lower NOD value we achieve, the more significant the degree of overlapping between the contrasting low-level correlations in \mathcal{E} and their common ancestor X becomes.

The mining task addressed by this work entails discovering from \mathcal{D} all the MGIs for which the NOD value is less than or equal to a maximum threshold max_NOD . The subset of Misleading Generalized Itemsets mined from Table 6.1 by setting the maximum NOD threshold to 80% is reported in Table 6.2.

6.5 The MGI-CLOUD architecture

The MGI-CLOUD architecture provides a cloud-based service for discovering hidden and actionable patterns among potentially *Big* datasets. it represents a very concrete example of the usage of distributed frequent itemset mining in a real context and as a part of a wider framework. We focus our analysis on two specific case studies, i.e., the analysis of the traffic law infractions committed in an urban environment and the Internet traffic generated by an Italian ISP. To efficiently cope with Big Data, the system implementation is distributed and

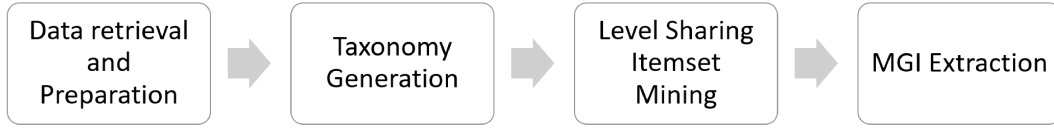


Fig. 6.3 Data transformation and preprocessing

most operations are mapped to the MapReduce programming paradigm [109]. The architecture has been designed as a chain of distributed jobs (Figure 6.3, contextualized version of Figure 6.1) running on a Hadoop cluster, as described below.

6.5.1 Data retrieval and preparation

Data about traffic law infractions was collected by traffic engineers. Reports about daily infractions are collected in local data repositories, which are then integrated into open Big Datasets. A traffic law infraction dataset \mathcal{D} consists of a set of records r , each one representing a different infraction. Each record is a set of *items*, where items are pairs (*attribute*, *value*). *Attribute* can be a specific characteristic of the traffic law infraction (e.g., infraction name, law article) or a property of the context in which the infraction was committed (location, date, time), while *value* is the value assumed by the corresponding attribute. Hereafter, for the sake of simplicity, we focus our analysis on the following attribute subset: *Infraction name*, *Vehicle type*, *Location*, *Date*, and *Time*. We discretized time stamps (e.g., 8.10 a.m.) into 1-hour time slots (e.g., from 8 a.m. to 9 a.m.) using ad-hoc mapping functions. The dataset reported in Table 6.1 is already the output of the discretization step.

The network traffic datasets has been obtained collecting network measurements. For this aim, a passive probe is located on the access link (vantage point) that connects an edge network to the Internet. The passive probe sniffs all incoming and outgoing packets flowing on the link, i.e., packets directed to a node inside the network and generated by a node in the Internet, and vice versa. The probe runs Tstat [74], [75], a passive monitoring tool allowing network and transport layer measurement collection. Tstat rebuilds each TCP connection by matching incoming and outgoing segments. Thus, a flow-level analysis can be performed [75]. A TCP flow is identified by snooping the signaling flags (SYN,

FIN, RST). The status of the TCP sender is rebuilt by matching sequence numbers on data segments with the corresponding acknowledgement (ACK) numbers. To evaluate the MGI-CLOUD tool in real-world application, we focus on a subset of measurements describing the traffic flow among the many provided by Tstat. The most meaningful features, selected with the support of domain experts, comprehends a set of 22 features including RTT, Port, Class and other numeric attributes such as Data Packets, Hops, Windows Size, etc. To obtain reliable estimates on reordering and duplicate probabilities, only TCP flows which last more than $P = 10$ packets are considered. This choice allow focusing the analysis on longlived flows, where the network path has a more relevant impact, thus providing more valuable information.

Since frequent itemset mining requires a transactional dataset of categorical values, data has to be discretized before the mining. The discretization step converts continuously valued measurements into categorical bins. Then, data are converted from the tabular to the transactional format. As already mentioned, attribute selection and data discretization are performed as distributed MapReduce jobs (specifically, as a single map only job). Each record is processed by the map function and, if the number of packets is above the threshold (10 packets), the corresponding discretized transaction is emitted as a result of the mapping. This task entails an inherently parallel elaboration, considering that can be applied independently to each record.

6.5.2 Taxonomy generation

To analyze data from a high-level viewpoint, the datasets are equipped with taxonomies. A taxonomy is a set of is-a hierarchies built over data items in \mathcal{D} . An example taxonomy built over the dataset in Table 6.1 is depicted in Figure 6.2. Items whose value is a high-level aggregation belonging to the taxonomy (e.g., *Duty* in the Infractions taxonomy of Figure 6.2) are called *generalized items*. In Figure 6.4, instead, is reported a sample taxonomy over the attribute RTT of the network traffic dataset. Analyst-provided taxonomies could be generated either manually or semi-automatically by domain experts. We built 3-level hierarchies over the contextual attributes for our analyzes about the traffic law dataset (Location, Time, Date). Specifically, geographical addresses are aggregated into the zip code, which in turn are aggregated into the

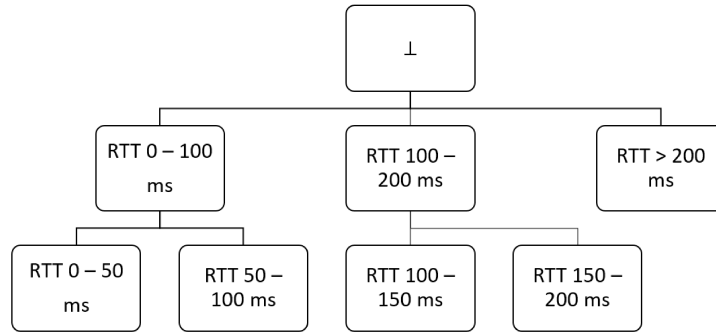


Fig. 6.4 Example of taxonomy over RTT attribute

corresponding district; 1-hour time slots are generalized as the corresponding 4- and 12-hour time slots, while dates are generalized as the corresponding month and year. Furthermore, vehicles are generalized as the corresponding category (e.g., *Car*, *Dumper truck*, *Pickup truck*), and infraction names are aggregated into the corresponding high-level class given by the public administration of Turin.

A similar process has been applied to network traffic dataset with a 2-level organization. Even in this case, the numerical values have been binned in equal-width classes. There were few cases where the taxonomy generation was not so straightforward: for instance, Protocols attributes have been grouped in classes based on use case domains (similar to [110]).

In this work we consider as input balanced taxonomies (i.e., taxonomies whose hierarchies have all the same height). If experts do not provide balanced taxonomies, a re-balancing procedure similar to those adopted in [107] is applied prior to level-sharing itemset mining.

6.5.3 Level-sharing itemset mining

Given a preprocessed infraction dataset and a minimum support threshold min_sup , this job accomplishes the first MGI mining step, i.e., the extraction of all frequent level-sharing itemsets [104]. This job performs the following tasks.

Dataset extension. This task entails producing a new dataset version which integrates taxonomy information. To enable frequent level-sharing itemset

mining from data containing items at different abstraction levels, it generates multiple copies of each record, one for each taxonomy level. While the original record contains only taxonomy leaves (i.e., the dataset items), each copy contains the corresponding combination of item generalizations at a different abstraction level. To avoid unnecessary I/O operations, the extended dataset version is not materialized on disk, but it is directly generated in the map function of the itemset extraction task and then immediately stored into a compact FP-tree structure [23].

Itemset extraction. To efficiently mine frequent level-sharing itemsets [104] from the extended dataset version, this task exploits a variation of the Hadoop-based itemset mining algorithm proposed in [37]. Indeed, since the use case cannot be considered High-Dimensional, PaMPa-HD was not a suitable solution.

6.5.4 MGI extraction

This job performs MGI mining on top of the frequent level-sharing itemsets. Specifically, it accomplishes the task stated in Section 6.4. This step consists of a MapReduce job, as described in the following. The contribution of this job is new because, to the best of our knowledge, no cloud-based service currently supports MGI mining from Big Data.

To extract MGIs we combine each frequent level-sharing itemset I with its corresponding set of descendant itemsets $\text{Desc}[I, \Gamma]$. More specifically, In the map function for each level-sharing itemset I , the following two pairs (*key*, *value*) are emitted: (i) a pair (*key*, *value*), where *key* is the direct ancestor of itemset I and *value* the itemset I with its main properties (i.e., support and Kulc values) and (ii) a pair (*key*, *value*), where *key* is the itemset I is the *value*: itemset I with its main properties (i.e., support and Kulc values). Two pairs are emitted because each itemset can be a descendant of an itemset and a parent of another one at the same time. The first pair allows us to associate I with the ancestor key, whereas the second pair is used to associate I to itself if MGIs in the form $I \triangleright \mathcal{E}$ are extracted. The generated pairs allow us to map each itemset and its corresponding descendants to the same key. Hence, in the reduce function, each key is associated with a specific itemset I and the corresponding set of values contains both the (ancestor) itemset I and

its respective descendants. By iterating on the set of values associated with key I , we generate candidate MGIs $I \triangleright \mathcal{E}$, where \mathcal{E} is the set of I 's descendants in contrast to I in terms of correlation type, and we compute the corresponding NOD values. Finally, only the MGIs satisfying the `max_NOD` threshold are stored into the HDFS file system.

6.6 Experiments

We performed experiments on two real datasets acquired in different domains:

AperTo dataset. This open dataset, available at <http://aperto.comune.torino.it>, collects information about approximately 2 million of traffic law infractions committed in the city of Turin over the 3-year period 2011-2013. The dataset is characterized by five attributes (*Infraction name*, *Vehicle type*, *Location*, *Date*, and *Time*). Its size is approximately 198 MB. Hierarchies over the infraction data items were defined according to the guidelines reported in Section 6.5.2.

BigNetData dataset. This relational network traffic dataset has been obtained by performing different capture stages on a backbone link of a nation-wide ISP in Italy that offers us three different vantage points. The dataset has size 192.56 GB and it consists of 413,012,989 records, i.e., one record for each bi-directional TCP flow). A more detailed dataset description is given in [37].

The MapReduce jobs of the MGI-CLOUD workflow (see Section 6.5) were developed in Java using the new Hadoop Java APIs. The experiments were performed on a cluster of 5 nodes running Cloudera's Distribution of Apache Hadoop (CDH4.5). Each cluster node is a 2.67 GHz six-core Intel(R) Xeon(R) X5650 machine with 32 Gbyte of main memory running Ubuntu 12.04 server with the 3.5.0-23-generic kernel. All the reported execution times are real times obtained from the Cloudera Manager web control panel.

In the experiments we addressed the following issues: (i) the analysis of the characteristics of the mining results achieved with different parameter settings (Section 6.6.1), (ii) the validation of the usefulness of the results achieved for performing in-depth analysis (Section 6.6.2), and (iii) the scalability of the MGI Miner algorithm with the number of nodes (Section 6.6.3). We addressed Tasks (i) and (ii) mainly on AperTo dataset, because data fully complies with

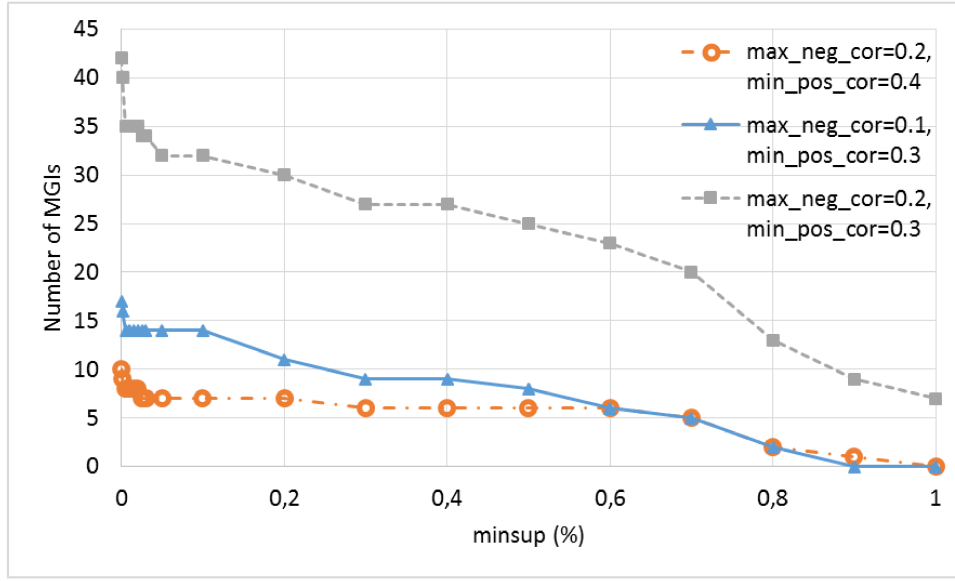


Fig. 6.5 Effect of the minimum support threshold. max_NOD=60%.

the context under analysis (i.e., infraction data analysis), whereas Task (iii) was addressed on BiGNetData, because it is a larger dataset characterized by a fairly complex data distribution.

6.6.1 Characteristics of the mining results

We analyzed the impact of the main input parameters of the MGI Miner algorithm on the number of MGIs mined. Figure 6.5 summarizes the number of mined MGIs by varying the minimum support threshold (min_sup) for different combinations of minimum positive and maximum negative correlation thresholds (max_neg_cor and min_pos_cor, respectively), while Figure 6.6 shows the number of mined MGIs by varying the max_NOD threshold for the same combinations of correlation threshold values.

The number of mined MGIs non-linearly increases by decreasing the minimum support threshold due to the combinatorial increase in the number of generated frequent itemsets [64]. Since most itemsets have correlation between 0.1 and 0.3, the maximum number of MGIs is extracted if max_neg_cor and min_pos_cor fall in this value range, because the generalization process is most likely to flip the itemset correlation types. As expected, the smaller the gap between max_neg_cor and min_pos_cor, the more MGIs are extracted

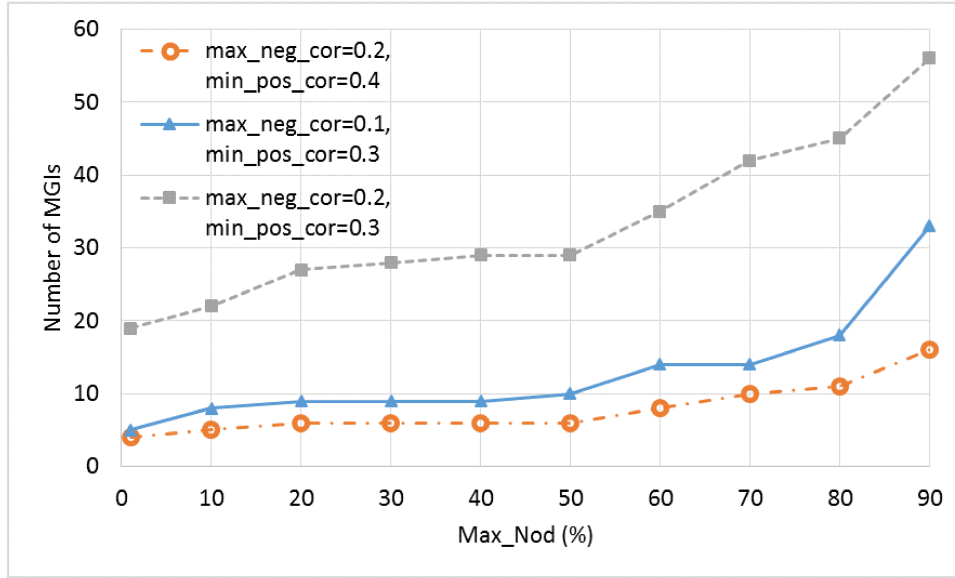


Fig. 6.6 Effect of the maximum NOD threshold. minsup=0.02%.

because correlation type changes occur, on average, more frequently. For all the tested configurations, the set of mined MGIs remains still manageable by domain experts for manual inspection even while setting relatively low support thresholds (e.g., 35 MGIs mined with max_neg_cor=0.2, min_pos_cor=0.3 and min_sup=0.01%).

The number of mined MGIs non-linearly increases while increasing the maximum not overlapping degree threshold max_NOD, because low-level itemsets are more likely to cover a significant portion of data already covered by the corresponding high-level itemsets. However, in all the performed experiments the set of MGIs, which represent anomalies/contrasting situations, remains easily manageable by domain experts for manual exploration.

6.6.2 Result validation

We examined the MGIs extracted from the AperTo dataset to validate their interestingness and usefulness in a real-life context, i.e., the analysis of the traffic law infractions committed in a urban environment.

As a first example, let us consider the following MGI extracted by enforcing min_sup=0.02%, max_neg_cor=0.1, min_pos_cor=0.4, and max_NOD=60%:

$$\{(\text{Location}, \text{Zip code 10125}), (\text{Infraction name}, \text{Prohibition})\} \triangleright \\ \{(\text{Location}, \text{Sommeiller Avenue}), (\text{Infraction name}, \text{One-way infraction})\}.$$

The high-level itemset $\{(\text{Location}, \text{Zip Code 10125}), (\text{Infraction name}, \text{Prohibition})\}$ is negatively correlated, whereas its frequent descendant $\{(\text{Location}, \text{Sommeiller Avenue}), (\text{Infraction name}, \text{One-way infraction})\}$ is positively correlated and it covers a significant portion of data already covered by the high-level itemset ($\sim 59\%$). Hence, to a certain extent, analyzing only the traditional high-level itemset instead of the complete MGI could be misleading. This pattern indicates that in a certain area of Turin, identified by zip code 10125, a category of infractions (prohibitions) is not very likely to occur, whereas for a specific avenue within the area wrong way driving prohibition is violated more commonly than expected. Hence, road signs in Sommeiller Avenue could be either not well visible or misplaced. The public administration of Turin should deem such information to be worthy for signage maintenance and monitoring.

Let us consider now the following MGI:

$$\{(\text{Location}, \text{District 1}), (\text{Vehicle type}, \text{Private car}), (\text{Time}, \text{p.m.})\} \triangleright \\ \{(\text{Location}, \text{Zip code 10122}), (\text{Vehicle type}, \text{Private car}), (\text{Time}, (4 \text{ p.m.}, 8 \text{ p.m.}]), \\ (\text{Location}, \text{Zip code 10121}), (\text{Vehicle type}, \text{Private car}), (\text{Time}, (8 \text{ p.m.}, 12 \text{ p.m.}]), \\ \dots\}.$$

The high-level itemset is positively correlated, whereas 11 of its descendant itemsets are negatively correlated and the NOD value of the mined MGI is 58%. District 1 of Turin appears to be an area in which many infractions are committed by private cars during the afternoon, evening, or night. Hence, traffic corps should monitor the area more carefully in these specific daily time periods. However, in 42% of the subareas of district 1 (e.g., the ones identified by zip codes 10121 and 10122, respectively), infractions are less likely to occur than in the others. Therefore, it would be more advisable to monitor the subareas other than district 1. In summary, MGI extraction from infraction data could help traffic corps optimize road monitoring services and identify anomalous situations be due to either inappropriate citizens' behaviors or to temporary service disruptions.

Even if the qualitative analysis of the results from the network traffic traces dataset requires a domain expert, here we deliver a tentative interpretation

of the most interesting obtained MGI. In this case we focused our analysis on the pattern related to either protocols or RTT values, because we deemed such patterns as interesting to understand application/service server geography. As an example let us consider the following MGI extracted by enforcing $\text{max_neg_cor}=0.2$, $\text{min_pos_cor}=0.3$, and $\text{max_NOD}=70\%$:

$$\{(\text{Class}, \text{Chat}) (\text{RTT-Min}, 100-200)\} \triangleright \\ \{(\text{Class}, 32) (\text{RTT-Min}, 165-170), (\text{Class}, 513) (\text{RTT-Min}, 145-150)\}.$$

The high-level itemset $\{(\text{Class}, \text{Chat}) (\text{RTT} - \text{Min}=100-200)\}$ is negatively correlated whereas its frequent descendants $\{(\text{Class}, 32) (\text{RTT-Min}, 165-170), (\text{Class}, 513) (\text{RTT-Min}, 145-150)\}$ are positively correlated and they cover a significant portion of data already covered by the high-level itemset (especially Class, 32, with the 32%). This means that the traffic flows associated with any chat protocol and characterized by RTT between 100 and 200 ms are less likely to occur than expected, whereas the flows associated with two specific chat protocols, i.e., MSN (class 32) and Skype (class 513), are likely to have RTTs in the ranges 165-170 ms and 145-150 ms, respectively. Hence, in this case, analyzing only the high-level itemset instead of the complete MGI could be misleading and the pattern may indicate that only some specific chat protocols (MSN, Skype) often rely on servers physically located relatively faraway with each other. In this specific example, MGI analysis proves its effectiveness in the network environment, i.e. helping network administrator to understand and optimize networks and identify anomalous situations. Nevertheless, there are many other possible use cases because of the generality of our approach and its compatibility with huge datasets due to its distributed architecture.

6.6.3 Scalability with the number of cluster nodes

We evaluated the scalability of the proposed architecture by measuring the speedup achieved increasing the number of Hadoop cluster nodes. Specifically, we considered three configurations: 1 node, 3 nodes, and 5 nodes. Figure 6.7 reports the speedup achieved setting min_sup to 1%, max_neg_cor to 0.1, min_pos_cor to 0.3, and max_nod to 60%. The first box in Figure 6.7 (i.e., 1 node) corresponds to a run of MGI-CLOUD on a single node. Speedup with increasing nodes is computed against the single-node performance. The

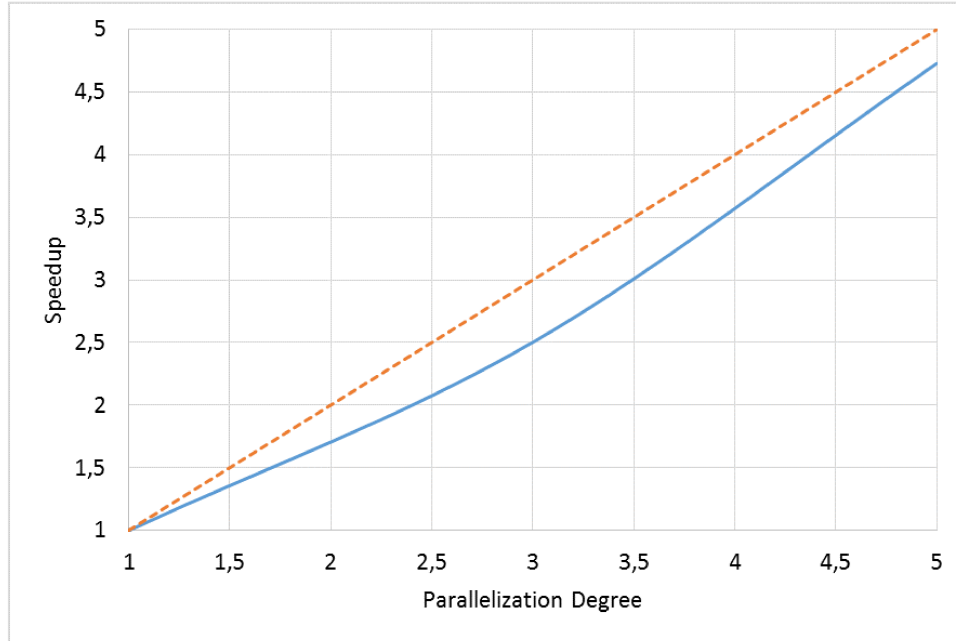


Fig. 6.7 Speedup on the BigNetData dataset.

achieved results show that our approach scales roughly linearly with the number of nodes and the speedup approximately corresponds to the number of cluster nodes.

6.7 Conclusions and future perspectives

This Chapter presented a cloud-based service for discovering Misleading Generalized Itemsets from Big Data equipped with taxonomies. To cope with Big Data the architecture has been designed to run on a distributed Hadoop architecture [109]. A preliminary analysis of the applicability and usefulness of the proposed architecture was conducted on two real Big Data datasets, respectively related to traffic law infractions and to network traffic captures. However, the offered service could find application in many other application contexts, such as social network analysis or financial data analysis. As future work, we aim at optimizing and extending the current Hadoop architecture as well as testing its applicability in other real-life contexts.

6.8 Relevant publications

E. Baralis, L. Cagliero, T. Cerquitelli, S. Chiusano, P. Garza, L. Grimaudo, and F. Pulvirenti, “Nemico: Mining network data through cloud-based data mining techniques,” in *Proceedings of the 2014 IEEE/ACM 7th International Conference on Utility and Cloud Computing*. IEEE Computer Society, 2014, pp. 503–504.

E. Baralis, L. Cagliero, T. Cerquitelli, S. Chiusano, P. Garza, L. Grimaudo, and F. Pulvirenti, “Misleading generalized itemset mining in the cloud,” in *2014 IEEE International Symposium on Parallel and Distributed Processing with Applications*, Aug 2014, pp. 211–216.

D. Apiletti, E. Baralis, L. Cagliero, T. Cerquitelli, S. Chiusano, P. Garza, L. Grimaudo, and F. Pulvirenti, “Network traffic analysis by means of misleading generalized itemsets,” *BIGDAP 2014 - Big Data and Applications*, p. 39, 2014.

E. Baralis, L. Cagliero, T. Cerquitelli, S. Chiusano, L. Grimaudo, F. Pulvirenti, and P. Garza, “Mgi-cloud: discovery of misleading generalized itemsets,” in *22nd Italian Symposium on Advanced Database Systems, SEBD 2014, Sorrento Coast, Italy, June 16-18, 2014.*, 2014, pp. 45–52.

Chapter 7

Conclusion

This dissertation focused on analyzing and enriching the state of the art of one of the most adopted Data Mining techniques: Frequent Itemset Mining. This is an exploratory data analysis method used to discover frequent co-occurrence among the items of a transactional dataset. Frequent Itemset extraction is a very demanding technique in terms of resources. The problem is caused by the inner data structure exploited by the algorithms to explore the search space. Depending on the depth of the analysis (i.e. the selected minimum support threshold) the search-space could potentially consider all the possible items combinations.

Applying frequent itemset mining in Big Data environment is even more challenging. Larger amounts of data lead to bigger data structures to handle and to analyze. Since centralized techniques revealed to be inefficient, in the last years, some scalable frequent itemset mining techniques has been re-designed to leverage distributed frameworks such as Hadoop MapReduce and Spark. One of the main contributions of the dissertation is the analysis of these techniques. Through a structured theoretical and experimental analysis, we taxonomized the proposed works in two families, search-space-split and data-split approaches. Then, we have thoroughly evaluated the behavior and the performances of all the algorithms with an extensive and comprehensive set of the experiments. Thanks to this review, we were able to identify the key aspects of the problem and the open issues. One of the most important was the lack of algorithms designed for high-dimensional data. For this reason,

we have designed a new high-dimensional frequent itemset miner, PaMPa-HD. This algorithm, which represents the second main contribution of this dissertation, partitions the search space in order to leverage the resources of cluster of commodity hardwares. At the same time, however, some aspects of a centralized state are kept, in order to prune the search-space and boost the performances. PaMPa-HD demonstrated to be a reliable solution when dealing with datasets characterized by a long number of items per transactions, outperforming all the competitors. The last contribution of the dissertation is the description of the usage of distributed frequent itemset mining in a wider data mining framework aimed to the extraction of misleading generalized itemsets.

7.1 Future works

Using our work as a starting point, we present possible further development:

Load balancing and Communication Costs. In the experimental evaluation in Chapter 4, we have seen how the importance of Communication Costs for frequent itemset mining, even in a Big Data environment, is secondary with respect to the one related to Load Balancing. High communication costs can be considered a price worth to be paying in the sake of a balanced load assignment to the independent commodity machines. The reason is related to the nature of the problem, in which the most demanding task is related to the inner data structure exploration. This implies that the reading costs hardly dominates the overall performances and that a higher priority should be given to the handling of the inner structures exploited for the itemsets extraction. In a similar way to [86], it could be very interesting for the community to analytically model the trade-off between Communication and I/O costs and the load assigned to a single task (or the degree of parallelism) in the very specific context of frequent itemset mining.

Self-tuning itemset mining frameworks. All the algorithms presented in this dissertation, requires specific skills and expertise to be efficiently leveraged to extract frequent itemsets from large amount of data. The analyst is required to select the best method to efficiently deal with the underlying data and use case features. From this point of view, the improvements in algorithm

usability could be addressed by designing innovative self-tuning itemset mining frameworks, capable of intelligently selecting the most appropriate itemset extraction algorithm and automatically configuring it. This passes from a preliminary analysis of the dataset in order to briefly predict which would be the characteristics of the search space.

Interestingness measures. In literature, many *Interestingness* measures for frequent patterns have been devised [55–63]. These are user-defined measures, closely related to the users’ objective, delivering additional insights with respect to the mere support of the itemset. Depending on the analysis target, the data mining experts could choose the appropriate measure to rank and filter the output of the frequent itemset mining, without being overwhelmed by a huge amount of patterns. As already mentioned in Section 3.1, some works focus on the integration of interestingness measures within the mining process, replacing the support-based constraints [60–63]. The integration of such type of measures within PaMPa-HD represents an interesting possible development of this work. Even in this case, the best candidates measures are the ones supporting upward/downward closure property. This feature would allow the pruning of the search-space during the mining and, as a consequence, the exploration of a much smaller search-space similarly to the support-based pruning. At the same time, because of the independence of the parallel exploration tasks, the pruning should be reliable also with a reduced visibility of the search-space. In PaMPa-HD, for instance, the support is not issued by the parallelization because the current partition strategy does not negatively affect the count of itemsets occurrences. However, *pruning rule 3* (itemset already encountered in the exploration, more details in Section 5.2) is less effective due to the limited visibility of the whole enumeration tree. This rule is not efficient as if it was implemented in a centralized environment, but, at the same time, the limited visibility of the search-space does not cause the pruning of branches that should not be deleted for the correctness of the result.

Sequence mining. Another possible development might be related to the exploration of the domain of Frequent Sequence Mining. Sequential Pattern mining is a data mining technique aimed to discover frequent sequences within a sequence dataset. As frequent pattern mining, centralized methods struggle under huge amount of data or low minsup values. Even in this case, in fact, the mining process becomes challenging when the sequences cannot be loaded into

main memory [111–115]. It might be interesting to try to take advantage of our knowledge of the distributed frequent itemset mining domain to analyze and address the issues related to the distributed extraction of frequent sequential patterns.

References

- [1] X. Wu, X. Zhu, G.-Q. Wu, and W. Ding, “Data mining with big data,” *ieee transactions on knowledge and data engineering*, vol. 26, no. 1, pp. 97–107, 2014.
- [2] E. Junqué de Fortuny, D. Martens, and F. Provost, “Predictive modeling with big data: is bigger really better?” *Big Data*, vol. 1, no. 4, pp. 215–226, 2013.
- [3] I. H. Witten and E. Frank, *Data Mining: Practical machine learning tools and techniques*. Morgan Kaufmann, 2005.
- [4] R. Agrawal, T. Imieliński, and A. Swami, “Mining association rules between sets of items in large databases,” in *Acm sigmod record*, vol. 22, no. 2. ACM, 1993, pp. 207–216.
- [5] D. Borthakur, “The hadoop distributed file system: Architecture and design,” *Hadoop Project*, vol. 11, p. 21, 2007.
- [6] M. Zaharia, M. Chowdhury, T. Das, A. Dave, J. Ma, M. McCauley, M. J. Franklin, S. Shenker, and I. Stoica, “Resilient distributed datasets: A fault-tolerant abstraction for in-memory cluster computing,” in *NSDI’12*, 2012, pp. 2–2.
- [7] D. Apiletti, E. Baralis, T. Cerquitelli, P. Garza, P. Michiardi, and F. Pulvirenti, “Pampa-hd: A parallel mapreduce-based frequent pattern miner for high-dimensional data,” in *IEEE ICDM Workshop on High Dimensional Data Mining (HDM)*, Atlantic City, NJ, USA, 2015. [Online]. Available: <http://ieeexplore.ieee.org/lpdocs/epic03/wrapper.htm?arnumber=7395755>
- [8] D. Apiletti, E. Baralis, T. Cerquitelli, P. Garza, F. Pulvirenti, and P. Michiardi, “A parallel mapreduce algorithm to efficiently support itemset mining on high dimensional data,” *Big Data Research*, vol. 10, no. Supplement C, pp. 53 – 69, 2017. [Online]. Available: <http://www.sciencedirect.com/science/article/pii/S2214579616301046>
- [9] E. Baralis, L. Cagliero, T. Cerquitelli, S. Chiusano, P. Garza, L. Grimaudo, and F. Pulvirenti, “Nemico: Mining network data through cloud-based

- data mining techniques,” in *Proceedings of the 2014 IEEE/ACM 7th International Conference on Utility and Cloud Computing*. IEEE Computer Society, 2014, pp. 503–504.
- [10] —, “Misleading generalized itemset mining in the cloud,” in *Parallel and Distributed Processing with Applications (ISPA), 2014 IEEE International Symposium on*. IEEE, 2014, pp. 211–216.
 - [11] E. Baralis, L. Cagliero, T. Cerquitelli, S. Chiusano, L. Grimaudo, F. Pulvirenti, and P. Garza, “Mgi-cloud: discovery of misleading generalized itemsets,” in *22nd Italian Symposium on Advanced Database Systems, SEBD 2014, Sorrento Coast, Italy, June 16-18, 2014.*, 2014, pp. 45–52.
 - [12] D. Apiletti, E. Baralis, L. Cagliero, T. Cerquitelli, S. Chiusano, P. Garza, L. Grimaudo, and F. Pulvirenti, “Network traffic analysis by means of misleading generalized itemsets,” *BIGDAP 2014 - Big Data and Applications*, p. 39, 2014.
 - [13] R. Xu and D. Wunsch, II, “Survey of clustering algorithms,” *Trans. Neur. Netw.*, vol. 16, no. 3, pp. 645–678, May 2005.
 - [14] C. C. Aggarwal, *Data Classification: Algorithms and Applications*, 1st ed. Chapman & Hall/CRC, 2014.
 - [15] J. Han, H. Cheng, D. Xin, and X. Yan, “Frequent pattern mining: Current status and future directions,” *Data Min. Knowl. Discov.*, vol. 15, no. 1, pp. 55–86, Aug. 2007.
 - [16] E. Glatz, S. Mavromatidis, B. Ager, and X. Dimitropoulos, “Visualizing big network traffic data using frequent pattern mining and hypergraphs,” *Computing*, vol. 96, no. 1, pp. 27–38, 2014.
 - [17] L. Cagliero and P. Garza, “Infrequent weighted itemset mining using frequent pattern growth,” *IEEE transactions on knowledge and data engineering*, vol. 26, no. 4, pp. 903–915, 2014.
 - [18] A. Gupta, A. Mittal, and A. Bhattacharya, “Minimally infrequent itemset mining using pattern-growth paradigm and residual trees,” in *Proceedings of the 17th International Conference on Management of Data*. Computer Society of India, 2011, p. 13.
 - [19] I. Paredes-Oliva, I. Castell-Uroz, P. Barlet-Ros, X. Dimitropoulos, and J. Sole-Pareta, “Practical anomaly detection based on classifying frequent traffic patterns,” in *Computer Communications Workshops (INFOCOM WKSHPS), 2012 IEEE Conference on*. IEEE, 2012, pp. 49–54.
 - [20] D. Brauckhoff, X. Dimitropoulos, A. Wagner, and K. Salamatian, “Anomaly extraction in backbone networks using association rules,” *IEEE/ACM Transactions on Networking (TON)*, vol. 20, no. 6, pp. 1788–1799, 2012.

- [21] B. Liu, W. Hsu, and Y. Ma, “Integrating classification and association rule mining,” in *KDD '98*, 1998, pp. 80–86.
- [22] L. Venturini, P. Garza, and D. Apiletti, *BAC: A Bagged Associative Classifier for Big Data Frameworks*. Cham: Springer International Publishing, 2016, pp. 137–146. [Online]. Available: http://dx.doi.org/10.1007/978-3-319-44066-8_15
- [23] Pang-Ning T. and Steinbach M. and Kumar V., *Introduction to Data Mining*. Addison-Wesley, 2006.
- [24] B. Goethals, “Survey on frequent pattern mining,” *Univ. of Helsinki*, 2003.
- [25] F. Pan, G. Cong, A. K. H. Tung, J. Yang, and M. J. Zaki, “Carpenter: Finding closed patterns in long biological datasets,” in *Proceedings of the Ninth ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, ser. KDD '03. New York, NY, USA: ACM, 2003, pp. 637–642. [Online]. Available: <http://doi.acm.org/10.1145/956750.956832>
- [26] S. Ghemawat, H. Gobioff, and S.-T. Leung, “The google file system,” in *ACM SIGOPS operating systems review*, vol. 37, no. 5. ACM, 2003, pp. 29–43.
- [27] J. Dean and S. Ghemawat, “Mapreduce: simplified data processing on large clusters,” in *OSDI'04*, 2004, pp. 10–10.
- [28] Y. Low, D. Bickson, J. Gonzalez, C. Guestrin, A. Kyrola, and J. M. Hellerstein, “Graphlab: A new framework for parallel machine learning.”
- [29] G. Malewicz, M. H. Austern, A. J. Bik, J. C. Dehnert, I. Horn, N. Leiser, and G. Czajkowski, “Pregel: A system for large-scale graph processing,” in *Proceedings of the 2010 ACM SIGMOD International Conference on Management of Data*, ser. SIGMOD '10. New York, NY, USA: ACM, 2010, pp. 135–146. [Online]. Available: <http://doi.acm.org/10.1145/1807167.1807184>
- [30] “Apache Giraph, last Accessed: 16/10/2015,” 2012. [Online]. Available: <http://giraph.apache.org/>
- [31] “simSQL, a system for stochastic analytics, last Accessed: 16/10/2015,” 2013. [Online]. Available: <http://cmj4.web.rice.edu/SimSQL/SimSQL.html>
- [32] M. P. Forum, “Mpi: A message-passing interface standard,” Knoxville, TN, USA, Tech. Rep., 1994.
- [33] “The Apache Mahout machine learning library, last Accessed: 16/10/2015,” 2013. [Online]. Available: <http://mahout.apache.org/>

- [34] “MADlib: Big Data Machine Learning in SQL, last Accessed: 16/10/2015.” [Online]. Available: <http://madlib.net/>
- [35] “The Apache Spark scalable machine learning library, last Accessed: 16/10/2015,” 2015. [Online]. Available: <https://spark.apache.org/mllib/>
- [36] H. Li, Y. Wang, D. Zhang, M. Zhang, and E. Y. Chang, “PFP: parallel fp-growth for query recommendation,” in *RecSys’08*, 2008, pp. 107–114.
- [37] D. Apiletti, E. Baralis, T. Cerquitelli, S. Chiusano, and L. Grimaudo, “Searum: A cloud-based service for association rule mining,” in *ISPA’13*, 2013, pp. 1283–1290.
- [38] D. Antonelli, E. Baralis, G. Bruno, L. Cagliero, T. Cerquitelli, S. Chiusano, P. Garza, and N. A. Mahoto, “MeTA: Characterization of Medical Treatments at Different Abstraction Levels,” *ACM TIST*, vol. 6, no. 4, p. 57, 2015.
- [39] G. Cong, A. K. H. Tung, X. Xu, F. Pan, and J. Yang, “FARMER: finding interesting rule groups in microarray datasets,” in *Proceedings of the ACM SIGMOD International Conference on Management of Data, Paris, France, June 13-18, 2004*, G. Weikum, A. C. König, and S. Deßloch, Eds. ACM, 2004, pp. 143–154. [Online]. Available: <http://doi.acm.org/10.1145/1007568.1007587>
- [40] T. Cerquitelli and E. D. Corso, “Characterizing thermal energy consumption through exploratory data mining algorithms,” in *Proceedings of the Workshops of the EDBT/ICDT 2016 Joint Conference, EDBT/ICDT Workshops 2016, Bordeaux, France, March 15, 2016.*, 2016. [Online]. Available: <http://ceur-ws.org/Vol-1558/paper15.pdf>
- [41] M. L. Antonie, O. R. Zaiane, and A. Coman, “Application of data mining techniques for medical image classification,” in *MDM/KDD*, 2001.
- [42] E. Baralis, G. Bruno, T. Cerquitelli, S. Chiusano, A. Fiori, and A. Grand, “Semi-automatic knowledge extraction to enrich open linked data,” *Cases on Open-Linked Data and Semantic Web Applications / Patricia Ordonez de Pablos*, In press.
- [43] E. Baralis, L. Cagliero, A. Fiori, and P. Garza, “Mwi-sum: A multilingual summarizer based on frequent weighted itemsets,” *ACM Trans. Inf. Syst.*, vol. 34, no. 1, p. 5, 2015.
- [44] A. de Andrade Lopes, R. Pinho, F. V. Paulovich, and R. Minghim, “Visual text mining using association rules,” *Computers & Graphics*, vol. 31, no. 3, pp. 316–326, 2007. [Online]. Available: <http://dx.doi.org/10.1016/j.cag.2007.01.023>

- [45] M. Mampaey, N. Tatti, and J. Vreeken, “Tell me what i need to know: Succinctly summarizing data with itemsets,” in *Proceedings of the 17th ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, ser. KDD ’11. New York, NY, USA: ACM, 2011, pp. 573–581. [Online]. Available: <http://doi.acm.org/10.1145/2020408.2020499>
- [46] D. Apiletti, P. Garza, and F. Pulvirenti, “A review of scalable approaches for frequent itemset mining,” in *East European Conference on Advances in Databases and Information Systems*. Springer International Publishing, 2015, pp. 243–247.
- [47] D. Apiletti, E. Baralis, T. Cerquitelli, P. Garza, F. Pulvirenti, and L. Venturini, “Frequent itemsets mining for big data: A comparative analysis,” *Big Data Research*, vol. 9, no. Supplement C, pp. 67 – 83, 2017. [Online]. Available: <http://www.sciencedirect.com/science/article/pii/S2214579616300193>
- [48] I. A. T. Hashem, I. Yaqoob, N. B. Anuar, S. Mokhtar, A. Gani, and S. U. Khan, “The rise of “big data” on cloud computing: Review and open research issues,” *Information Systems*, vol. 47, pp. 98–115, 2015.
- [49] K. Kambatla, G. Kollias, V. Kumar, and A. Grama, “Trends in big data analytics,” *Journal of Parallel and Distributed Computing*, vol. 74, no. 7, pp. 2561–2573, 2014.
- [50] A. Pavlo, E. Paulson, A. Rasin, D. J. Abadi, D. J. DeWitt, S. Madden, and M. Stonebraker, “A comparison of approaches to large-scale data analysis,” in *Proceedings of the 2009 ACM SIGMOD International Conference on Management of data*. ACM, 2009, pp. 165–178.
- [51] J. L. Reyes-Ortiz, L. Oneto, and D. Anguita, “Big data analytics in the cloud: Spark on hadoop vs mpi/openmp on beowulf,” *Procedia Computer Science*, vol. 53, pp. 121–130, 2015.
- [52] J. Han, J. Pei, and Y. Yin, “Mining frequent patterns without candidate generation,” in *SIGMOD ’00*, 2000, pp. 1–12.
- [53] M. J. Zaki, S. Parthasarathy, M. Ogihara, and W. Li, “New algorithms for fast discovery of association rules,” in *KDD’97*. AAAI Press, 1997, pp. 283–286.
- [54] B. Mobasher, H. Dai, T. Luo, and M. Nakagawa, “Effective personalization based on association rule discovery from web usage data,” in *Proceedings of the 3rd international workshop on Web information and data management*. ACM, 2001, pp. 9–15.
- [55] P.-N. Tan and V. Kumar, “Interestingness measures for association patterns: A perspective,” in *Proc. of Workshop on Postprocessing in Machine Learning and Data Mining*, 2000.

- [56] A. Zimmermann, “Objectively evaluating interestingness measures for frequent itemset mining,” in *Pacific-Asia Conference on Knowledge Discovery and Data Mining*. Springer, 2013, pp. 354–366.
- [57] J. Rabatel, M. Croitoru, D. Ienco, and P. Poncelet, “Contextual itemset mining in dbpedia,” in *LD4KD: Linked Data for Knowledge Discovery*, vol. 1232. CEUR, 2014.
- [58] P. Lenca, P. Meyer, B. Vaillant, and S. Lallich, “On selecting interestingness measures for association rules: User oriented description and multiple criteria decision aid,” *European Journal of Operational Research*, vol. 184, no. 2, pp. 610 – 626, 2008. [Online]. Available: <http://www.sciencedirect.com/science/article/pii/S0377221706011465>
- [59] L. Geng and H. J. Hamilton, “Interestingness measures for data mining: A survey,” *ACM Computing Surveys (CSUR)*, vol. 38, no. 3, p. 9, 2006.
- [60] S. Brin, R. Motwani, and C. Silverstein, “Beyond market baskets: Generalizing association rules to correlations,” in *Acm Sigmod Record*, vol. 26, no. 2. ACM, 1997, pp. 265–276.
- [61] H. Yao, H. J. Hamilton, and C. J. Butz, “A foundational approach to mining itemset utilities from databases,” in *Proceedings of the 2004 SIAM International Conference on Data Mining*. SIAM, 2004, pp. 482–486.
- [62] R. Meo, “Theory of dependence values,” *ACM Transactions on Database Systems (TODS)*, vol. 25, no. 3, pp. 380–406, 2000.
- [63] R. Meo and D. Ienco, “Replacing support in association rule mining,” *Rare Association Rule Mining and Knowledge Discovery: Technologies for Infrequent and Critical Event Detection: Technologies for Infrequent and Critical Event Detection*, vol. 3, p. 33, 2009.
- [64] R. Agrawal and R. Srikant, “Fast algorithms for mining association rules in large databases,” in *VLDB ’94*, 1994, pp. 487–499.
- [65] L. Vu and G. Alaghband, “Mining frequent patterns based on data characteristics,” in *Proceedings of 2012 International Conference on Information and Knowledge Engineering*, 2012, pp. 369–375.
- [66] M. Herlihy and N. Shavit, “The art of multiprocessor programming,” 2011.
- [67] I. Foster, *Designing and building parallel programs*. Addison Wesley Publishing Company Reading, 1995, vol. 191.
- [68] S. Moens, E. Aksehirli, and B. Goethals, “Frequent itemset mining for big data,” in *SML: BigData 2013 Workshop on Scalable Machine Learning*. IEEE, 2013.

- [69] H. Qiu, R. Gu, C. Yuan, and Y. Huang, “YAFIM: A parallel frequent itemset mining algorithm with spark,” in *IPDPSW’14*, May 2014, pp. 1664–1671.
- [70] S. Moens, E. Aksehirli, , and B. Goethals, “Dist-eclat and bigfim,” <https://github.com/ua-adrem/bigfim>, 2013.
- [71] N. Agrawal, T. Imielinski, and A. Swami, “Database mining: A performance perspective,” In *IEEE TKDE*, vol. 5, no. 6, 1993.
- [72] “Cloudera, last Accessed: 16/10/2015.” [Online]. Available: <http://www.cloudera.com>
- [73] R. Wetzker, C. Zimmermann, and C. Bauckhage, “Analyzing social bookmarking systems: A delicious cookbook,” in *Mining Social Data (MSoDa) Workshop Proceedings*. ECAI 2008, July 2008, pp. 26–30.
- [74] A. Finamore, M. Mellia, M. Meo, M. Munafò, and D. Rossi, “Experiences of internet traffic monitoring with tstat,” *IEEE Network*, vol. 25, no. 3, pp. 8–14, 2011.
- [75] M. Mellia, M. Meo, L. Muscariello, and D. Rossi, “Passive analysis of tcp anomalies,” *Computer Networks*, vol. 52, no. 14, pp. 2663–2676, 2008.
- [76] D. Giordano, S. Traverso, L. Grimaudo, M. Mellia, E. Baralis, A. Tongaonkar, and S. Saha, “Youlighter: An unsupervised methodology to unveil youtube cdn changes,” *arXiv preprint arXiv:1503.05426*, 2015.
- [77] D. Apiletti, E. Baralis, T. Cerquitelli, S. Chiusano, and L. Grimaudo, “Searum: A cloud-based service for association rule mining,” in *12th IEEE International Conference on Trust, Security and Privacy in Computing and Communications, TrustCom 2013 / 11th IEEE International Symposium on Parallel and Distributed Processing with Applications, ISPA-13 / 12th IEEE International Conference on Ubiquitous Computing and Communications, IUCC-2013, Melbourne, Australia, July 16-18, 2013*, 2013, pp. 1283–1290.
- [78] J.-G. Lee and M. Kang, “Geospatial big data: Challenges and opportunities,” *Big Data Research*, vol. 2, no. 2, pp. 74 – 81, 2015, visions on Big Data. [Online]. Available: <http://www.sciencedirect.com/science/article/pii/S2214579615000040>
- [79] M. Cuturi, “UCI machine learning repository. PEMS-SF data set,” 2011. [Online]. Available: <https://archive.ics.uci.edu/ml/datasets/PEMS-SF>
- [80] J. Leskovec and A. Krevl, “SNAP Datasets: Stanford large network dataset collection,” <http://snap.stanford.edu/data>, Jun. 2014.
- [81] M. Lichman, “UCI machine learning repository,” 2013. [Online]. Available: <http://archive.ics.uci.edu/ml>

- [82] “California department of transportation.” [Online]. Available: <http://http://pems.dot.ca.gov/>. Lastaccess: April, 21st 2016
- [83] M. L. data set repository, “Breast cancer dataset (kent ridge.” [Online]. Available: <http://mldata.org/repository/data/viewslug/breast-cancer-kent-ridge-2> Lastaccess: July, 15th 2015
- [84] V. Jacobson, “Congestion avoidance and control,” *SIGCOMM Comput. Commun. Rev.*, vol. 18, no. 4, pp. 314–329, Aug. 1988. [Online]. Available: <http://doi.acm.org/10.1145/52325.52356>
- [85] Apache Software Foundation. Apache mahout:: Scalable machine-learning and data-mining library. [Online]. Available: <http://mahout.apache.org>
- [86] A. D. Sarma, F. N. Afrati, S. Salihoglu, and J. D. Ullman, “Upper and lower bounds on the cost of a map-reduce computation,” *Proc. VLDB Endow.*, vol. 6, no. 4, pp. 277–288, Feb. 2013. [Online]. Available: <http://dx.doi.org/10.14778/2535570.2488334>
- [87] R. Vimeiro and P. Moscato, “A new method for mining disjunctive emerging patterns in high-dimensional datasets using hypergraphs,” *Information Systems*, vol. 40, pp. 1 – 10, 2014. [Online]. Available: <http://www.sciencedirect.com/science/article/pii/S0306437913001221>
- [88] P. Bermejo, L. de la Ossa, J. A. Gámez, and J. M. Puerta, “Fast wrapper feature subset selection in high-dimensional datasets by means of filter re-ranking,” *Knowledge-Based Systems*, vol. 25, no. 1, pp. 35 – 44, 2012, special Issue on New Trends in Data Mining. [Online]. Available: <http://www.sciencedirect.com/science/article/pii/S095070511100027X>
- [89] B. Kamsu-Foguem, F. Rigal, and F. Mauget, “Mining association rules for the quality improvement of the production process,” *Expert Systems with Applications*, vol. 40, no. 4, pp. 1034 – 1045, 2013. [Online]. Available: <http://www.sciencedirect.com/science/article/pii/S0957417412010007>
- [90] J. Nahar, T. Imam, K. S. Tickle, and Y.-P. P. Chen, “Association rule mining to detect factors which contribute to heart disease in males and females,” *Expert Systems with Applications*, vol. 40, no. 4, pp. 1086 – 1093, 2013. [Online]. Available: <http://www.sciencedirect.com/science/article/pii/S095741741200989X>
- [91] Cisco, “Netflow.” [Online]. Available: <http://www.cisco.com/c/en/us/products/ios-nx-os-software/ios-netflow/index.html> Lastaccess: July, 15th 2015
- [92] D. Brauckhoff, X. Dimitropoulos, A. Wagner, and K. Salamatian, “Anomaly extraction in backbone networks using association rules,” *Networking, IEEE/ACM Transactions on*, vol. 20, no. 6, pp. 1788–1799, Dec 2012.

- [93] D. Apiletti, E. Baralis, T. Cerquitelli, and V. D'Elia, "Characterizing network traffic by means of the netmine framework," *Comput. Netw.*, vol. 53, no. 6, pp. 774–789, Apr. 2009. [Online]. Available: <http://dx.doi.org/10.1016/j.comnet.2008.12.011>
- [94] E. Baralis, L. Cagliero, T. Cerquitelli, V. D'Elia, and P. Garza, "Expressive generalized itemsets," *Information Sciences*, vol. 278, pp. 327–343, 2014.
- [95] T. Karagiannis, K. Papagiannaki, and M. Faloutsos, "Blinc: multilevel traffic classification in the dark." in *SIGCOMM*, 2005, pp. 229–240.
- [96] J. Ertman, M. Arlitt, and A. Mahanti, "Traffic classification using clustering algorithms," in *MineNet '06*, 2006, pp. 281–286.
- [97] P.-N. Tan, M. Steinbach, and V. Kumar, *Introduction to Data Mining, (First Edition)*. Addison-Wesley Longman Publishing Co., Inc., 2005.
- [98] R. Srikant and R. Agrawal, "Mining generalized association rules," in *VLDB 1995*, 1995, pp. 407–419.
- [99] E. Baralis, L. Cagliero, T. Cerquitelli, V. D'Elia, and P. Garza, "Support driven opportunistic aggregation for generalized itemset extraction," in *IEEE Conf. of Intelligent Systems*, 2010, pp. 102–107.
- [100] E. Baralis, L. Cagliero, T. Cerquitelli, S. Chiusano, and P. Garza, "Frequent weighted itemset mining from gene expression data," in *BIBE*, 2013, pp. 1–4.
- [101] L. Cagliero, T. Cerquitelli, P. Garza, and L. Grimaudo, "Misleading generalized itemset discovery," *Expert Syst. Appl.*, vol. 41, no. 4, pp. 1400–1410, 2014.
- [102] K. Sriphaew and T. Theeramunkong, "A new method for finding generalized frequent itemsets in association rule mining," in *Proceeding of the VII Intern. Symposium on Computers and Communications*, 2002, pp. 1040–1045.
- [103] E. Baralis, L. Cagliero, T. Cerquitelli, and P. Garza, "Generalized association rule mining with constraints," *Inf. Sci.*, vol. 194, pp. 68–84, 2012.
- [104] J. Han and Y. Fu, "Mining multiple-level association rules in large databases," *IEEE Transactions on knowledge and data engineering*, vol. 11, no. 7, pp. 798–805, 1999.
- [105] D. Kunkle, D. Zhang, and G. Cooperman, "Mining frequent generalized itemsets and generalized association rules without redundancy," *J. Comput. Sci. Technol.*, vol. 23, no. 1, pp. 77–102, 2008.

- [106] L. Cagliero, “Discovering temporal change patterns in the presence of taxonomies,” *IEEE Trans. Knowl. Data Eng.*, vol. 25, no. 3, pp. 541–555, 2013.
- [107] M. Barsky, S. Kim, T. Weninger, and J. Han, “Mining flipping correlations from large datasets with taxonomies,” *Proc. VLDB Endow.*, vol. 5, no. 4, pp. 370–381, Dec. 2011.
- [108] T. Wu, Y. Chen, and J. Han, “Re-examination of interestingness measures in pattern mining: a unified framework,” *Data Min. Knowl. Discov.*, vol. 21, no. 3, pp. 371–397, Nov. 2010.
- [109] J. Dean and S. Ghemawat, “Mapreduce: simplified data processing on large clusters,” *Commun. ACM*, vol. 51, no. 1, pp. 107–113, Jan. 2008.
- [110] L. Grimaudo, M. Mellia, and E. Baralis, “Hierarchical learning for fine grained internet traffic classification,” in *Wireless Communications and Mobile Computing Conference (IWCMC), 2012 8th International*. IEEE, 2012, pp. 463–468.
- [111] C.-C. Chen, C.-Y. Tseng, and M.-S. Chen, “Highly scalable sequential pattern mining based on mapreduce model on the cloud,” in *Big Data (BigData Congress), 2013 IEEE International Congress on*. IEEE, 2013, pp. 310–317.
- [112] J.-W. Huang, S.-C. Lin, and M.-S. Chen, “Dpsp: Distributed progressive sequential pattern mining on the cloud,” *Advances in Knowledge Discovery and Data Mining*, pp. 27–34, 2010.
- [113] Y.-q. Wei, D. Liu, and L.-s. Duan, “Distributed prefixspan algorithm based on mapreduce,” in *Information Technology in Medicine and Education (ITME), 2012 International Symposium on*, vol. 2. IEEE, 2012, pp. 901–904.
- [114] D. Yu, W. Wu, S. Zheng, and Z. Zhu, “Bide-based parallel mining of frequent closed sequences with mapreduce,” *Algorithms and Architectures for Parallel Processing*, pp. 177–186, 2012.
- [115] I. Miliaraki, K. Berberich, R. Gemulla, and S. Zoupanos, “Mind the gap: Large-scale frequent sequence mining,” in *Proceedings of the 2013 ACM SIGMOD International Conference on Management of Data*. ACM, 2013, pp. 797–808.